



$$
\begin{aligned}
& \hline \hline \text { Example } \\
& \hline \text { I'm at work, neighbor John calls to say my alarm is ringing, but neighbor } \\
& \text { Mary doesn't call. Sometimes it's set off by minor earthquakes. Is there a } \\
& \text { burglar? } \\
& \text { Variables: Burglar, Earthquake, Alarm, JohnCalls, MaryCalls } \\
& \text { Network topology reflects "causal" knowledge: } \\
& \text { - A burglar can set the alarm off } \\
& \text { - An earthquake can set the alarm off } \\
& \text { - The alarm can cause Mary to call } \\
& \text { - The alarm can cause John to call }
\end{aligned}
$$


Global semantics
"Global" semantics defines the full joint distribution
as the product of the local conditional distributions:
$\quad P\left(x_{1}, \ldots, x_{n}\right)=\prod_{i=1}^{n} P\left(x_{i} \mid p a r e n t s\left(X_{i}\right)\right)$
e.g., $P(j \wedge m \wedge a \wedge \neg \wedge \wedge \neg e)$
$\quad=P(j \mid a) P(m \mid a) P(a \mid \neg b, \neg e) P(\neg b) P(\neg e)$
$=0.9 \times 0.7 \times 0.001 \times 0.999 \times 0.998$
$\approx 0.00063$


\section*{Each node is conditionally independent of all others gild

Markov blanket: parents + children + children's parents


Local semantics: each node is conditionally independent
of its nondescendants given its parents






| Compact conditional distributions |
| :--- |
| CPT grows exponentially with number of parents |
| CPT becomes infinite with continuous-valued parent or child |
| Solution: canonical distributions that are defined compactly |
| Deterministic nodes are the simplest case: |
| $\quad X=f($ Parents $(X))$ for some function $f$ |
| E.g., Boolean functions |
| $\quad$ NorthAmerican $\Leftrightarrow$ Canadian $\vee U S \vee$ Mexican |
| E.g., numerical relationships among continuous variables |
| $\frac{\partial L e v e l ~}{\partial t}=$ inflow + precipitation - outflow - evaporation |


Testable variables (green), "broken, so fix it" variables (orange)
Hidden variables (gray) ensure sparse structure, reduce parameters Example: Car diagnosis

## Option 1: discretization-possibly large errors, Option 2: finitely parameterized canonical fam 1) Continuous variable, discrete+continuous p 2) Discrete variable, continuous parents (e.g.,

## เsonder ifpisqns <br>  Hybrid (discrete+continuous) networks






