Fundamentals of Cryptography: Algorithms, and Security Services

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Network Security: Private Communication in a Public World [Chap. 2-8] Charles Kaufman, Mike Speciner, Radia Perlman, Prentice-Hall

Cryptography: Theory and Practice, Douglas Stinson, Chapman & Hall/CRC

Cryptography and Network Security, William Stallings, Prentice Hall

Why, How, What?

- Cryptography provides key building block for many network security services
- Security services:
 - Authentication, Confidentiality, Integrity, Access control, Nonrepudiation, availability, key management, audit
- Cryptographic algorithms (building blocks):
 - Encryption: symmetric encryption (e.g., AES), asymmetric encryption (e.g., RSA, El-Gamal)
 - Hashing functions
 - Message Authentication Code (e.g., HMAC + SHA1)
 - Digital signature functions (e.g., RSA, El-Gamal)

What you need to know at the end of this lecture

- What are the important cryptographic mechanisms?
- What are the two fundamental classes of cryptographic mechanisms: symmetric, and asymmetric?
- What are the important algorithms for symmetric crypto?
- How are these algorithms used?
- Some of the main asymmetric crypto algorithms: RSA, DH, how do they work? how can they be used?

Outline

- Introduction to Cryptography
- Secret Key Cryptography (symmetric crypto)
- Modes of Operation of Encryption Algorithms
 - ECB, CBC, OFB, CFB, CTR
- Hashes and Message Authentication Codes
- Public Key Algorithms (asymmetric crypto)

Terminology

- Security services:
 - Authentication, confidentiality, integrity, access control, nonrepudiation, availability, key management, audit
- Security attacks:
 - Passive, active
- Cryptography models:
 - Symmetric (secret key), asymmetric (public key)
- Cryptanalysis:
 - Ciphertext only, known plaintext, chosen plaintext, chosen ciphertext, chosen text

Security services

- Authentication:
 - assures the recipient of a message the authenticity of the claimed source
- Access control:
 - limits the access to authorized users
- Confidentiality:
 - protects against unauthorized release of message content
- Integrity:
 - guarantees that a message is received as sent
- Non-repudiation:
 - protects against sender/receiver denying sending/receiving a message
- Availability:
 - guarantees that the system services are always available when needed
- Security audit:
 - keeps track of transactions for later use (diagnostic, alarms...)
- Key management:
 - allows to negotiate, setup and maintain keys between communicating entities

Security Attacks

- Security attacks:
 - Interception (confidentiality)
 - Interruption (availability)
 - Modification (integrity)
 - Fabrication (authenticity)
- Kent's classification
 - Passive attacks:
 - Release of message content
 - Traffic analysis
 - Active attacks:
 - Masquerade
 - Replay
 - Modification of message
 - Denial of service

Kerchoff's Principle

- The cipher should be secure even if the intruder knows all the details of the encryption process except for the secret key
- "No security by obscurity"
 - Examples of system that did not follow this rule and failed?

Securing Networks

- Where to put the security in a protocol stack?
- Practical considerations:
 - End to end security
 - No modification to OS

Applications Layer Control/Management (configuration) telnet/ftp: ssh, http: shttp, mail: PGP (SSL/TLS) Transport Layer (TCP) (IPSec, IKE) Network Layer (IP) Link Layer (IEEE802.1x/IEEE802.10)Physical Layer (spread-Spectrum, quantum crypto, etc.)

Network Security

Cryptography Overview

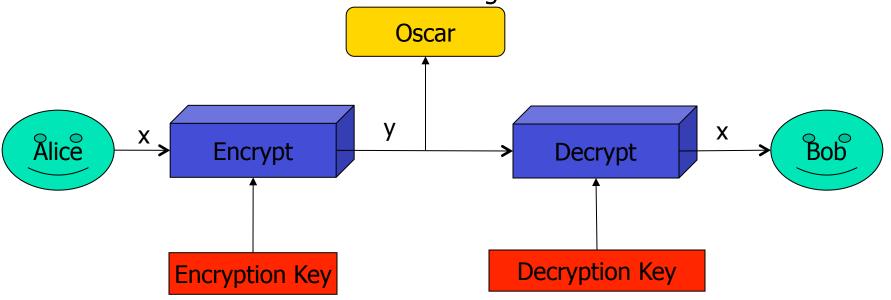
Monitoring/Logging/Intrusion Detection

Network Security Tools:

Encryption

Basic Goal:

 Allow two entities (e.g., Alice, and Bob) to communicate over an insecure channel, such that an opponent (e.g., Oscar) cannot understand what is being communicated

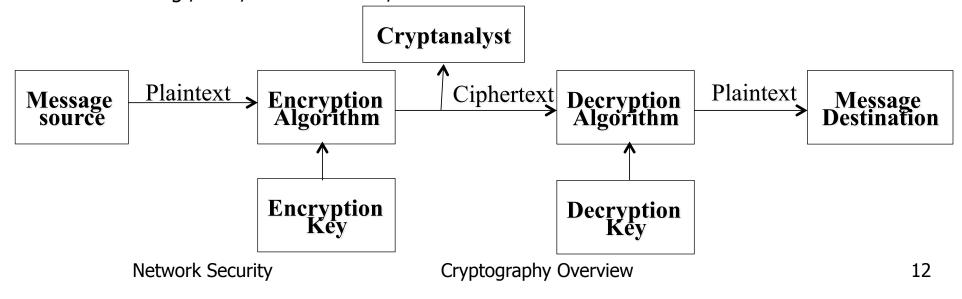


Encryption Algorithms

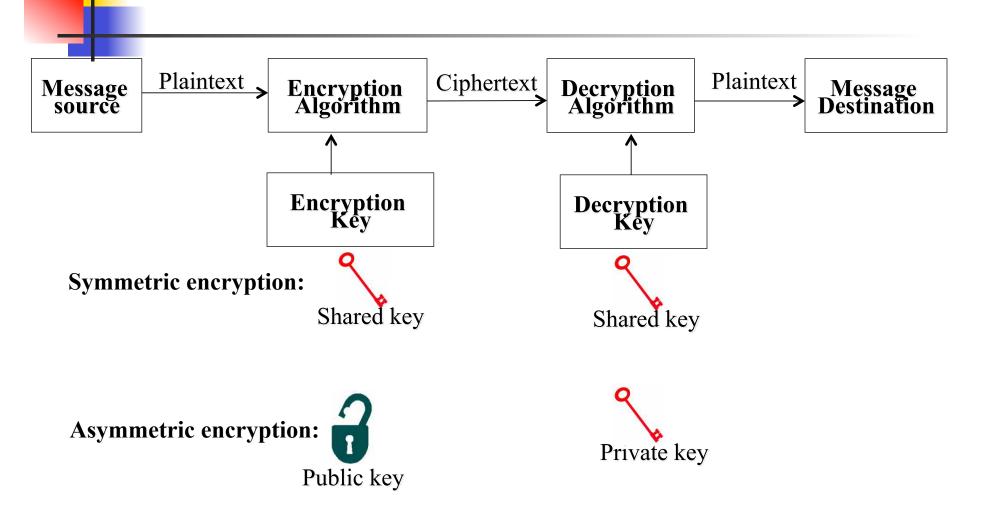
- Block vs. Stream ciphers
 - Block ciphers:
 - Input: block of n bits; Output: block of n bits
 - Examples: AES, DES
 - Stream ciphers:
 - Input: stream of symbols ; Output: stream of symbols
 - Examples: GSM A5, RC4
 - Block ciphers can be used to build stream ciphers (under some assumptions)
 - Examples: AES-CBC

Encryption Models

- Symmetric encryption (conventional encryption)
 - Encryption Key = Decryption Key
 - I.e., Decryption key can be derived from encryption key
 - E.g., AES, DES, FEAL, IDEA, BLOWFISH
- Asymmetric encryption
 - Encryption Key ≠ Decryption key
 - I.e., Decryption key cannot be derived from encryption key
 - E.g., RSA, Diffie-Hellman, ElGamal



Encryption Models



Symmetric vs. Asymmetric Algorithms

- Symmetric algorithms are much faster
 - In the order of a 1000 times faster
- Symmetric algorithms require a shared secret
 - Impractical if the communicating entities don't have another secure channel
- Both algorithms are combined to provide practical and efficient secure communication
 - E.g., establish a secret session key using asymmetric crypto and use symmetric crypto for encrypting the traffic

Attacks on Encrypted Messages

- Ciphertext only:
 - encryption algorithm, ciphertext to be decoded
- Known plaintext:
 - encryption algorithm, ciphertext to be decoded, pairs of (plaintext, ciphertext)
- Chosen plaintext:
 - encryption algorithm, ciphertext to be decoded, plaintext (chosen by cryptanalyst) + corresponding ciphertext
- Chosen ciphertext:
 - encryption algorithm, ciphertext to be decoded, ciphertext (chosen by cryptanalyst) + corresponding plaintext
- Chosen text:
 - encryption algorithm, ciphertext to be decoded, plaintext + corresponding ciphertext (both can be chosen by attacker)



Secret Key Cryptography

Symmetric Cryptography

Conventional Cryptography

Examples of Encryption Algorithms

Advances Encryption Algorithm (AES)

Block size: 128 bits

Key size:128/196/256

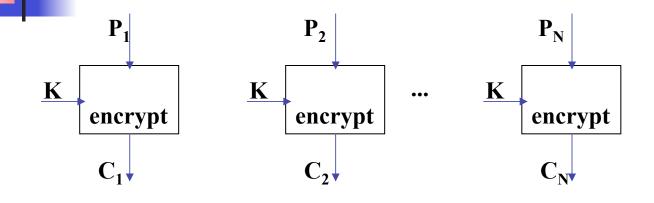
Data Encryption Standard (DES) – not secure

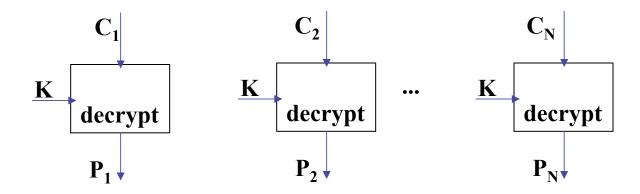
Block size: 64 bits

Key size: 56 bits

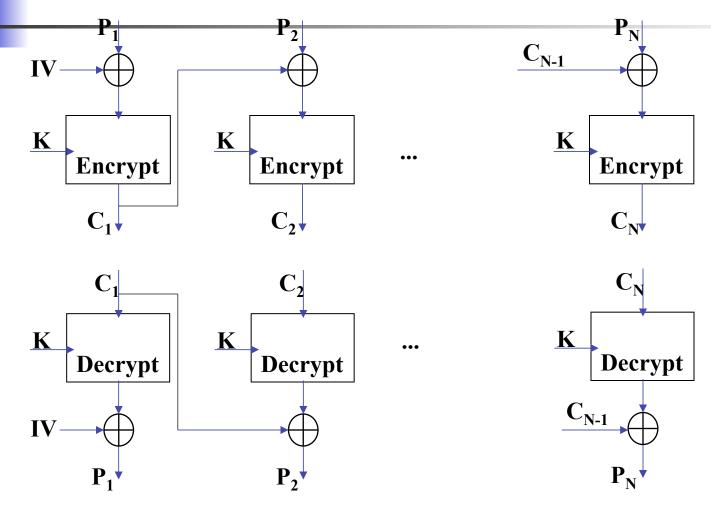
It is not recommended to use DES

Encryption Modes: Electronic Codebook (ECB)

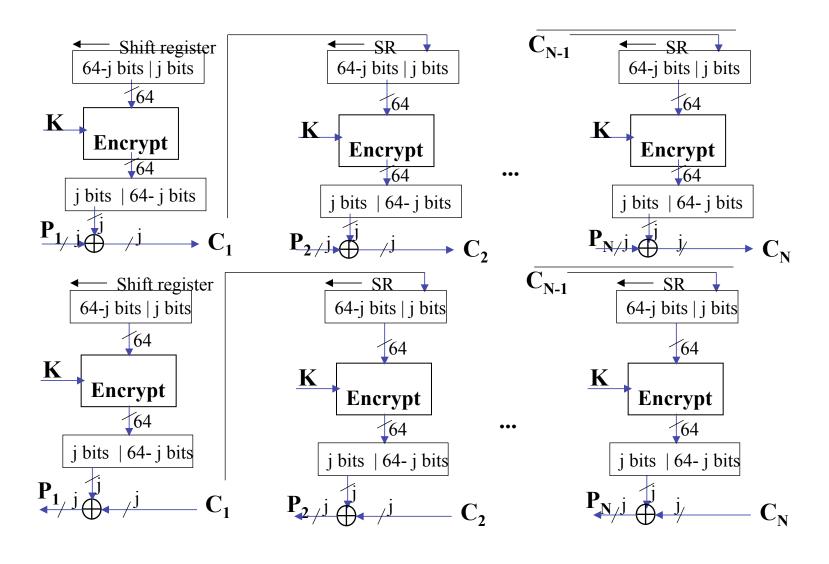




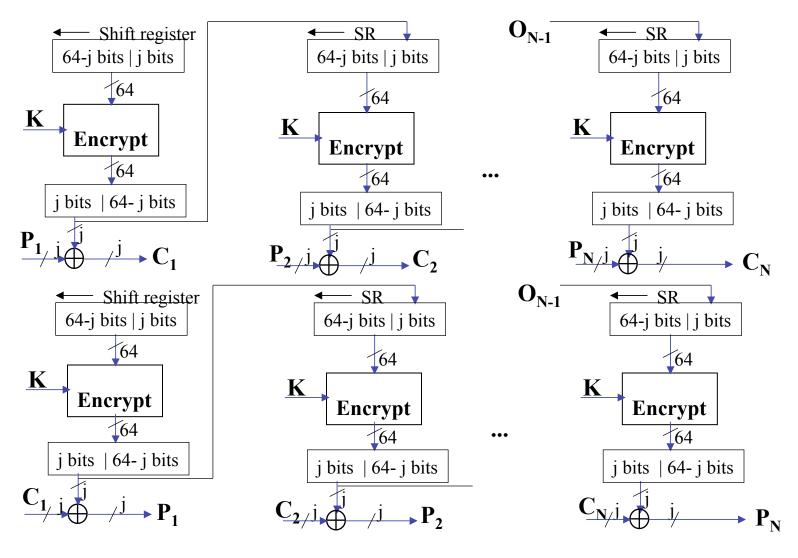
Encryption Modes: Cipher Block Chaining (CBC)



Encryption Modes: Cipher Feedback (CFB)



Encryption Modes: Output Feedback (OFB)



Counter (CTR)

- Similar to OFB but encrypts counter value rather than any feedback value
- Must have a different key & counter value for every plaintext block (never reused)

```
C_i = P_i XOR O_i

O_i = Encrypt_{K1}(i)
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Uses: high-speed network encryptions, random access to files

Symmetric Encryption Algorithms Internals

Historical ciphers

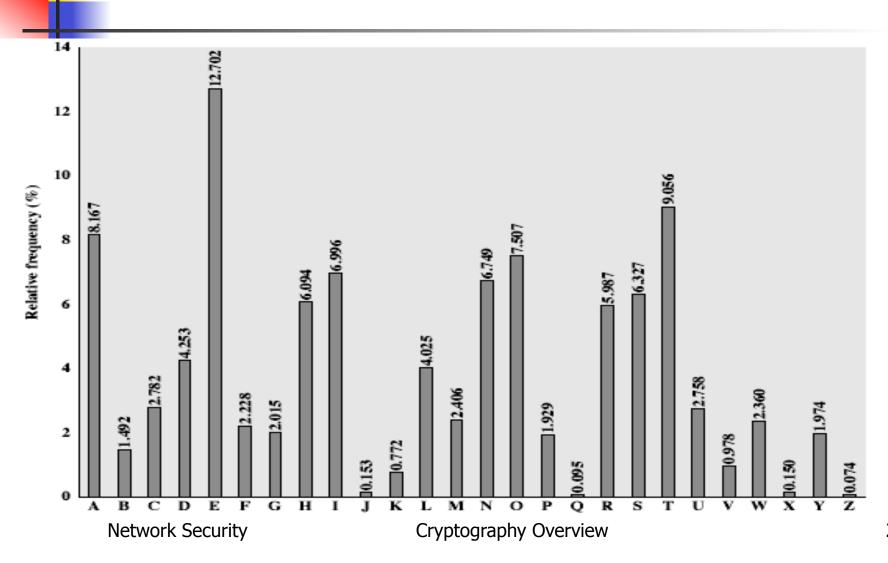
Not necessary to understand all the details

Symmetric cryptosystems (conventional cryptosystems)

Substitution techniques:

- Caesar cipher
 - Replace each letter with the letter standing x places further
 - Example: (x = 3)
 - plain: meet me after the toga party
 - cipher: phhw ph diwhu wkh wrjd sduwb
 - Key space: 25
 - Brut force attack: try 25 possibilities
- Monoalphabetic ciphers
 - Arbitrary substitution of alphabet letters
 - Key space: 26! > 4x10²⁶ > key-space(DES)
 - Attack if the nature of the plaintext is known (e.g., English text):
 - compute the relative frequency of letters and compare it to standard distribution for English (e.g., E:12.7, T:9, etc.)
 - compute the relative frequency of 2-letter combinations (e.g., TH)

English Letters Frequencies



Symmetric cryptosystems (Continued)

- Multiple-Letter Encryption (Playfair cipher)
 - Plaintext is encrypted two-letters at a time
 - Based on a 5x5 matrix
 - Identification of individual diagraphs is more difficult (26x26 possibilities)
 - A few hundred letters of ciphertext allow to recover the structure of plaintext (and break the system)
 - Used during World War I & II
- Polyalphabetic Ciphers (Vigenère cipher)
 - 26 Caesar ciphers, each one denoted by a key letter
 - key: deceptivedeceptive
 - plain: wearediscoveredsaveyourself
 - cipher: zicvtwongrzgvtwavzhcoyglmgj
 - Enhancement: auto-key (key = initial||plaintext)
- Rotor machines: multi-round monoalphabetic substitution
 - Used during WWII by Germany (ENIGMA) and Japan (Purple)

Transposition/Permutation Techniques

- Based on permuting the plaintext letters
- Example: rail fence technique

mematrhtgpry

etefeteoaat

A more complex transposition scheme

Key: 4312567

Plain: attackp

ostpone

duntilt

woamxyz

Cipher: TTNAAPTMTSUOAODWCOIXKNLYPETZ

- Attack: letter/diagraph frequency
- Improvement: multiple-stage transposition

One-Time Pad

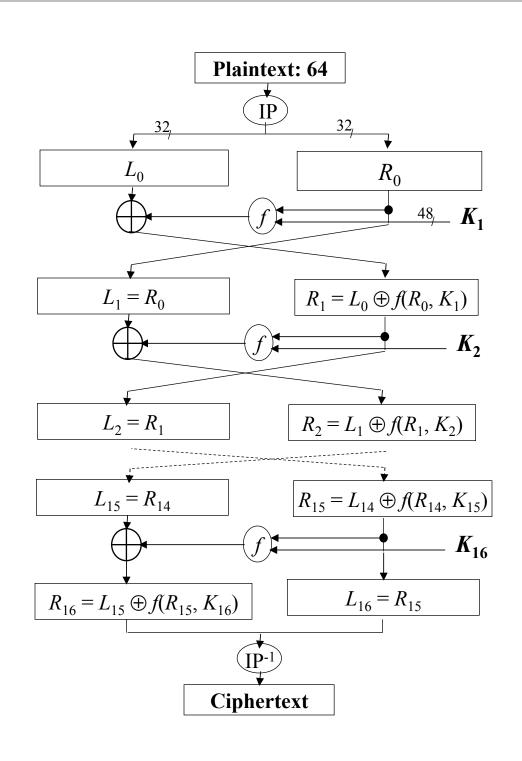
- Introduced by G. Vernam (AT&T, 1918), improved by J. Mauborgne
- Scheme:
 - Encryption: $c_i = p_i \oplus k_i$
 - c_i : f^{th} binary digit of plaintext, p_i : plaintext, k_i : key
 - Decryption: $p_i = c_i \oplus k_i$
 - Key is a random sequence of bits as long as the plaintext
- One-Time Pad is unbreakable
 - No statistical relationship between ciphertext and plaintext
 - Example (Vigenère One-Time Pad):
 - Cipher: ANKYODKYUREPFJBYOJDSPLREYIUN
 - Plain-1 (with k1): MR MUSTARD WITH THE CANDLE
 - Plain-2 (with k2): MISS SCARLET WITH THE KNIFE
- Share the same long key between the sender & receiver

Today's Block Encryption Algorithms

- Key size:
 - Too short => easy to guess
- Block size:
 - Too short easy to build a table by the attacker: (plaintext, ciphertext)
 - Minimal size: 64 bits
- Properties:
 - One-to-one mapping
 - Mapping should look random to someone who doesn't have the key
 - Efficient to compute/reverse
- How:
 - Substitution (small chunks) & permutation (long chunks)
 - Multiple rounds
 - ⇒ SPN (Substitution and Permutation Networks) and variants

Data Encryption Standard (DES)

- Developed by IBM for the US government
- Based on Lucifer (64-bits, 128-bits key in 1971)
- To respond to the National Bureau of Standards
 CFP
 - Modified characteristics (with help of the NSA):
 - 64-bits block size, 56 bits key length
 - Concerns about trapdoors, key size, sbox structure
- Adopted in 1977 as the DES (FIPS PUB 46, ANSI X3.92) and reaffirmed in 1994 for 5 more years
- Replaced by AES (not secure today)

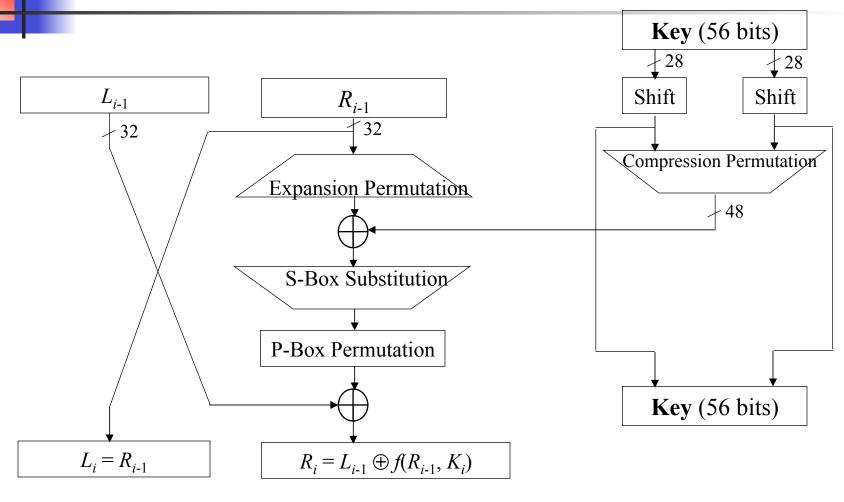


DES is based on Feistel Structure

$$L_i = R_{i-1}$$

 $R_i = L_{i-1} \oplus f(R_{i-1}, K_i)$

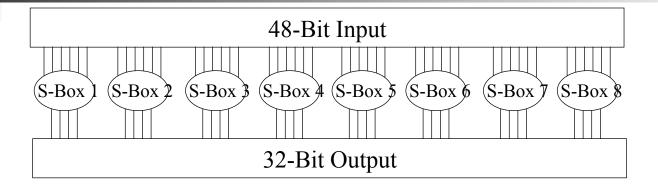
One DES Round



Network Security

Cryptography Overview

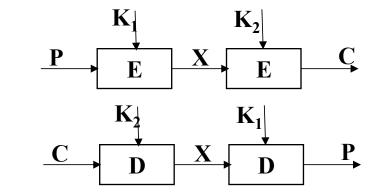
S-Box Substitution



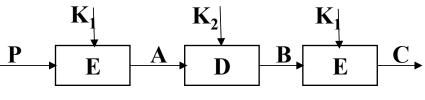
- S-Box heart of DES security
- S-Box: 4x16 entry table
 - Input 6 bits:
 - 2 bits: determine the table (1/4)
 - 4 bits: determine the table entry
 - Output: 4 bits
- S-Boxes are optimized against Differential cryptanalysis

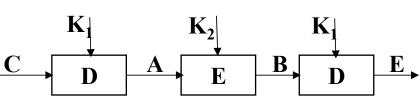
Double/Triple DES

- Double DES
 - Vulnerable to Meet-inthe-Middle Attack [DH77]



- Triple DES
 - Used two keys K₁ and K₂
 - Compatible with simple DES (K1=K2)
 - Used in ISO 8732, PEM, ANS X9.17





Linear/Differential Cryptanalysis

- Differential cryptanalysis
 - "Rediscovered" by E. Biham & A. Shamir in 1990
 - Based on a chosen-plaintext attack:
 - Analyze the difference between the ciphertexts of two plaintexts which have a known fixed difference
 - The analysis provides information on the key
 - 8-round DES broken with 2¹⁴ chosen plaintext
 - 16-round DES requires 2⁴⁷ chosen plaintext
- DES design took into account this kind of attacks
- Linear cryptanalysis
 - Uses linear approximations of the DES cipher (M. Matsui 1993)
- IDEA first proposal (PES) was modified to resist to this kind of attacks
- GSM A3 algorithm is sensitive to this kind of attacks
 - SIM card secret key can be recoverd => GSM cloning

Breaking DES

- Electronic Frontier Foundation built a "DES Cracking Machine" [1998]
 - Attack: brute force
 - Inputs: two ciphertext
 - Architecture:
 - PC
 - array of custom chips that can compute DES
 24 search units/chip x 64chips/board x 27 boards
 - Power:
 - searches 92 billion keys per second
 - takes 4.5 days for half the key space
 - Cost:
 - \$130'000 (all the material: chips, boards, cooling, PC etc.)
 - \$80'000 (development from scratch)

The Advanced Encryption Standard (AES) Cipher - Rijndael

- Designed by Rijmen-Daemen (Belgium)
- Key size: 128/192/256 bit
- Block size: 128 bit data
- Properties: iterative rather than Feistel cipher
 - Treats data in 4 groups of 4 bytes
 - Operates on an entire block in every round
- Designed to be:
 - Resistant against known attacks
 - Speed and code compactness on many CPUs
 - Design simplicity

AES

State: 16 bytes structured in a array

S _{0,0}	S _{0,1}	S _{0,2}	S _{0,3}
S _{1,0}		S _{1,2}	S _{1,3}
S _{2,0}	l	S _{2,2}	S _{2,3}
S _{3,0}	S _{3,1}		S _{3,3}

- Each byte is seen as an element of \mathbf{F}_{2^8} =GF(2⁸)
 - **F**₂₈ finite field of 256 elements
 - Operations
 - Elements of \mathbf{F}_{2^8} are viewed as polynomials of degree 7 with coefficients $\{0, 1\}$
 - Addition: polynomials addition ⇒ XOR
 - Multiplication: polynomials multiplication modulo $x^8 + x^4 + x^3 + x + 1$

AES Outline

- 1. Initialize State $\leftarrow x \oplus$ RoundKey;
- 2. For each of the Nr-1 rounds:
 - SubBytes(State);
 - 2. ShiftRows(State);
 - MixColumns(State);
 - AddRoundKey(State);
- 3. Last round:
 - SubBytes(State);
 - 2. ShiftRows(State);
 - AddRoundKey(State);
- 4. Output $y \leftarrow$ State

Implementation Aspects

- Can be efficiently implemented on 8-bit CPU
 - byte substitution works on bytes using a table of 256 entries
 - shift rows is a simple byte shifting
 - add round key works on byte XORs
 - mix columns requires matrix multiply in GF(2⁸) which works on byte values, can be simplified to use a table lookup

Implementation Aspects

- Can be efficiently implemented on 32-bit CPU
 - redefine steps to use 32-bit words
 - can pre-compute 4 tables of 256-words
 - then each column in each round can be computed using 4 table lookups + 4 XORs
 - at a cost of 16Kb to store tables
- Designers believe this very efficient implementation was a key factor in its selection as the AES cipher

Hashing Functions and Message Digests

Goal:

- Input: long message
- Output: short block (called hash or message digest)
- Desired properties:
 - Pre-image: Given a hash h it is computationally infeasible to find a message that produces h
 - Second preimage
 - Collisions
- Examples: http://www.slavasoft.com/quickhash/links.htm
 - Secure Hash Algorithm (SHA-1, SHA-2) by NIST
 - MD2, MD4, and MD5 by Ron Rivest [RFC1319, 1320, 1321]
 - SHA-1: output 160 bits
 - SHA-2: output 256-384-512 believed to be more secure than others
 - SHA-3: ongoing competition with objective of 2012 http://csrc.nist.gov/groups/ST/hash/timeline.html

Birthday Attacks

- Is a 64-bit hash secure?
 - Brute force: 1ns per hash $=> 10^{13}$ seconds over 300 thousand years
- But by Birthday Paradox it is not
- Example: what is the probability that at least two people out of 23 have the same birthday? P > 0.5

Birthday attack technique

- opponent generates 2^{m/2} variations of a valid message all with essentially the same meaning
- opponent also generates 2^{m/2} variations of a desired fraudulent message
- two sets of messages are compared to find pair with same hash (probability > 0.5 by birthday paradox)
- have user sign the valid message, then substitute the forgery which will have a valid signature
- Need to use larger MACs

Message Digest 5 (MD5) by R. Rivest [RFC1321]

- Input: message of arbitrary length
- Output: 128-bit hash
- Message is processed in blocks of 512 bits (padding if necessary)
- Security: not recommended
 - Designed to resist to the Birthday attack
 - Collisions where found in MD5, SHA-0, and almost found for SHA-1
 - Near-Collisions of SHA-0, Eli Biham, Rafi Chen, Proceedings of Crypto 2004, http://www.cs.technion.ac.il/~biham/publications.html
 - Collisions for Hash Functions MD4, MD5, HAVAL-128 and RIPEMD, Xiaoyun Wang and Dengguo Feng and Xuejia Lai and Hongbo Yu, http://eprint.iacr.org/2004/199.pdf
 - MD5 considered harmful today: creating a rogue CA certificate, Alexander Sotirov, Marc Stevens, Jacob Appelbaum, Arjen Lenstra, David Molnar, Dag Arne Osvik, Benne de Weger, December 30, 2008

Applications of Hashing Functions

- Authentication: how?
- Encryption: how?
- Message Authentication Codes

Message Authentication Code (MAC) Using an Encryption Algorithm

- Also called Message Integrity Code (MIC)
- Goal:
 - Detect any modification or forgery of the content by an attacker
- Some techniques:
 - Simple techniques have flaws
 - Use CBC mode, send only the last block (residue) along with the plaintext message
 - For confidentiality + integrity:
 - Use two keys (one for CBC encryption and one for CBC residue computation)
 - Append a cryptographic hash to the message before CBC encryption
 - New technique: use a Nested MAC technique such as HMAC

HMAC

- $\mathsf{HMAC}_{\mathsf{K}}(\mathsf{x}) = \mathsf{SHA-1}((\mathsf{K} \oplus \mathit{opad}) \mid \mathsf{SHA-1}((\mathsf{K} \oplus \mathit{ipad}) \mid \mathsf{x}))$
 - *ipad* = 3636...36; *opad* = 5C5C...5C
- HMAC can be combined with any hashing function
- Proven to be secure under some assumptions...



Public Key Systems

Asymmetric cryptosystems

- Invented by Diffie and Hellman [DH76], Merkle
 - When DES was proposed for standardization
- Asymmetric systems are much slower than the symmetric ones (~1000 times)
- Advantages:
 - does not require a shared key
 - simpler security architecture (no-need to a trusted third party)

Public Key Encrypted Message Private Key







Modular Arithmetic

- Modular addition:
 - E.g., $3 + 5 = 1 \mod 7$
- Modular multiplication:
 - E.g., 3 * 4 = 5 mod 7
- Modular exponentiation:
 - E.g., $3^3 = 6 \mod 7$
- Group, Rings, Finite/Galois Fields ...

RSA Cryptosystem [RSA78]

•
$$E(M) = M^e \mod n = C$$

$$D(C) = C^d \bmod n = M$$

(Encryption)

(Decryption)

RSA parameters:

•
$$n = pq, \phi(n) = (p-1)(q-1)$$

•
$$e$$
, with gcd($\phi(n)$, e) = 1, 1< e < $\phi(n)$

$$\bullet d = e^{-1} \bmod \phi(n)$$

 $D(E(M)) = M^{ed} \bmod n = M^{k\phi(n)+1} = M$

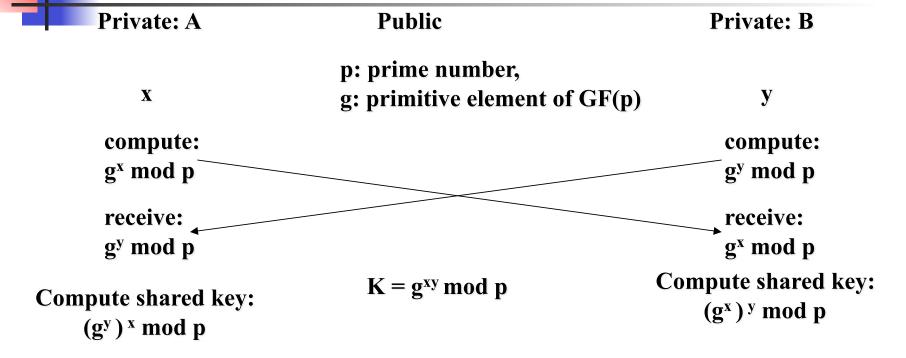
Prime Numbers Generation

- Density of primes (prime number theorem):
 - $\pi(x) \sim x/\ln(x)$
- Sieve of Erathostène
 - Try if any number less than SQRT(n) divides n
- Based on Fermat's Little Theorem but does not detect Carmichael numbers
 - $b^{n-1} = 1 \mod n$ [if there exists b s.t. gcd(b, n) = 1 and $b^{n-1} \neq 1 \mod n$ then n does not pass Fermat's test for half b's relatively prime with n]
- Solovay-Strassen primality test
 - If n is not prime at least 50% of b fail to satisfy the following:
 - $b^{(n-1)/2} = J(b, n) \mod n$
- Rabin-Miller primality test
 - If n is not prime then it is not pseudoprime to at least 75% of b<n:</p>
 - Pseudoprime: $n-1 = 2^s t$, $b^t = \pm 1 \mod n$ **OR** $b^{t2^r} = -1 \mod n$ for some r<r
 - Probabilistic test, deterministic if the Generalized Riemann Hypothesis is true
- Deterministic polynomial time primality test [Agrawal, Kayal, Saxena'2002]
 Network Security
 Cryptography Overview

Use of RSA

- Encryption (A wants to send a message to B):
 - A uses the public key of B and encrypts M (i.e., $E_B(M)$)
 - Since only B has the private key, only B can decrypt M (i.e., $M = D_B(M)$
- Digital signature (A want to send a signed message to B):
 - Based on the fact that $E_A(D_A(M)) = D_A(E_A(M))$
 - A encrypts M using its private key (i.e., $D_A(M)$) and sends it to B
 - B can check that $E_A(D_A(M)) = M$
 - Since only A has the decryption key, only can generate this message

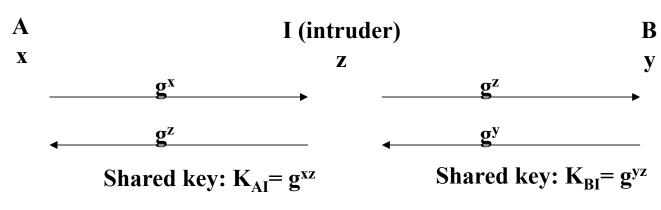
Diffie-Hellman Key Exchange



- Based on the difficulty of computing discrete logarithms
- Works also in extension Galois fields: GF(pq)

Attack on Diffie-Hellman Scheme: Public Key Integrity

Man-in-the-Middle Attack



Message encrypted using K_{AI}

Decrypt using K_{AI} +Decrypt using K_{BI}

- Need for a mean to verify the public information: certification
- Another solution: the Interlock Protocol (Rivest & Shamir 1984)

El Gamal Scheme

Parameters:

- p: prime number
- *g*<*p*: random number
- x<p: random number</p>
- $y = g^x \mod p$
- Encryption of message M:
 - choose random k < p-1</p>
 - $\bullet \quad a = g^k \bmod p$
 - $b = y^k M \mod p$
- Decryption:
 - $M = b/y^k \mod p = b/g^{xk} \mod p = b/a^x$
- Message signature
 - choose random k relatively prime with p-1
 - find b: $M = (xa + kb) \mod (p-1)$ (extended Euclid algorithm)
 - signature(M) = (a, b)
 - verify signature: $y^a a^b \mod p = g^M \mod p$

(public, chosen)
(public, chosen)
(private, chosen)
(public, computed)

Knapsack

- Introduced by R. Merkle
- Based on the difficulty of solving the Knapsack problem in polynomial time (Knapsack is an NP-complete problem)

```
• cargo vector: a = (a_1, a_2, ..., a_n) (seq. Int)
```

• plaintext msg:
$$x = (x_1, x_2, ..., x_n)$$
 (seq. Bits)

• ciphertext:
$$S = a_1 x_1 + a_2 x_2 + ... + a_n x_n$$

- $a_i = wa'_i$ such that $a'_i > a'_1 + ... + a'_{i-1}$, $m > a'_1 + ... + a'_n$
- w is relatively prime with m
- One-round Knapsack was broken by A. Shamir in 1982
- Several variations of Knapsack were broken

Others

- Elliptic Curve Cryptography (ECC)
- Zero Knowledge Proof Systems

Building Security Services

- Confidentiality:
 - Use an encryption algorithm
 - Generally a symmetric algorithm
- Integrity:
 - MAC algorithm
- Access control:
 - Use access control tables
- Authentication
 - Use authentication protocols
- Non-repudiation
 - Digital signatures