Name:

Student Id (last 4 digits):

• Write down the answers in the space provided.

• You may use all parts of the Java language we have learned. If you need a method and you don't know whether it is provided, define it. You do not need to include the curly braces for every **if** or every **else**, as long as the statements you write are correct in standard Java.

• For tests you only need to provide the expression that computes the actual value, connecting it with an arrow to the expected value. For example s.method() -> true is sufficient.

• Remember that the phrase "develop a class" or "develop a method" means more than just providing a definition. It means to design them according to the **design recipe**. You are *not* required to provide a method template unless the problem specifically asks for one. However, be prepared to struggle if you choose to skip the template step.

• We will not answer *any* questions during the exam.

Good luck.

Problem	Points	/
1A		/ 8
1B		/ 4
1C		/ 7
1D		/ 7
1E		/ 4
1F		/ 4
1G		/11
1H		/ 5
1I		/10
1J EXTRA		/ 8
Total		/60

Try to solve all problems other than G, I, and J, then work on those, if you have the time.

30 Points

Problem 1

In decoding secret messages it often helps to know the frequency which which each letter of alphabet occurs in a typical text.

A. 8 POINTS

We start by recording the text as an ArrayList of Strings, where each String is just one character.

Design the method allSingles that consumes an ArrayList of Strings and mutates this list so that each item is a String of length 1. If the item was null, it is replaced by a String that represents one blank space. It the item was a String longer than one, it will be replaced by a String that is the first letter of the original String.

B. 4 POINTS

We now want to compute the frequency of all letters in the given ArrayList of Strings of length one.

These frequencies are typically shown as a histogram that records how often each character (including the space) occurs in the given text.

We decided to use the following the data representation for the histogram data, so that you can easily tell how often each letter appears in the text. The histogram is then a simple ArrayList of item of the type LFreq. The number of entries in the ArrayList is equal to the number of distinct letters in the text we are working with. For English language, this would be 27, representing all letter of alphabet and the blank space — if we ignore all other special characters and all digits.

Class LFreq (Letter Frequency):

+----+ | LFreq | +----+ | int freq | | String s | +----+

Make an example of the ArrayList that represents the histogram you would get from the following text:

go on and do great things

You can include only the letters that occur in this text - and the order does not matter. Make sure you include the blank space character.

Hint: You need to build the ArrayList inside a void init()... method.

C. 7 POINTS

Design the (*override*) method equals for the class LFreq that returns true if the two Strings match, even if the freq are different.

Make sure you do everything that is required to properly override the Java equals method.

This page is for your work

D. 7 POINTS

Design the method (in some Algorithms class) computeHisto that computes the histogram for a given text. It consumes the ArrayList of Strings of length one and produces an ArrayList of LFreq items.

Alternately, instead of an ArrayList of LFreq items, you may produce a HashMap of entries where the String will be the key and the frequency will be the value (see the hint 2).

Hint 1: You may assume that all letters of alphabet will be represented, as will be the space. Alternately, you may build the ArrayList that would contain only the letters in the text you are now analyzing (such as our example text go on and do great things).

Hint 2: You may choose to built first a HashMap of entries where the String will be the key and the frequency will be the value. If you do this, you can stop there, you do not need to produce the ArrayList.

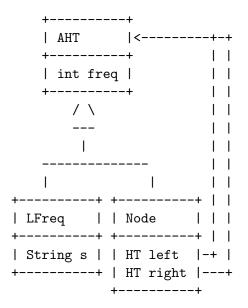
E. 4 POINTS

We need to find out which letter has the highest frequency. To do so, we need a Comparator.

Design the class that implements the Comparator interface by comparing items of the type LFreq, the ordering based on the letter frequencies.

F. 4 POINTS

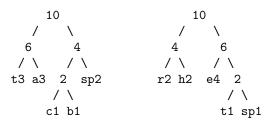
The encoding for each letter in our **String** is given by a binary tree we can build, once we know the frequencies of all letters:



(We explain later how this kind of trees are built.)

Show the representation of the following two trees as an instance of AHT, as they would appear in the Examples class.

(The first tree represents an optimal encoding for the String *cat at bat*, the second one represents an optimal encoding for the String *here there*)



Each leaf node includes the frequency of that letter in the examined text.

Each path from the root of the tree to a leaf can be described as a sequence of choices: *left* or *right*.

A path from the root to the leaf is then a secret encoding of the letter in the leaf.

So, for the first sample tree shown, the path 'left right' leads to the letter a, the path 'right left right' leads to the letter b, and the path 'right right' leads to sp, i.e. the space (that would be represented as String s = ""

G. 11 POINTS

We now describe such path from the root to a leaf as an ArrayList of Boolean values, with true representing the *left* choice and false representing the choice of moving to the *right*.

Design the method whereTo for the classes that implement the interface AHT that consumes an ArrayList of Boolean values that represent the path from the root of the tree to a leaf, and returns the String value of the Leaf reached by this path.

If the path does not lead to a Leaf throw an RuntimeException with a message "Invalid path".

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H. 5 POINTS

The tree we have built (called the *Huffman tree*) has the property that the value of each node is the sum of the values of its left and right children.

Design the method validTree for the AHT class hierarchy that verifies that this tree is a valid *Huffman tree*.

I. 10 POINTS

If we use 0 for false and 1 for true then a String s = "0010', represents the letter t and the String s = "0010', represents the letter t.

Design the method findPath for the AHT classes that consumes a String of length one and produces a String that represents this encoding and ends with the given String.

So, for the input "t'' your first tree would produce the String "Olt", your second tree would produce the String "110t".

J. 8 POINTS EXTRA CREDIT

To design our encoding, David Huffman tells us that we should save the histogram data in a priority queue where the highest priority item is the one with the lowest frequency of occurrence, and then convert it into a *Huffman* tree in a clever way that then defines the encoding for every character in our original **String**.

The only thing you need to know at this point is that the priority queue built from the histogram will contain as data instances of AHT and will use the freq field to determine the priority (defined in some class FreqComp that extends Comparator<AHT>). The lowest freq == the highest priority.

Design the method buildTree that consumes the priority queue we have built and produces the AHT that represents the encoding. It works as follows:

- if the size of the priority queue is empty, no tree can be built and it throws an exception.
- if the size of the priority queue is 1, the priority queue contains just one AHT, and the method removes it from the priority queue and returns it.
- otherwise, the method removes the two items with the highest priority and adds to the priority queue a new AHT that has the two removed AHTs as its left and right subtrees.

The documentation for the needed methods for the JavaPriorityQueue is attached.

The method **buildPQ** shown below has been used to build the initial priority queue.

```
// insert the letter frequency data into a priority queue
// produce an priority queue of LFreq data
public PriorityQueue<AHT> buildPQ(ArrayList<LFreq> lfreqList){
    PriorityQueue<AHT> pq = new PriorityQueue<AHT>(20, new FreqComp());
    for (LFreq lf: lfreqList){
        pq.offer(lf));
    }
    return pq;
}
```

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//remove all elements from this list void clear() // add the given element at the end of this list boolean add(T t) // add the given element at the given index, shifting all items after // to the right void add(int index, T t)

*** class ArrayList<T> ***

// Returns the element at the specified position in this list T get(int index) % f(x) = 0

// Returns true if this list contains no elements
boolean isEmpty()

// Removes the element at the specified position in this list
T remove(int index)

// Returns the number of elements in this collection
int size()

*** class String ***

// Returns the length of this string
int length()

// Tests if this string ends with the specified suffix boolean endsWith(String suffix)

// Returns a new string that is a substring of this string // The substring begins at the specified beginIndex // and extends to the character at index endIndex - 1 String substring(int beginIndex, int endIndex) *** class HashMap<K, V> ***

// Returns the value to which the specified key is mapped, // or null if this map contains no mapping for the key. V get(Object key)

// Associates the specified value with the specified key in this map. // Returns the previous value associated with key, // or null if there was no mapping for key or the key mapped to null V put(K key, V value)

//Returns true if this map contains a mapping for the specified key. boolean containsKey(Object key)

*** class PriorityQueue<T> ***

// the constructor that reserves the given capacity
// that orders the elements according to the specified comparator
PriorityQueue(int initalCapacity, Comparator<T> comparator)

// Inserts the specified element into this priority queue boolean add(T t)

// Inserts the specified element into this priority queue boolean offer(T t)

// Retrieves, but does not remove, the head of this queue, // or returns null if the queue is empty T peek()

// retrieves and removed the head of this queue
// or returns null if the queue is empty
T poll()

// retrieves and removed the head of this queue
// or returns null if the queue is empty
T remove()

// Returns the number of elements in this collection int size() $% \left({{\left({{{\left({{{\left({{{\left({{{c}}} \right)}} \right.}$