## Homework 07

Due: Friday, November 17, 2006

## Instructions

- 1. Please review the homework grading policy outlined in the course information page.
- 2. On the *first page* of your solution write-up, you *must* make explicit which problems are to be graded for regular credit, which problems are to be graded for extra credit, and which problems you did not attempt. Use a table that looks like this:

Problem	1	2	3	4	5	6	7	8	9	
Credit	RC	RC	RC	EC	RC	EC	NA	NA	EC	

where "RC" denotes "regular credit", "EC" denotes "extra credit", and "NA" denotes "not attempted". Failure to include such a table will result in an arbitrary set of problems being graded for regular credit, no problems being graded for extra credit, and a 5% penalty assessment.

3. You must also write down with whom you worked on the assignment. If this varies from problem to problem, write down this information separately with each problem.

## Problems

**Required:** 4 of the following 6 problems **Points:** 25 points per problem

- 1. Do Exercise 4.2.
  - Do Problem 4.12.
- 2. Do Exercise 4.3.
- 3. Do Exercise 4.4.
- 4. Do Problem 4.19. *Hint:* Consider how closure of the class of regular languages under string reversal is proved.
- 5. Prove that  $ONE_{DFA} = \{ \langle D \rangle \mid D \text{ is a DFA and } |L(D)| = 1 \}$  is decidable.
- 6. Prove that  $INFINITE_{CFG} = \{\langle G \rangle \mid G \text{ is a CFG and } L(G) \text{ is infinite}\}$  is decidable. *Hint:* One way to do this is to consider the appropriate Pumping Lemma and the first few steps of its proof. Whatever approach you use, provide a mathematical argument justifying it.