

# Super-resolution for MAX-SAT

November 15, 2006

We use  $N$  to keep track of the best assignment so far.  $N$  is a complete assignment, and is assigned arbitrarily at the beginning.

1. Unit-Propagation:

$$M||F, C + k||N \Rightarrow Mk||F, C + k||N$$

if  $C + k$  is a super-resolvent, and  
 $M \vdash \neg C$ , and  
 $k$  is undefined in  $M$ .

or if  $C + k$  is not a super-resolvent, and  
 $M \vdash \neg C$ , and  
 $k$  is undefined in  $M$ , and  
 $unsat(M\neg k; F, C + k) \geq unsat(N; F, C + k)$ .

2. Semi-Super-resolution:

$$I||F||N \Rightarrow I||F, (\text{the disjunction of the negated decision literals in } I)||N$$

if  $R = \text{Contradiction}(I, F) \neq \emptyset$ , and  
 $unsat(IR; F) \geq unsat(N; F)$ .

Informal: Intuitively, since  $R$  is driven by  $I$  through unit-propagation, thus, the fact that " $unsat(IR; F) \geq unsat(N; F)$ " implies that we have made a mistake by setting the partial interpretation to  $I$ , which is the reason why we add the negated decision literals in  $I$  to  $F$  so that we won't make the same mistake again.

$\text{Contradiction}(I, F)$ : there is a sequence of transitions from the state  $I||F||N$  by Unit-Propagation to a state  $IR||F||N$  where some clause(s) is unsatisfied by  $(IR)$ . Contradiction returns  $R$  if there is a contradiction and  $\emptyset$  otherwise.

3. Decide:

$$M||F||N \Rightarrow Mk^*||F||N$$

if  $k$  is undefined in  $M$ , and  
 $k$  and  $\neg k$  occur in some clause(s) of  $F$ .

4. Finale:

$$M||F||N \Rightarrow M||F||N$$

if  $unsat(M; F) = unsat(N; F)$ , and  
 $M$  is complete, and  
 $M$  contains no decision literals.

5. Restart:

$$M||F||N \Rightarrow \emptyset||F||N$$

6. Update:

$$M||F||N \Rightarrow M||F||M$$

if  $M$  is complete, and  
 $unsat(M; F) < unsat(N; F)$ .

7. Subsumption:

$$M||F, SR_1, SR_2||N \Rightarrow M||F, SR_2||N$$

if  $SR_1$  and  $SR_2$  are super-resolvents, and  
 $SR_2$  is a subset of  $SR_1$ .