

## 9 Homework

**Due:** Thursday, April 4, 2013.

### Problems

**Required:** 4 of the following 5 problems

**Points:** 25 points per problem

1. Do the Problem 5.1

Show that  $EQ_{CFG}$  is undecidable.

2. Do the Problem 5.9

Let  $T = \{ \langle M \rangle \mid M \text{ is a TM that accepts } W^R \text{ whenever it accepts } w \}$ .  
Show that a  $T$  is undecidable.

3. Do the Problem 5.20

Prove that there exists an undecidable subset of  $\{1^*\}$ .

4. Use a mapping reduction to prove that

$DECIDER_{TM} = \{ \langle M \rangle \mid M \text{ is a TM and } M \text{ is a decider} \}$   
is undecidable.

5. Prove that  $REGULAR_{TM}$  (defined on p. 191 of Sipser) is neither Turing-recognizable nor co-Turing-recognizable. *Hint:* For part of this you should create one new mapping reduction.