

Brains

- $\sim 10^{11}$ neurons of > 20 types, $\sim 10^{14}$ synapses, 1-10ms cycle time
- Signals are noisy spike trains of electrical potential
- Synaptic strength believed to increase or decrease with use (⇔learning?)

A Neuron Axonal arborization Axon from another cell Synapse Axon Nucleus Cell body or Soma





















What about learning?

- Start with training data {(\mathbf{x}^r , d^r)}, where each input/desired output pair is indexed by r = 1, ..., R and $\mathbf{x}^r = (1, x_1^r, x_2^r, ..., x_n^r)$ represents the input (this time augmented by the bias input $x_0^r = I$)
- Each d^r is of course either 0 or 1
- The objective is to find a weight vector $\mathbf{w} = (w_0, w_1, w_2, \dots, w_n)$ such that $y' = g(\mathbf{w} \cdot \mathbf{x}^r)$ agrees with d^r for each r, where g is the hard-limiting threshold function

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Multilayer Networks

- This algorithm has been known since ~1960 (Rosenblatt)
- But the most interesting functions we might want to learn are not necessarily linearly separable
- Dilemma faced by ANN researchers between ~1960 and ~1985:
 - for greater expressiveness, need multilayer networks of these linear threshold units
 - only known reasonable algorithm was for singlelayer networks (i.e., one layer of weights)





• simplest way: define this error measure for each training example and then define the overall error measure as the sum of these

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Learning in multilayer nets Define the error on the rth training example to be $E^{r} = \frac{1}{2} \sum_{i \in OutputUnits} (d^{r}_{i} - y^{r}_{i})^{2}$ where d^{r}_{i} and y^{r}_{i} are the desired and actual outputs, respectively, of the ith unit for training example r. This is a function of the network weights since y^{r}_{i} is. Then define the overall error to be $E = \sum_{r} E^{r}$ Attical Neural Network: Side 21





- So gradient descent useless in this case
- Now introduce a trick ...

























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Remarks

- Batch version represents true gradient descent
- Incremental version only an approximation, but often converges faster in practice
- Many variations:
 - Momentum essentially smooths successive weight changes
 - Different values of η for different units, or as function of time, or adapted based on still other considerations
 - Use of second-order techniques or approximations to
- themDrawbacks
 - May take many iterations to converge
 - May converge to suboptimal local minima
 - Learned network may be hard to interpret in humanunderstandable terms

Remarks (cont.)

- Gradient-based "credit assignment"
 - make changes to all parameters where such changes
 would contribute some beneficial effect
 - size of change proportional to sensitivity make larger changes to parameters to which beneficial outcome most sensitive

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Practical considerations

- Useful squashing functions only approach their extreme values asymptotically
- E.g., logistic function can never actually attain values of 0 or 1
- With such output units, training to unattainable output values would never terminate
- · Instead, in practice use either
 - a dead zone: e.g., train to targets of 0 and 1 but consider any output within a tolerance of, say, 0.1 to be correct
 - targets of, say, 0.1 and 0.9 in place of 0 and 1, respectively

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Neural net representations

- Have to encode all possible input and output as Euclidean vectors
- What if input or output is discrete (e.g., symbolic)?
- If exactly two possible values, one natural encoding would be to use 0 for one of these and 1 for the other
- Alternative encoding that works for any finite number of values: use a separate node for each value and set exactly one node to 1 and all others to 0

 called 1-out-of-n or radio button encoding
- But if the values have a natural topology (e.g., fall on an ordinal scale), might make sense to use an encoding that captures this

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Representation example

- Consider Outlook = Sunny, Overcast, or Rain
- 1-out-of-3 encoding:
 - Sunny ⇔ 1 0 0
 - Overcast ⇔ 0 1 0 Uses 3 input nodes
 - Rain ⇔ 0 0 1
- Treating Overcast as halfway between Sunny and Rain:
 - Sunny ⇔ 0.0
- Uses 1 input node
- Overcast ⇔ 0.5
 Rain ⇔ 1.0
- Such choices help determine the underlying inductive bias

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Other considerations

- Avoiding overfitting
 - early stopping
 - explicit penalty terms
 - weight decay
- Incorporating prior knowledge
 - enforcing invariances through "weight sharing"
 - limiting connectivity
 - letting some of the input represent more complex precomputed features
 - initializing the network according to a best guess, then letting backprop fine-tune the weights
 - setting some weights by hand and keeping them fixed



Expressiveness

 Any continuous function can be approximated arbitrary closely over a bounded region by a two-layer network with sigmoid squashing functions in the hidden layer and linear units in the output layer (given enough hidden units)

Inductive bias

• When weights are close to zero, behavior is approximately linear

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• Keeping weights near zero gives a preference bias toward linear functions

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Wide variety of applications

- Speech recognition
- Autonomous driving
- Handwritten digit recognition
- Credit approval
 - But may be hard to translate network behavior into more explicit, easily-understood rules
- Backgammon
- Etc.

Generally appropriate for problems where the final answer depends heavily on combinations of many input features

Decision trees might be better when decisions depend on only a small subset of the input features







Summary

- Most brains have lots of neurons, so maybe the kinds of computing that brains are good at are best accomplished by large networks of simple computing units (linear threshold units?)
- One-layer networks insufficiently expressive
- Multilayer networks are sufficiently expressive and can be trained by gradient descent, i.e., error backpropagation
- Some general-purpose ways to look at learning
 Formulation as an optimization problem
 Gradient search when appropriate
- Various techniques for incorporating prior knowledge and for avoiding overfitting
 Many applications
- Even some temporal behaviors can be trained by backpropagation-like gradient descent algorithms