

Inducing Decision Trees from Data

- Suppose we have a set of training data and want to construct a decision tree consistent with that data
- One trivial way: Construct a tree that essentially just reproduces the training data, with one path to a leaf for each example
 no hope of generalizing
 - no nope or generalizing

Day Outlook

D3 Overcast

D7 Overcast

D11 Sunny

D12 Overcast

D13 Overcast

Sunny

Sunny

Rain

Rain

Rain

Sunnv

Sunny

 Rain

 Rain

Mild

Mild

Mild

Hot

Mild

Normal

 High

Normal

 High

Normal Strong

Weak

Strong

Weak

 Strong

D1

D2

D4

D5

D6

D8

D9

D10

D14

- Better way: ID3 algorithm
 - tries to construct more compact trees
 - uses information-theoretic ideas to create tree recursively

Decision Trees: Slide 3

Inducing a decision tree: example

- Suppose our tree is to determine whether it's a good day to play tennis based on attributes representing weather conditions
- Input attributes

Attribute	Possible Values
Outlook	Sunny, Overcast, Rain
Temperature	Hot, Mild, Cool
Humidity	High, Normal
Wind	Strong, Weak

• Target attribute is PlayTennis, with values Yes or No

Training Data Temperature Humidity Wind PlayTennis Hot High Weak No Hot High Strong No Hot High Weak Yes Weak Mild High Yes Cool Normal Weak Yes Strong Cool Normal No Strong Cool Normal Yes Mild High Weak No Cool Normal Weak Yes

Yes

Yes

Yes

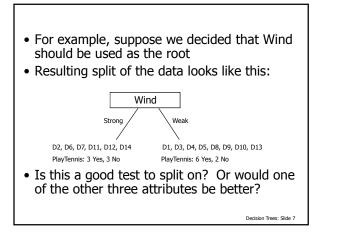
Yes

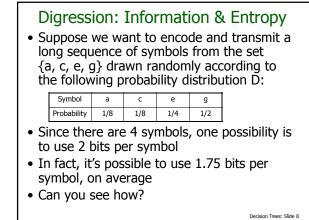
No Decision Trees: Slide 5

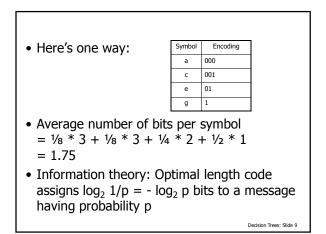
Essential Idea Main question: Which attribute test should be placed at the root? In this example, 4 possibilities Once we have an answer to this question, apply the same idea recursively to the resulting subtrees Base case: all data in a subtree give rise to the same value for the target attribute In this case, make that subtree a leaf with the appropriate label

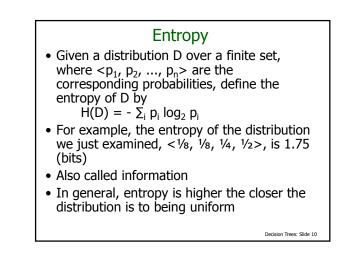
Decision Trees: Slide 6

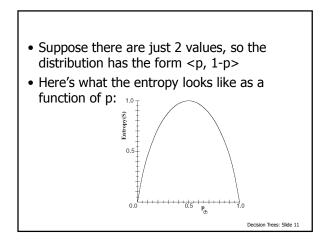
Decision Trees: Slide 4

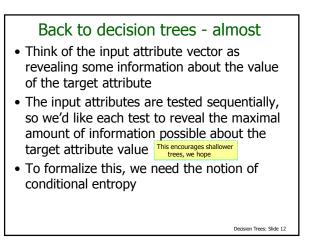










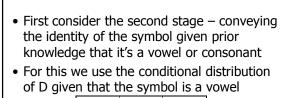


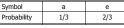
٠	Return	to	our	symbol	encoding	example:
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Symbol	а	с	е	g
Probability	1/8	1/8	1/4	1/2

- Suppose we're given the identity of the next symbol received in 2 stages:
 - we're first told that the symbol is a vowel or consonant
 - then we learn its actual identity
- We'll analyze this 2 different ways

Decision Trees: Slide 13

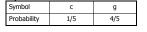




and the conditional distribution of D given that the symbol is a consonant

Decision Trees: Slide 14

Decision Trees: Slide 16



• We can compute the entropy of each of these conditional distributions: $H(D|Vowel) = -1/3 \log_2 1/3 - 2/3 \log_2 2/3$ = 0.918H(D|Consonant) $= -1/5 \log_2 1/5 - 4/5 \log_2 4/5$ = 0.722• We then compute the expected value of this as 3/8 * 0.918 + 5/8 * 0.722 = 0.796

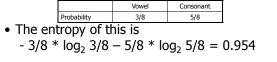
- H(D|Vowel) = 0.918 represents the expected number of bits to convey the actual identity of the symbol given that it's a vowel
- H(D|Consonant) = 0.722 represents the expected number of bits to convey the actual identity of the symbol given that it's a consonant
- Then the weighted average 0.796 is the expected number of bits to convey the actual identity of the symbol given whichever is true about it – that it's a vowel or that it's a consonant

Information Gain

- Thus while it requires an average of 1.75 bits to convey the identity of each symbol, once it's known whether it's a vowel or a consonant, it only requires 0.796 bits, on average, to convey its actual identity
- The difference 1.75 0.796 = 0.954 is the number of bits of information that are gained, on average, by knowing whether the symbol is a vowel or a consonant
 - called *information gain*

Decision Trees: Slide 17

- The way we computed this corresponds to the way we'll apply this to identify good split nodes in decision trees
- But it's instructive to see another way: Consider the first stage – specifying whether vowel or consonant
- The probabilities look like this:



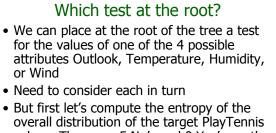
Decision Trees: Slide 18

Now back to decision trees for real

- We'll illustrate using our PlayTennis data
- The key idea will be to select as the test for the root of each subtree the one that gives maximum information gain for predicting the target attribute value
- Since we don't know the actual probabilities involved, we instead use the obvious frequency estimates from the training data
- Here's our training data again:

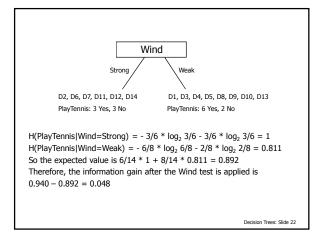
Decision Trees: Slide 19

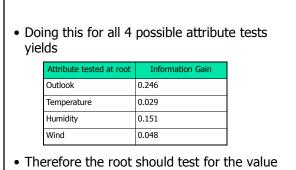
	Training Data						
Da	y Outlook	Temperature	Humidity	Wind	PlayTennis		
D	1 Sunny	Hot	High	Weak	No		
D	2 Sunny	Hot	High	Strong	No		
D	3 Overcast	Hot	High	Weak	Yes		
D-4	4 Rain	Mild	High	Weak	Yes		
D	5 Rain	Cool	Normal	Weak	Yes		
D	6 Rain	Cool	Normal	Strong	No		
D'	7 Overcast	Cool	Normal	Strong	Yes		
D	8 Sunny	Mild	High	Weak	No		
D	9 Sunny	Cool	Normal	Weak	Yes		
D1	0 Rain	Mild	Normal	Weak	Yes		
D1	1 Sunny	Mild	Normal	Strong	Yes		
D1	2 Overcast	Mild	High	Strong	Yes		
D1	3 Overcast	Hot	Normal	Weak	Yes		
D1	4 Rain	Mild	High	Strong	No		
	Decision Trees: Slide 20						



- values: There are 5 No's and 9 Yes's, so the entropy is - 5/14 * log₂ 5/14 – 9/14 * log₂ 9/14
 - = 0.940

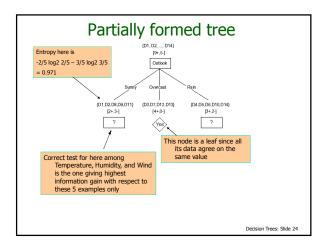
Decision Trees: Slide 21





of Outlook

Decision Trees: Slide 23



Extensions

- Continuous input attributes
 - Sort data on any such attribute and try to identify a high information gain threshold, forming binary split
- Continuous target attribute
 - Called a regression tree won't deal with it here
- Avoiding overfitting
 More on this later
 - Use separate validation set
 - Use tree post-pruning based on statistical tests

Decision Trees: Slide 25

Extensions (continued)

- Inconsistent training data (same attribute vector classified more than one way)
 - Store more information in each leaf
- Missing values of some attributes in training data
 - Won't deal with this here
- Missing values of some attributes in a new attribute vector to be classified (or missing branches in the induced tree)
 - Send the new vector down multiple branches corresponding to all values of that attribute, then let all leaves reached contribute to result