

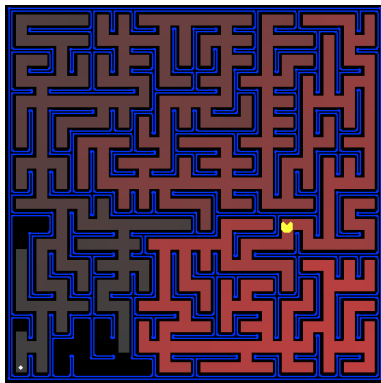
# CS 4100/5100: Foundations of AI Search

Instructor: Rob Platt  
rplatt@ccs.neu.edu

College of Computer and information Science  
Northeastern University

Fall, 2014

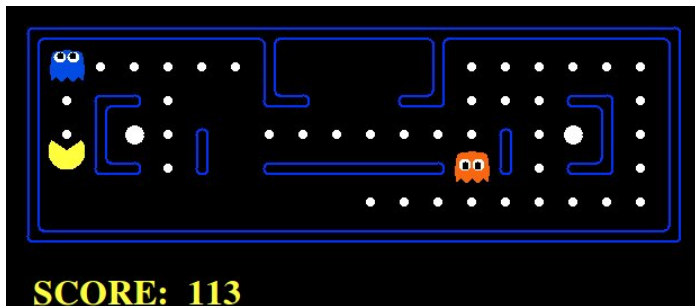
## Examples of search problems



Suppose the problem is to find a path to the x.

- ▶ state space ( $n = 56$ )?
- ▶ action space?
- ▶ transition function?
- ▶ goal test / path cost?

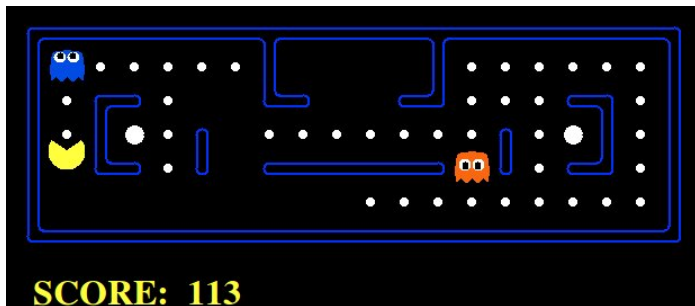
# Examples of search problems



Suppose the problem is to reach the x while avoiding ghosts.

- ▶ state space ( $56^3 = 175k$ )?
- ▶ action space?
- ▶ transition function?
- ▶ goal test / path cost?

# Examples of search problems



Suppose the problem is to eat all the dots and avoid the ghosts?

- ▶ state space  $56^3 + 2^56 > 7.2^{16}$ ?
- ▶ action space?
- ▶ transition function?
- ▶ goal test / path cost?

# Examples of search problems

7	2	4
5		6
8	3	1

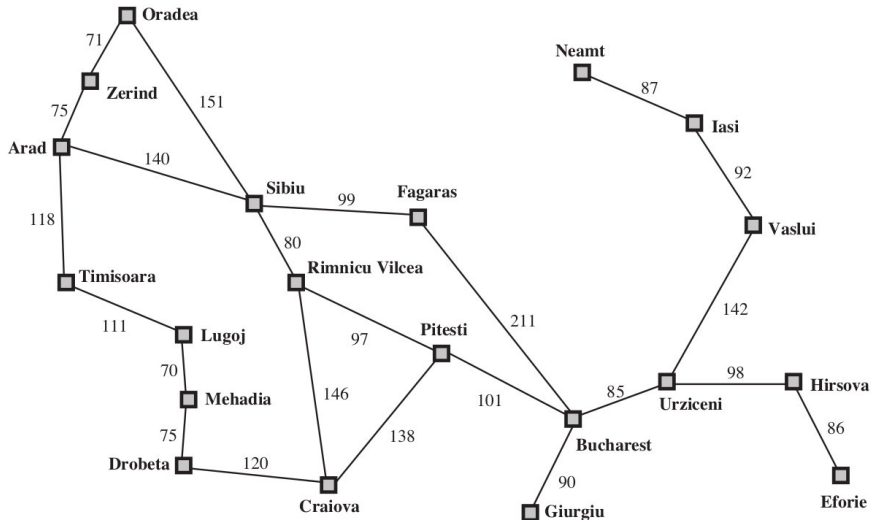
Start State

	1	2
3	4	5
6	7	8

Goal State

- ▶ state space (no greater than  $9! = 362k$  states)?
- ▶ action space?
- ▶ transition function?
- ▶ goal test / path cost?

# Examples of search problems



# Generalized search algorithm

```
function TREE-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of problem
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    expand the chosen node, adding the resulting nodes to the frontier
```

---

```
function GRAPH-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of problem
  initialize the explored set to be empty
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    add the node to the explored set
    expand the chosen node, adding the resulting nodes to the frontier
    only if not in the frontier or explored set
```

# Breadth First Search (BFS)

---

**function** BREADTH-FIRST-SEARCH(*problem*) **returns** a solution, or failure

*node*  $\leftarrow$  a node with STATE = *problem*.INITIAL-STATE, PATH-COST = 0

**if** *problem*.GOAL-TEST(*node*.STATE) **then return** SOLUTION(*node*)

*frontier*  $\leftarrow$  a FIFO queue with *node* as the only element

*explored*  $\leftarrow$  an empty set

**loop do**

**if** EMPTY?(*frontier*) **then return** failure

*node*  $\leftarrow$  POP(*frontier*) /\* chooses the shallowest node in *frontier* \*/

    add *node*.STATE to *explored*

**for each** *action* **in** *problem*.ACTIONS(*node*.STATE) **do**

*child*  $\leftarrow$  CHILD-NODE(*problem*, *node*, *action*)

**if** *child*.STATE is not in *explored* or *frontier* **then**

**if** *problem*.GOAL-TEST(*child*.STATE) **then return** SOLUTION(*child*)

*frontier*  $\leftarrow$  INSERT(*child*, *frontier*)

# Uniform Cost Search (UCS)

---

**function** UNIFORM-COST-SEARCH(*problem*) **returns** a solution, or failure

*node*  $\leftarrow$  a node with STATE = *problem*.INITIAL-STATE, PATH-COST = 0

*frontier*  $\leftarrow$  a priority queue ordered by PATH-COST, with *node* as the only element

*explored*  $\leftarrow$  an empty set

**loop do**

**if** EMPTY?(*frontier*) **then return** failure

*node*  $\leftarrow$  POP(*frontier*) /\* chooses the lowest-cost node in *frontier* \*/

**if** *problem*.GOAL-TEST(*node*.STATE) **then return** SOLUTION(*node*)

    add *node*.STATE to *explored*

**for each** *action* **in** *problem*.ACTIONS(*node*.STATE) **do**

*child*  $\leftarrow$  CHILD-NODE(*problem*, *node*, *action*)

**if** *child*.STATE is not in *explored* or *frontier* **then**

*frontier*  $\leftarrow$  INSERT(*child*, *frontier*)

**else if** *child*.STATE is in *frontier* with higher PATH-COST **then**

            replace that *frontier* node with *child*

# Depth Limited Depth First Search (DLDFS)

---

**function** DEPTH-LIMITED-SEARCH(*problem*, *limit*) **returns** a solution, or failure/cutoff  
    **return** RECURSIVE-DLS(MAKE-NODE(*problem*.INITIAL-STATE), *problem*, *limit*)

**function** RECURSIVE-DLS(*node*, *problem*, *limit*) **returns** a solution, or failure/cutoff  
    **if** *problem*.GOAL-TEST(*node*.STATE) **then return** SOLUTION(*node*)  
    **else if** *limit* = 0 **then return** *cutoff*  
    **else**  
        *cutoff\_occurred?*  $\leftarrow$  false  
        **for each** *action* **in** *problem*.ACTIONS(*node*.STATE) **do**  
            *child*  $\leftarrow$  CHILD-NODE(*problem*, *node*, *action*)  
            *result*  $\leftarrow$  RECURSIVE-DLS(*child*, *problem*, *limit* - 1)  
            **if** *result* = *cutoff* **then** *cutoff\_occurred?*  $\leftarrow$  true  
            **else if** *result*  $\neq$  failure **then return** *result*  
        **if** *cutoff\_occurred?* **then return** *cutoff* **else return** failure

# Bidirectional search

