

# Information Organization Algorithms

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## Abstract

*In this paper we present a system for static and dynamic information organization and show our evaluations of this system on TREC data. We introduce the off-line and on-line star clustering algorithms for information organization. Our evaluation experiments show that the off-line star algorithm outperforms the single link and average link clustering algorithms. Since the star algorithm is also highly efficient and simple to implement, we advocate its use for tasks that require clustering, such as information organization, browsing, filtering, routing, topic tracking, and new topic detection.*

## 1 Introduction

Modern information systems have vast amounts of unorganized data that change dynamically. Consider, for example, the flow of information that arrives continuously on news wires, or is aggregated by a news organization such as CNN. Some stories are new while other stories are follow-ups on previous stories. Yet another type of stories make previous reportings obsolete. The news focus changes regularly with this flow of information. In such dynamic systems, users need to locate information quickly and efficiently.

Current information systems such as Inquiry [Tur90], Smart [Sal91] and Alta Vista provide some simple automation by computing ranked (sorted) lists of documents, but it is ineffective for users to scan a list of hundreds of document titles. To cull the critical information out of a large set of potentially useful dynamic sources, we need methods for organizing information to highlight the topic content of a collection and reorganize the data to adapt to the incoming flow of documents. Such information organization algorithms would support incremental information processing tasks such as routing, topic tracking and new topic detection in a stream of documents.

In this paper, we present a system for the static and dynamic organization of information and we evaluate

the system on TREC data. We introduce the off-line and on-line star clustering algorithms for information organization. We also describe a novel method for visualizing clusters, by embedding them in the plane so as to capture their relative difference in content. Our evaluation experiments show that the off-line star algorithm outperforms the single link and average link clustering algorithms. Since the star algorithm is also highly efficient and simple to implement, we advocate its use for tasks that require clustering, such as information organization, routing, topic tracking, and new topic detection.

### 1.1 Previous Work

There has been extensive research on clustering and applications to many domains. For a good overview see [JD88]. For a good overview of using clustering in information retrieval see [Wil88].

The use of clustering in information retrieval was mostly driven by *the cluster hypothesis* [Rij79] which states that relevant documents tend to be more closely related to each other than to non-relevant documents. Efforts have been made to determine whether the cluster hypothesis is valid. Voorhees [Voo85] discusses a way of evaluating whether the cluster hypothesis holds and shows negative results. Jardine and van Rijsbergen [JR71] show some evidence that search results could be improved by clustering. Hearst and Pedersen [HP96] re-examine the cluster hypothesis by focusing on the Scatter/Gather system [CKP93] and conclude that it holds for browsing tasks.

Systems like Scatter/Gather [CKP93] provide a mechanism for user-driven organization of data into a fixed number of clusters, but user feedback is required and the computed clusters do not have accuracy guarantees. Scatter/Gather uses fractionation to compute nearest-neighbor clusters. In a recent paper, Charika et al. [CCFM97] consider a dynamic clustering algorithm to partition a collection of text documents into a fixed number of clusters. However, since the num-

ber of topics in a dynamic information systems is not generally known *a priori*, a fixed number of clusters cannot generate a natural partition of the information.

## 1.2 Our Work

Our work on clustering presented in this paper and in [APR99] describes a simple incremental algorithm, provides positive evidence for the cluster hypothesis, and shows promise for on-line tasks that require dynamically adjusting the topic content of a collection such as filtering, browsing, new topic detection and topic tracking. We propose an off-line algorithm for clustering static information and an on-line version of this algorithm for clustering dynamic information. These two algorithms compute clusters induced by the natural topic structure of the space. Thus, this work is different than [CKP93, CCFM97] in that we do not impose a fixed number of clusters as a constraint on the solution. As a result, we can guarantee a lower bound on the topic similarity between the documents in each cluster.

To compute accurate clusters, we formalize the clustering problem as one of covering a thresholded similarity graph by cliques. Covering by cliques is NP-complete and thus intractable for large document collections. Recent graph-theoretic results have shown that the problem cannot even be approximated in polynomial time [LY94, Zuc93]. We instead use a cover by dense subgraphs that are star-shaped<sup>1</sup>, where the covering can be computed off-line for static data and on-line for dynamic data. We show that the off-line and on-line algorithms produce high-quality clusters very efficiently. Asymptotically, the running time of both algorithms is roughly linear in the size of the similarity graph that defines the information space. We also derive lower bounds on the topic similarity within clusters guaranteed by a star covering, thus providing theoretical evidence that the clusters produced by a star cover are of high-quality. We packaged these algorithms as a system that supports ad-hoc queries, static information organization, dynamic information organization, and routing. In this system we contributed a novel way of visualizing topic clusters by using disks whose radii are proportional to the size of the cluster and that are embedded in the plane in a way that captures the topic distance between the clusters. Finally, we provide experimental data for off-line and on-line topic organization. In particular, our off-line results on a TREC collection indicate that star covers exhibit significant performance improvements over either the single link [Cro77] or

average link [Voo85] methods (21.6% and 16.2% improvements, respectively, with respect to a common cluster quality measure) without sacrificing simplicity or efficiency.

## 2 Off-line Information Organization

In this section, we begin by presenting an efficient algorithm for off-line organization of information. We then describe our system built around this algorithm, including user interface design and visualization techniques. Finally, we present a performance evaluation of our organization algorithm. We begin by examining the organization problem and introducing the star algorithm.

### 2.1 The Star Algorithm

We formalize our problem by representing an information system by its *similarity graph*. A similarity graph is an undirected, weighted graph  $G = (V, E, w)$  where vertices in the graph correspond to documents and each weighted edge in the graph corresponds to a measure of similarity between two documents. We measure the similarity between two documents by using the cosine metric in the vector space model of the Smart information retrieval system [Sal91].

$G$  is a complete graph with edges of varying weight. An organization of the graph that produces reliable clusters of similarity  $\sigma$  (*i.e.*, clusters where documents have pairwise similarities of at least  $\sigma$ ) can be obtained by first thresholding the graph at  $\sigma$  and then performing a *minimum clique cover* with maximal cliques on the resulting graph  $G_\sigma$ . The *thresholded graph*  $G_\sigma$  is an undirected graph obtained from  $G$  by eliminating every edge whose weight is lower than  $\sigma$ . The minimum clique cover has two features. First, by using cliques to cover the similarity graph, we are guaranteed that all the documents in a cluster have the desired degree of similarity. Second, minimal clique covers with maximal cliques allow vertices to belong to *several* clusters. In our information retrieval application this is a desirable feature as documents can have multiple subthemes. However, the algorithm can also be used to compute non-overlapping clusters. In our experimental evaluations (see Figure 3) we show that the difference in results between star with overlapping clusters and star without overlapping clusters is very small.

Unfortunately, this approach is not tractable computationally. For real corpora, similarity graphs can be very large. The clique cover problem is NP-complete, and it does not admit polynomial-time approximation algorithms [LY94, Zuc93]. While we cannot perform a clique cover nor even approximate such

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<sup>1</sup>In [SJ70] stars were also identified to be potentially useful for clustering.

a cover, we can instead cover our graph by *dense subgraphs*. What we lose in intra-cluster similarity guarantees, we gain in computational efficiency. In this section and the sections that follow, we describe off-line and on-line covering algorithms and analyze their performance and efficiency.

We approximate a clique cover by covering the associated thresholded similarity graph with *star-shaped subgraphs*. A star-shaped subgraph on  $m + 1$  vertices consists of a single *star center* and  $m$  *satellite vertices*, where there exist edges between the star center and each of the satellite vertices. While finding cliques in the thresholded similarity graph  $G_\sigma$  guarantees a pairwise similarity between documents of at least  $\sigma$ , it would appear at first glance that finding star-shaped subgraphs in  $G_\sigma$  would provide similarity guarantees between the star center and each of the satellite vertices, but no such similarity guarantees *between satellite vertices*. However, by investigating the geometry of our problem in the vector space model, we can derive a *lower bound* on the similarity between satellite vertices as well as provide a formula for the *expected* similarity between satellite vertices. The latter formula predicts that the pairwise similarity between satellite vertices in a star-shaped subgraph is high, and together with empirical evidence supporting this formula, we shall conclude that covering  $G_\sigma$  with star-shaped subgraphs is a reliable method for clustering a set of documents.

The star algorithm is based on a greedy cover of the thresholded similarity graph by star-shaped subgraphs; the algorithm itself is summarized in Figure 1. The star algorithm is very efficient. In [APR99] we show that the star algorithm can be correctly implemented in such a way that given a thresholded similarity graph  $G_\sigma$ , the running time of the algorithm is  $\Theta(V + E_\sigma)$ , linear in the size of the input graph.

## 2.2 Cluster Quality

In this section, we argue that the clusters produced by a star cover have high average intra-cluster similarity weights; thus, the clusters produced are accurate and of high quality. Consider three documents  $C$ ,  $S_1$  and  $S_2$  which are vertices in a star-shaped subgraph of  $G_\sigma$ , where  $S_1$  and  $S_2$  are satellite vertices and  $C$  is the star center. By the definition of a star-shaped subgraph of  $G_\sigma$ , we must have that the similarity between  $C$  and  $S_1$  is at least  $\sigma$  and that the similarity between  $C$  and  $S_2$  is also at least  $\sigma$ . In the vector space model, these similarities are obtained by taking the cosine of the angle between the vectors associated with each document. Let  $\alpha_1$  be the angle between  $C$  and  $S_1$ , and let  $\alpha_2$  be the angle between  $C$  and  $S_2$ . We then

For any threshold  $\sigma$ :

1. Let  $G_\sigma = (V, E_\sigma)$  where  $E_\sigma = \{e : w(e) \geq \sigma\}$ .
2. Let each vertex in  $G_\sigma$  initially be *unmarked*.
3. Calculate the degree of each vertex  $v \in V$ .
4. Let the highest degree unmarked vertex be a star center and construct a cluster from the star center and its associated satellite vertices. Mark each node in the newly constructed cluster.
5. Repeat step 4 until all nodes are marked.
6. Represent each cluster by the document corresponding to its associated star center.

Figure 1: The star algorithm

have that  $\cos \alpha_1 \geq \sigma$  and  $\cos \alpha_2 \geq \sigma$ . Note that the angle between  $S_1$  and  $S_2$  can be at most  $\alpha_1 + \alpha_2$ , and therefore we have the following lower bound on the similarity between satellite vertices in a star-shaped subgraph of  $G_\sigma$ .

**Theorem 1** *Let  $G_\sigma$  be a similarity graph and let  $S_1$  and  $S_2$  be two satellites in the same star in  $G_\sigma$ . If  $\alpha_1 \geq \sigma$  and  $\alpha_2 \geq \sigma$  are the respective similarities between  $S_1$  and the star center and between  $S_2$  and the star center, then the similarity between  $S_1$  and  $S_2$  must be at least*

$$\cos(\alpha_1 + \alpha_2) = \cos \alpha_1 \cos \alpha_2 - \sin \alpha_1 \sin \alpha_2.$$

If  $\sigma = 0.7$ ,  $\cos \alpha_1 = 0.75$  and  $\cos \alpha_2 = 0.85$ , for instance, we can conclude that the similarity between the two satellite vertices must be at least<sup>2</sup>

$$(0.75) \cdot (0.85) - \sqrt{1 - (0.75)^2} \sqrt{1 - (0.85)^2} \approx 0.29.$$

While this may not seem very encouraging, the above analysis is based on absolute worst-case assumptions, and in practice, the similarities between satellite vertices are much higher. We further undertook a study to determine the *expected* similarity between two satellite vertices. Under the assumption that “similar” documents are essentially “random” perturbations of one another in an appropriate vector space, we have proven the following [APR99]:

<sup>2</sup>Note that  $\sin \theta = \sqrt{1 - \cos^2 \theta}$ .

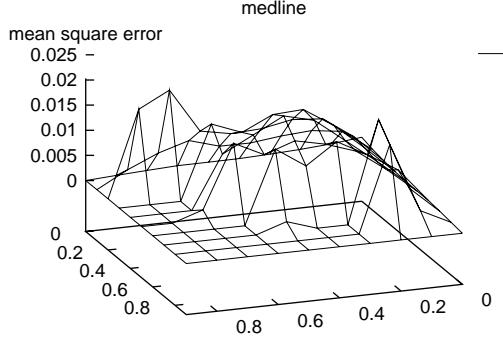


Figure 2: This figure shows the actual mean-squared prediction error for a 6,000 abstract subset of MEDLINE.

**Theorem 2** Let  $G_\sigma$  be a similarity graph and let  $S_1$  and  $S_2$  be two satellites in the same star in  $G_\sigma$ . If  $\alpha_1 \geq \sigma$  and  $\alpha_2 \geq \sigma$  are the respective similarities between  $S_1$  and the star center and between  $S_2$  and the star center, then the expected similarity between  $S_1$  and  $S_2$  is

$$\cos \alpha_1 \cos \alpha_2 + \frac{\sigma}{1 + \sigma} \sin \alpha_1 \sin \alpha_2.$$

For the previous example, the above formula would predict a similarity between satellite vertices of approximately 0.78. We have tested this formula against real data, and the results of the test with the MEDLINE data set are shown in Figure 2. In this plot, the  $x$ - and  $y$ -axes are similarities between a cluster center and each of two satellite vertices, and the  $z$ -axis is the actual mean squared prediction error of the above formula for the similarity between satellite vertices. Note that the root mean square error (RMS) is quite small (approximately 0.13 in the worst case), and for reasonably high similarities, the error is negligible. From our tests with real data, we have concluded that this formula is quite accurate and that star-shaped subgraphs are reasonably “dense” in the sense that they imply relatively high pairwise similarities between documents.

### 2.3 Performance Comparison with Two Clustering Algorithms

In order to evaluate the performance of our system, we tested the star algorithm against two classic clustering algorithms: the single link method [Cro77] and the average link method [Voo85]. We used data from the TREC-6 conference as our testing medium.

The TREC collection contains a set of 130,471 documents of which 21,694 have been ascribed relevance data with respect to 47 topics. These 21,694 documents were partitioned into 22 separate subcollections of approximately 1,000 documents each. Within a subcollection, each of the 47 topics has a corresponding subset of documents which is relevant to that topic.

The goal of a clustering method is to organize the set of documents in such a way that the subset of documents corresponding to a selected topic appears as a cluster in the organization. For each of the subcollections, we performed the following experiment. Given a selected topic, the set of documents was organized by a clustering method in question, and the “best” cluster corresponding to this topic was returned. Two issues immediately arise: first, how does one measure the “quality” of a cluster to determine which is “best”; and second, how does one appropriately generate clusters from which to choose. To measure the quality of a cluster, we use the common  $E$  measure [Rij79] as defined below

$$E(p, r) = 1 - \frac{2}{1/p + 1/r}$$

where  $p$  and  $r$  are the standard *precision* and *recall* of the cluster with respect to the set of documents relevant to the topic. Note that  $E(p, r)$  is simply one minus the harmonic mean of the precision and recall; thus,  $E(p, r)$  ranges from 0 to 1 where  $E(p, r) = 0$  corresponds to perfect precision and recall and  $E(p, r) = 1$  corresponds to zero precision and recall. It is worthwhile to note that when viewing data comparing two clustering methods, lower  $E(p, r)$  values correspond to *better* performance. In order to compare the clustering methods fairly, each of the methods was run in such a way so as to produce the “best” possible cluster with respect to a given topic, as defined by the  $E(p, r)$  measure above. (This is in keeping with previous comparative analyses of clustering methods; see, for example, Burgin [Bur95] and Shaw [Sha93].) In the case of the single link and star cover algorithms, the algorithms were run using a range of thresholds, and the best cluster obtained over all thresholds was returned. (One can view the clustering obtained with respect to a given threshold as a “slice” within a hierarchical clustering over all thresholds; thus, in effect, the best cluster in the hierarchy was returned in these experiments.) In the case of the average-link algorithm which naturally produces a hierarchical clustering, the best cluster within the hierarchy was returned.

Unlike the star algorithm, single and average link algorithms do not allow overlapping clusters. It has

been suggested that the differences in performance may be attributed to the effects of overlapping rather than to the actual properties of the algorithm. To investigate this issue we conducted the same experiments using a version of the star clustering algorithm that eliminates the overlapping clusters. In this setting we used the star algorithm to find a set of star centers, then partitioned a collection by assigning a document to the closest star center. This methodology has been used before [JD88]. We note that the difference in results between star with overlapping clusters and star without overlapping clusters is very small. Both algorithms still outperform single link and average link (See Figure 3).

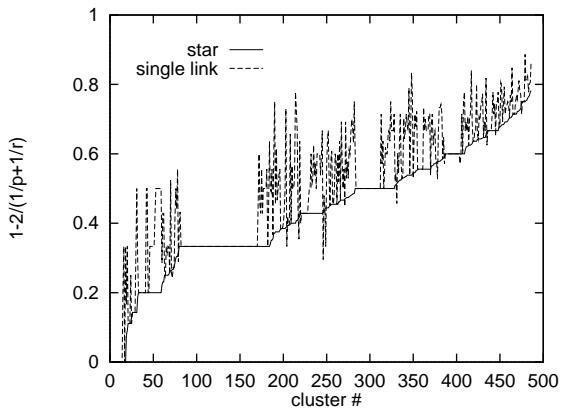


Figure 4: This figure shows the  $E(p, r)$  measure for the partitioning star clustering algorithm and for the single link clustering algorithm. The  $y$  axis shows the  $E(p, r)$  measure, while the  $x$  axis shows the cluster number. Clusters have been sorted according to the  $E(p, r)$  values of the star algorithm.

Each subcollection of 1,000 documents corresponded to an individual experiment. For a given clustering method, the appropriate algorithm was employed to determine the best possible cluster (as defined by the  $E(p, r)$  measure) for each of the 47 topics. For each optimal cluster, the  $E(p, r)$ , precision and recall values were calculated with respect to the actual set of documents relevant to the topic, and these values were averaged over all topics to obtain the three numbers reported for each experiment and clustering method in Figure 3. Averaging over all 22 experiments, we find that the mean  $E(p, r)$  values for star, partitioning star, average link and single link are 0.37, 0.39, 0.43 and 0.45, respectively. Thus, the star algorithm represents a 16.2% improvement in performance

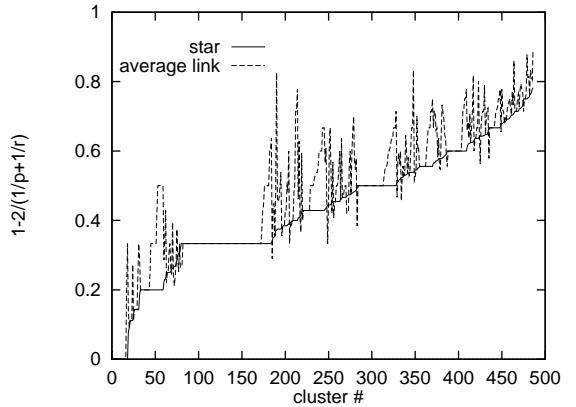


Figure 5: This figure shows the  $E(p, r)$  measure for the partitioning star clustering algorithm and for the average link clustering algorithm. The  $y$  axis shows the  $E(p, r)$  measure, while the  $x$  axis shows the cluster number. Clusters have been sorted according to the  $E(p, r)$  values of the star algorithm.

with respect to average link and an 21.6% improvement with respect to single link. The difference is only partly due to the effect of allowing overlapping clusters - the partitioning star algorithm still gives us a 10.2% and 15.4% improvement in performance over average link and single link respectively.

We repeated this experiment on the same data, using one collection only (of 21,694 documents.) The precision, recall, and  $E$  values for star (overlap), star, average link, and single link were (.52, .36, .58), (.53, .32, .61), (.63, .25, .64), and (.66, .20, .70) respectively. We note that the  $E$  measures are worse for all four algorithms on this larger collection and that the star algorithm outperforms average link by 10.3% and single link by 20.7%.

Figures 4 and 5 show detailed  $E(p, r)$  values for the star algorithm vs. the single link algorithm and for the star algorithm vs. the average link algorithm over the collection of experiments. Each cluster computed by the algorithm has an  $E(p, r)$  value. For better readability of these graphs, we sorted the clusters produced by the star algorithm according to their  $E(p, r)$  values. We plotted the corresponding  $E(p, r)$  values for the single link algorithm (see the oscillating line in Figure 4) and for the average link algorithm (see the oscillating line in Figure 5). We note that the  $E(p, r)$  values for the star clusters are almost everywhere lower than the corresponding values for the single link and average link algorithms; thus, the star algorithm out-

coll	star (overlap)			star (partition)			average link			single link		
	p	r	E	p	r	E	p	r	E	p	r	E
1	0.78	0.56	0.35	0.79	0.53	0.36	0.74	0.50	0.40	0.77	0.47	0.41
2	0.74	0.59	0.35	0.70	0.55	0.38	0.88	0.43	0.43	0.88	0.41	0.44
3	0.78	0.53	0.37	0.79	0.48	0.41	0.84	0.44	0.43	0.83	0.43	0.43
4	0.76	0.50	0.40	0.81	0.46	0.41	0.71	0.46	0.44	0.73	0.41	0.48
5	0.80	0.50	0.38	0.78	0.50	0.39	0.85	0.40	0.46	0.81	0.40	0.46
6	0.76	0.41	0.47	0.68	0.45	0.46	0.78	0.39	0.48	0.83	0.34	0.51
7	0.76	0.62	0.32	0.79	0.61	0.31	0.81	0.52	0.36	0.78	0.50	0.39
8	0.75	0.57	0.35	0.73	0.57	0.36	0.82	0.48	0.39	0.86	0.44	0.42
9	0.82	0.49	0.39	0.80	0.50	0.38	0.89	0.44	0.41	0.87	0.43	0.43
10	0.74	0.52	0.39	0.79	0.46	0.42	0.85	0.42	0.44	0.87	0.38	0.47
11	0.82	0.55	0.34	0.86	0.48	0.38	0.83	0.45	0.42	0.85	0.44	0.42
12	0.80	0.55	0.35	0.83	0.53	0.36	0.82	0.49	0.38	0.83	0.40	0.46
13	0.81	0.53	0.36	0.81	0.49	0.39	0.84	0.46	0.40	0.89	0.40	0.44
14	0.76	0.47	0.42	0.73	0.46	0.43	0.86	0.36	0.50	0.91	0.31	0.54
15	0.75	0.54	0.37	0.79	0.48	0.40	0.83	0.35	0.50	0.87	0.33	0.52
16	0.87	0.47	0.39	0.86	0.46	0.40	0.91	0.40	0.45	0.95	0.39	0.45
17	0.64	0.53	0.42	0.64	0.51	0.43	0.80	0.39	0.48	0.76	0.39	0.48
18	0.77	0.56	0.35	0.81	0.51	0.37	0.79	0.53	0.36	0.81	0.48	0.40
19	0.73	0.54	0.38	0.74	0.50	0.40	0.83	0.42	0.45	0.85	0.39	0.46
20	0.71	0.51	0.41	0.76	0.48	0.41	0.81	0.41	0.45	0.86	0.36	0.49
21	0.74	0.61	0.33	0.79	0.56	0.34	0.84	0.49	0.38	0.88	0.46	0.40
22	0.76	0.63	0.31	0.80	0.60	0.32	0.83	0.47	0.40	0.85	0.46	0.40
avg	0.77	0.54	0.37	0.78	0.51	0.39	0.83	0.44	0.43	0.84	0.41	0.45

Figure 3: This figure shows comparison data for the star algorithm, the partitioning star algorithm, the single link algorithm, and the average link algorithm for 22 subcollections of TREC documents. For each algorithm,  $p$  represents the average precision computed across all clusters found for the collection;  $r$  represents the average recall computed across all clusters found for the collection; and  $E(p, r)$  is the aggregate measure  $1 - \frac{2}{1/p+1/r}$ .

performs these two methods.

These experiments show that the star algorithm outperforms the single link and average link methods. Since the star algorithm is also simple to implement and highly efficient, we believe that the star algorithm is very effective for information organization and other text clustering applications.

### 3 On-line Information Organization

In this section we consider algorithms for computing the organization of a dynamic information system. We derive an on-line version of the star algorithm for information organization that can incrementally compute clusters of similar documents. We continue assuming the vector space model and the cosine metric to capture the pairwise similarity between the documents of the corpus.

#### 3.1 The On-line Star Algorithm

We assume that documents are inserted or deleted from the collection one at a time. For simplicity, we will focus our discussion on adding documents to the collection. The delete algorithm is similar. The intuition behind the incremental computation of the star cover of a graph after a new vertex is inserted is depicted in Figure 6. The top figure denotes a thresholded similarity graph and a correct star cover for this graph. Suppose a new vertex is inserted in the graph, as in the middle figure. The original star cover is no longer correct for the new graph. The bottom figure shows the correct star cover for the new graph. How

does the addition of this new vertex affect the correctness of the star cover? In general, the answer depends on the degree of the new vertex and on its adjacency list. If the adjacency list of the new vertex does not contain any star centers, the new vertex can be added in the star cover as a star center. If the adjacency list of the new vertex contains any center vertex  $c$  whose degree is higher, the new vertex becomes a satellite vertex of  $c$ . The difficult case that destroys the correctness of the star cover is when the new vertex is adjacent to a collection of star centers, each of whose degree is lower than that of the new vertex. In this situation, the star structure already in place has to be modified to assign the new vertex as a star center. The satellite vertices in the stars that are broken as a result have to be re-evaluated.

Motivated by the intuition in the previous paragraph, we have developed an on-line algorithm for incrementally computing star covers of dynamic graphs [APR99]. In this paper we have shown that the star cover produced by the on-line star algorithm is correct in that it is identical to the star cover produced by the off-line algorithm (or one of the correct covers, if more than one exists) [APR99]. Furthermore, the on-line star algorithm is very efficient. In our initial tests, we have implemented the on-line star algorithm using a heap for the priority queue and simple linked lists for the various lists required. The time required to insert a new vertex and associated edges into a thresholded similarity graph and to appropriately update the star

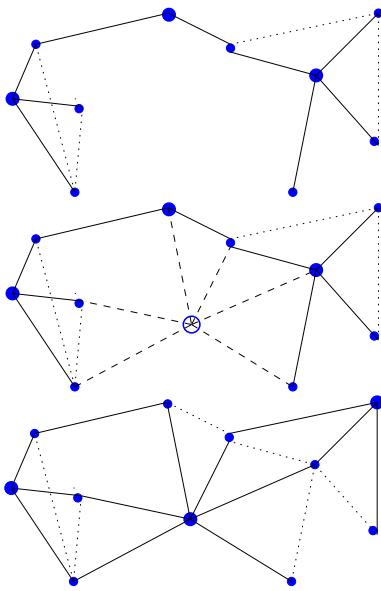


Figure 6: This figure shows the star cover change after the insertion of a new vertex. The larger-radius disks denote star centers, the other disks denote satellite vertices. The star edges are denoted by solid lines. The inter-satellite edges are denoted by dotted lines. The top figure shows an initial graph and its star cover. The middle figure shows the graph after the insertion of a new document. The bottom figure shows the star cover of the new graph.

cover is largely governed by the number of stars that are broken during the update, since breaking stars requires inserting new elements into the priority queue. In practice, very few stars are broken during any given update (see Figure 7). This is due partly to the fact that relatively few stars exist at any given time (as compared to the number of vertices or edges in the thresholded similarity graph) and partly to the fact that the likelihood of breaking any individual star is also small [APR99].

We evaluated the on-line star cover algorithm on a 2224 document corpus consisting of a judged subcollection of TREC documents augmented with our department's technical reports. We ran 4 experiments. Each time we selected a different threshold and proceeded to insert the 2224 documents in random order, using the on-line star cluster algorithm. The results of these experiments were averaged. The running time measurements appear to be linear in the number of edges of the similarity graph. Figures 7 and 8 show the experimental data. Note that the number of bro-

ken stars is roughly linear in the number of vertices, the running time is linear in the number of edges in the graph, although we can see the effects of lower order terms.

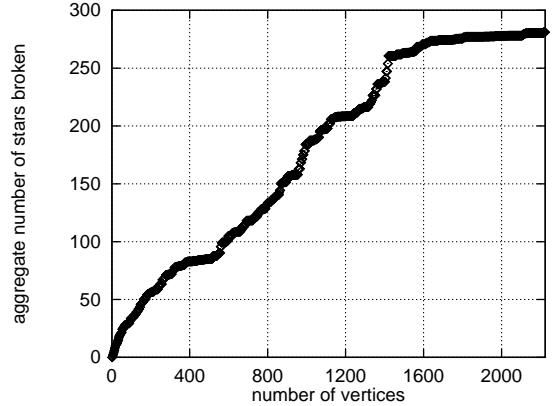


Figure 7: The dependence of number of broken stars on the number of vertices for TREC data.

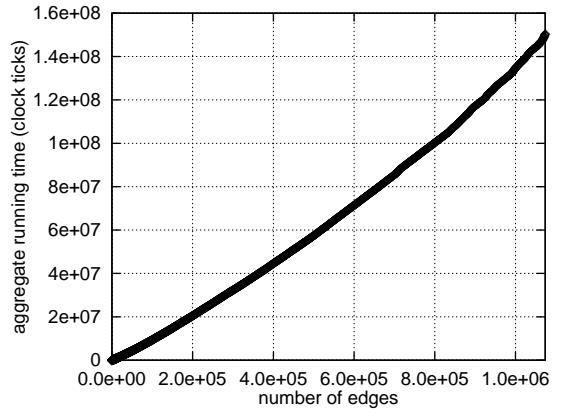


Figure 8: This figure shows the dependence of the running time of the on-line star algorithm on the number of edges in a TREC subcollection.

## 4 Applications to Filtering

Filtering is the task of selecting from an incoming stream of documents those relevant to a query. Typically, the filtering system decides whether a new document is relevant instantly, without waiting for the subsequent documents to arrive. The user may correct the *filtering profile* by providing relevance feedback on the retrieved documents.

## 4.1 Filtering algorithms

We use the topic clusters computed with the star algorithm and relevance feedback information to deduce the relevancy of a new document. Our cluster-based approach to document filtering is based on the premise that the similarity between a new document and a star center that corresponds to a given topic approximates well the relevance of the document to the topic. We base this assertion on the following observations:

- the cluster hypothesis (“closely related documents are relevant to the same queries”);
- the star clustering algorithm finds accurate clusters; and
- a cluster obtained with the star clustering algorithm is well-represented by the document at the star center.

Thus, we define the following rules for determining the relevancy of a document based on the relevancy the cluster center:

1. A document is relevant if its adjacent center is relevant.
2. A document is not relevant if its adjacent center is not relevant.

These rules result in the following algorithm for filtering:

1. Select clustering threshold.
2. Cluster documents using the star algorithm.
3. Obtain initial relevancy information.
4. For each new document:
5. Add the document to the clustering using the star algorithm Update procedure [APR99].
6. Decide whether the document is relevant based on its cluster membership.
7. Retrieve the document, if relevant; correct relevance information based on the user’s input.

An implementation of a filtering system based in this algorithm needs to address the following points:

- Which threshold parameter for clustering to select?
- How to obtain the relevance feedback?
- How to resolve undefined cases when deciding document relevancy?

We explore the performance of this filtering system in the next section.

## 4.2 Filtering Evaluation

The TREC filtering track experimented with different evaluation measures over the years. For administrative and practical reasons, the TREC filtering task uses utility measures F1 and F3 (see Table 1). Precision and recall based measures were discarded because of their inability to differentiate between systems that return no relevant documents (where clearly returning no documents at all is a much better behavior than returning a great number of non-relevant documents).

	Relevant	Not Relevant
Retrieved	$R^+$	$N^+$
Not Retrieved	$R^-$	$N^-$
$F1$	$= 3R^+ - 2N^+$	
$F3$	$= 4R^+ - N^+$	

Table 1: Utility measures.

The drawback of these utility measures is that they cannot be meaningfully averaged over all topics. Furthermore, these (and other) utility measures place equal value on all relevant documents. An example cited in the TREC-7 filtering report points out that the 1000th retrieved relevant document likely will provide no new content over the previous 999 relevant documents, and should therefore be valued less than the others. One can similarly argue about the relative importance of the 998th relevant document, and so on. It is not only the fact that we already have many relevant documents that makes a new relevant document potentially uninteresting, but the actual *content similarity* of this document to the previous ones.<sup>3</sup> Unfortunately, current performance measures do not take content retrieval into account. Given a choice of traditional performance measures, we select one such measure ( $F = 2pr/(p + r)$ , where  $p$  is precision and  $r$  is recall) for our experiments. Our preference for this measure is based on the ease of averaging and comparison across the topics, even though we are aware of the limitations of recall-precision based evaluation measures.

We have used the above collections to evaluate the performance of cluster-based filtering. We tested each of the following three procedures with each test col-

<sup>3</sup>In fact, a filtering system that uses clustered organization is well suited to dealing with this problem by separating the documents with new content from the rest. This way, the total number of retrieved relevant documents does not matter, as long as they fit into a small number of topics.

lection.

**Filtering around the topic centroid.** In this method, we take a set consisting of all training relevant documents for a topic, find the centroid of this set, and the minimum similarity between the centroid and vectors in the set. Select documents from the test set which similarity to the centroid is no less than the minimum similarity established on the training set. Compare the selected set of documents to the set of relevant test documents using  $F = 2pr/(p + r)$  measure. We will refer to this method by *CENT*, and look at two variations. In the first variation called *static*, we use the centroid and the best threshold from the training collection throughout the filtering experiments. In the second variation, called *moving*, we adjust the centroid with each new relevant document added.

**Filtering using the optimal cluster in a topic.** In this method, we take a set consisting of all training relevant documents for a topic, for every possible threshold find all clusters in this set using the star algorithm. A document from the test set is selected if its similarity to a cluster center is no less than the threshold used to obtain the clustering. Compare the selected set of documents to the set of relevant test documents using  $F = 2pr/(p + r)$  measure, find the threshold that maximizes  $F$ . We will refer to this method by *CLUS*, and look at two variations. In the first variation called *static*, we use the centroid of the best cluster from the training collection throughout the filtering experiments. In the second variation, called *moving*, we adjust the centroid with each new relevant document added.

**Filtering using the star algorithm.** In this method, a new document is added to the clustering using the star algorithm Update procedure. If the new document is not at the center of a new cluster, then it is relevant if all its adjacent cluster centers are relevant. If the new document is at the cluster center, it is relevant if 75% of its adjacent vertices are relevant. We will refer to this method by *STAR*.

Figure 2 presents the results from the five experiments outlined above on the three test collections. We describe the performance of each algorithm as the average  $F$ -measure, where  $F$  is averaged over all topics. Thus, the higher the  $F$  value, the better the performance. We observe that the moving methods outperform the static methods and that the cluster methods outperform the centroid methods. Furthermore, the method based on the star algorithm has the best

	static CENT	moving CENT	static CLUS	moving CLUS	STAR
FBIS	.230	.263	.243	.285	.294
AP	.257	.285	.260	.302	.310
News	.842	.893	.904	.907	.907

Table 2: This tables shows the best  $F_{avg}$  achieved by each of the three filtering algorithms described above (with two variations for the centroid (CENT) and cluster (CLUS) algorithms) over several filtering thresholds.

performance. Thus, we conclude that clustering, and especially the star algorithm are useful in improving the performance of the filtering task.

## 5 Discussion

We have presented, analyzed, and evaluated the star clustering algorithm for information organization. We described an off-line version of this algorithm that can be used to organize static information in accurate clusters efficiently. We also described an on-line version of the algorithm that can be used to organize dynamic data for tasks that require incremental updates in the topic structure of the corpus, such as the routing task, the new topic detection task, and the topic tracking task.

Our implementation of this algorithm contributes a novel visualization method for clusters that presents users with disks whose radii correspond to the cluster size and that are embedded in the plane so as to capture the topic distance between the clusters.

We evaluated the star algorithm by comparing it against the single link and the average link algorithms in several experiments with TREC data. We found that the star algorithm outperforms the single link algorithm and the average link algorithm. Since the star algorithm is faster and easier to implement and than the average link algorithm, we advocate its use. The on-line algorithm produces the same clustering as the off-line algorithm. Thus, our evaluation of the off-line star algorithm also suggests using the on-line star algorithm for tasks that require computing the topic structure incrementally and adaptively.

Our findings so far suggest using the star algorithm for a variety of tasks. We are currently conducting experiments using the on-line star algorithm for new topic detection and topic tracking. Because of its cluster quality, efficiency, and incremental properties, we believe this algorithm will lead to improved results in solving these tasks.

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