Hash-based Index

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Outline

Deep dive Hash Index

Hashed-Based Indexing

- Static Hashing: A simple solution; does not support incremental maintenance
- Extendible Hashing: A more advanced incremental hash-based index
 - Gracefully supports inserting and deleting data entries
- Linear Hashing: Another incremental hash-based index

Why is Indexing necessary?

- There are lots of data structures like trees, DAGs, and things with many algorithms that operate on them efficiently.
- Why don't these algorithms and data structures translate directly into disk-space structures?
- Pointers work nicely in main memory -- how do you represent pointers in main memory?
- Data structures can be arbitrarily sized, but disk blocks are fixed size (and are larger than many objects).
- Files typically only grow at the end -- they don't support "insert into the middle."

Introduction

- As for any index, 3 alternatives for data entries k*:
 - Data record with key value k
 - <k, rid of data record with search key value k>
 - <k, list of rids of data records with search key k>
 - Choice orthogonal to the indexing technique
- <u>Hash-based</u> indexes are best for <u>equality selections</u>. <u>Cannot</u> support range searches.
- Static and dynamic hashing techniques exist; trade-offs similar to ISAM vs. B+ trees.

Hashing mechanism

- Your index is a collection of buckets (bucket = page)
- Define a hash function, h, that maps a key to a bucket.
- Store the corresponding data in that bucket.
- Collisions
 - Multiple keys hash to the same bucket.
 - Store multiple keys in the same bucket.
- What do you do when buckets fill?
 - Chaining: link new pages(overflow pages) off the bucket.

Hashing to search key

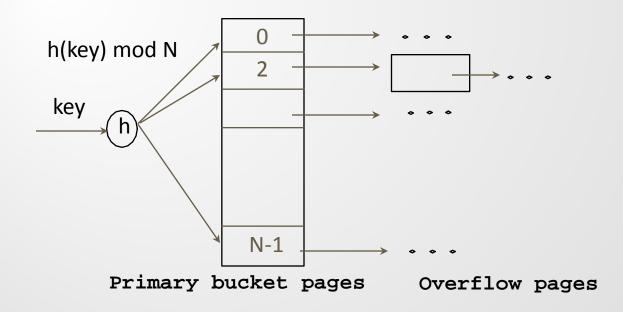
- Buckets contain data entries.
- Hash fn works on search key field of record r. Must distribute values over range 0 ... M-1.
 - h(key) = (a * key + b) usually works well.
 - a and b are constants; lots known about how to tune h.
- Long overflow chains can develop and degrade performance.
 - Extendible and Linear Hashing: Dynamic techniques to fix this problem.

Static vs. Dynamic Hashing

- Static: number of buckets predefined; never changes.
 - Either, overflow chains grow very long, OR
 - A lot of wasted space in unused buckets.
- Dynamic: number of buckets changes over time.
 - Hash function must adapt.
 - Usually, start revealing more bits of the hash value as the hash table grows.

Static Hashing

- # primary pages fixed, allocated sequentially, never deallocated; overflow pages if needed.
- h(k) mod M = bucket to which data entry with key k belongs.
 (M = # of buckets)



Static Hashing (Contd.)

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Extendible Hashing

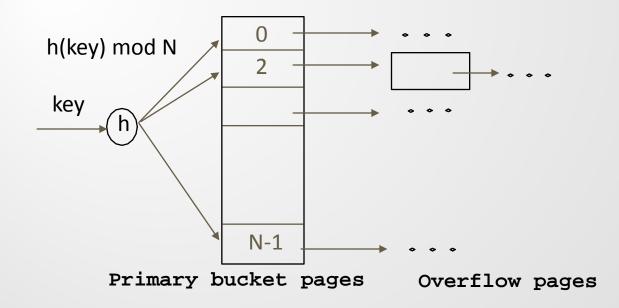
- Situation: Bucket (primary page) becomes full. Why not reorganize file by doubling # of buckets?
 - Reading and writing all pages is expensive!
 - <u>Idea</u>: Use <u>directory of pointers to buckets</u>, double # of buckets by doubling the directory, splitting just the bucket that overflowed!
 - Directory much smaller than file, so doubling it is much cheaper.
 Only one page of data entries is split. No overflow page!
 - Trick lies in how hash function is adjusted!

Static Hash-based Index

- Number of buckets (N) is fixed ahead of time,
 when the index is created
- What happens if we insert a lot of data entries?
 - Long overflow chains of pages, slower search
- Might consider periodically doubling N and "rehashing" the file
 - Entire file has to be read and written (expensive)
 - Index unavailable while reorganizing
 - Extendible hashing is a dynamic hash index, which helps fix this problem

Static Hashing

- # primary pages fixed, allocated sequentially, never deallocated; overflow pages if needed.
- h(k) mod M = bucket to which data entry with key k belongs.
 (M = # of buckets)



Static hashing

- Buckets map to pages.
 - Must be able to directly translate from a bucket number to a page number.
 - Where do you store overflow pages?
 - If number of buckets is fixed (static hashing), store overflow buckets after regular buckets.
 - Use free list to manage overflow buckets.
- Static hashing isn't very practical for databases.
- Databases change in size fairly substantially.
- If you have to pre-allocate, often waste space

Extendible Hashing

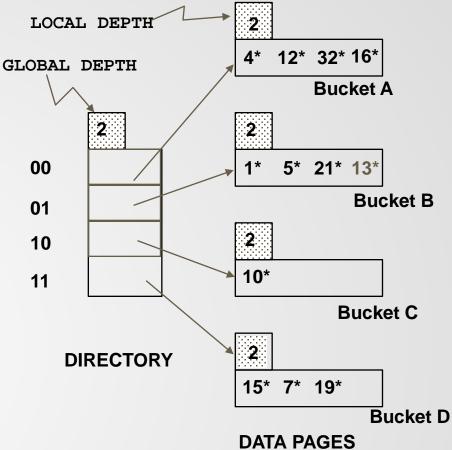
- Main Idea: Use a directory of (logical) pointers to bucket pages
- On overflow, double the directory (not # number of buckets)
 - Why does this help?
 - Directory much smaller than entire index
 - Only one page of data entries is split at a time
 - No overflow pages

Extendible Hashing

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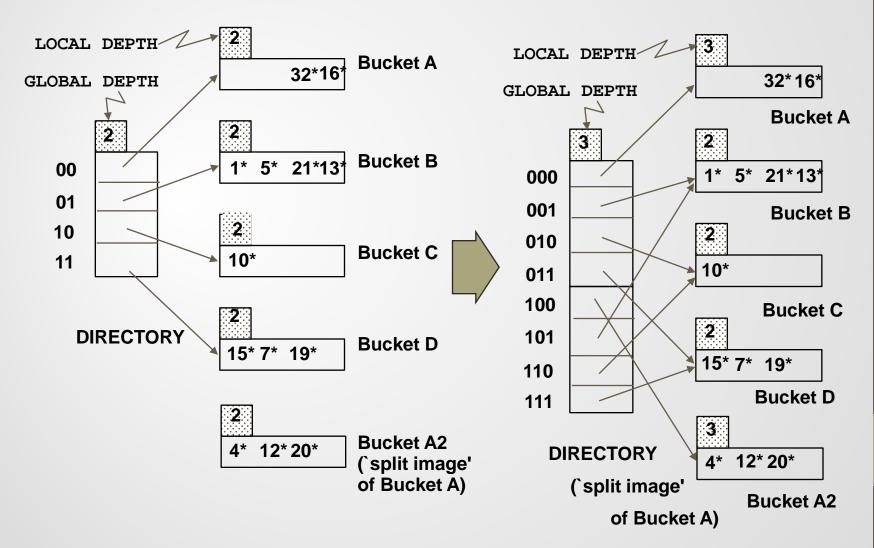


- Directory is array of size 4.
- To find bucket for r, take last `global depth' # bits of h(r); we denote r by h(r).
 - If h(r) = 5 = binary 101, it is in bucket pointed to by 01.



- **❖** <u>Insert</u>: If bucket is full, <u>split</u> it (allocate new page, re-distribute).
- If necessary, double the directory. (As we will see, splitting a bucket does not always require doubling; we can tell by comparing global depth with local depth for the split bucket.)

Insert h(r)=20 (Causes Doubling)



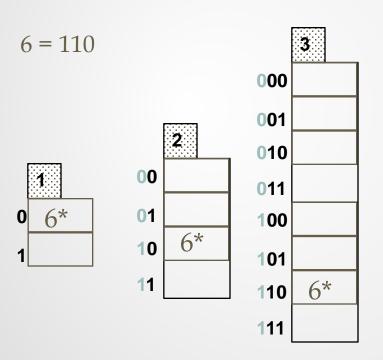
Points to Note

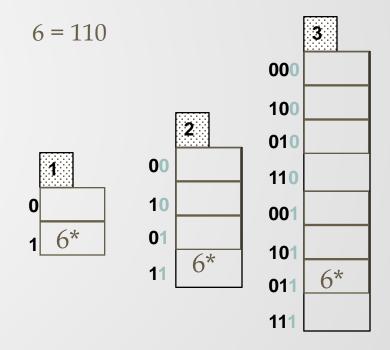
- 20 = binary 10100. Last **2** bits (00) tell us *r* belongs in A or A2. Last **3** bits needed to tell which.
 - Global depth of directory: Max # of bits needed to tell which bucket an entry belongs to.
 - Local depth of a bucket: # of bits used to determine if an entry belongs to this bucket.
- When does bucket split cause directory doubling?
 - Before insert, local depth of bucket = global depth. Insert causes
 local depth to become > global depth; directory is doubled by
 copying it over and `fixing' pointer to split image page. (Use of least
 significant bits enables efficient doubling via copying of directory!\)

Directory Doubling

Why use least significant bits in directory?

⇔ Allows for doubling via copying!





Comments on Extendible Hashing

- If directory fits in memory, equality search answered with one disk access; else two.
 - 100MB file, 100 bytes/rec, 4K pages contains 1,000,000 records (as data entries) and 25,000 directory elements; chances are high that directory will fit in memory.
 - Directory grows in spurts, and, if the distribution of hash values is skewed, directory can grow large.
 - Multiple entries with same hash value cause problems!
- <u>Delete</u>: If removal of data entry makes bucket empty, can be merged with 'split image'. If each directory element points to same bucket as its split image, can halve directory.

Linear Hashing

- This is another dynamic hashing scheme, an alternative to Extendible Hashing.
- LH handles the problem of long overflow chains without using a directory, and handles duplicates.
- <u>Idea</u>: Use a family of hash functions h₀, h₁, h₂, ...
 - h_i(key) = h(key) mod(2ⁱN); N = initial # buckets
 - h is some hash function (range is not 0 to N-1)
 - If N = 2^{d0} , for some d0, \mathbf{h}_i consists of applying \mathbf{h} and looking at the last di bits, where di = d0 + i.
 - \mathbf{h}_{i+1} doubles the range of \mathbf{h}_{i} (similar to directory doubling)

Linear Hashing (Contd.)

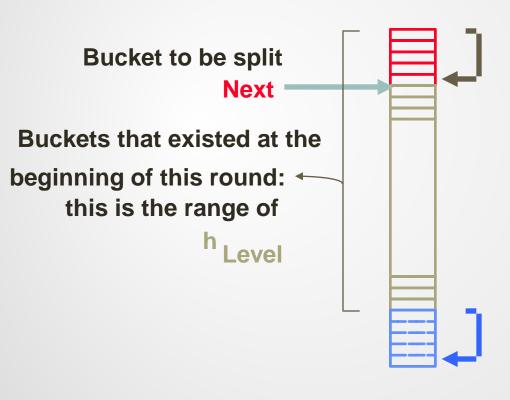
- Directory avoided in LH by using overflow pages, and choosing bucket to split round-robin.
 - Splitting proceeds in `rounds'. Round ends when all N_R initial (for round R) buckets are split. Buckets 0 to Next-1 have been split; Next to N_R yet to be split.
 - Current round number is Level.
 - Search: To find bucket for data entry r, find h_{Level}(r):
 - If $\mathbf{h}_{Level}(r)$ in range `Next to N_R' , r belongs here.
 - Else, r could belong to bucket $\mathbf{h}_{Level}(r)$ or bucket $\mathbf{h}_{Level}(r) + N_R$; must apply $\mathbf{h}_{Level+1}(r)$ to find out.

Dynamic Hashing vs. Linear Hashing

- Dynamic hash implementation.
 - Periodically double the size of the database.
 - Rehash every key into new table.
- Dynamic Linear Hashing (Litwin)
 - Grow table one bucket at a time.
 - Split buckets sequentially; rehash just the splitting bucket.
 - Maintain overflow buckets as necessary.
 - Keep track of max bucket to identify the correct number of bits to consider in the hash value

Overview of LH File

In the middle of a round.



Buckets split in this round:

If h Level (search key value)
is in this range, must use
h Level+1 (search key value)
to decide if entry is in

'split image' bucket.

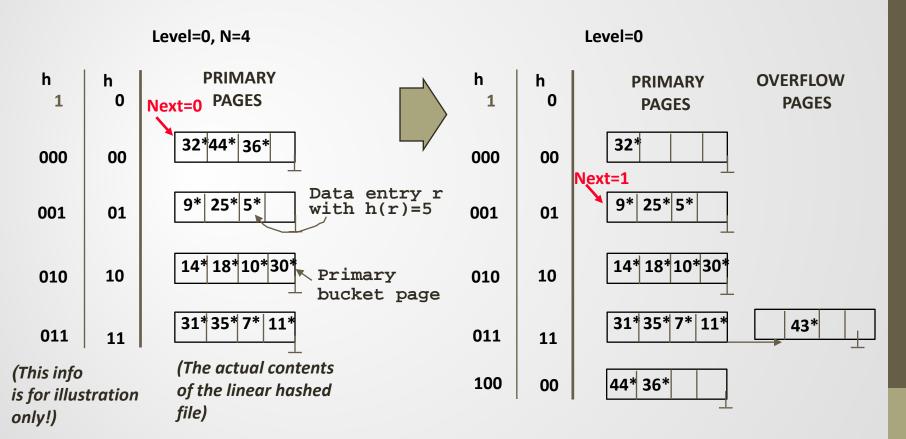
`split image' buckets: created (through splitting of other buckets) in this round

Linear Hashing (Contd.)

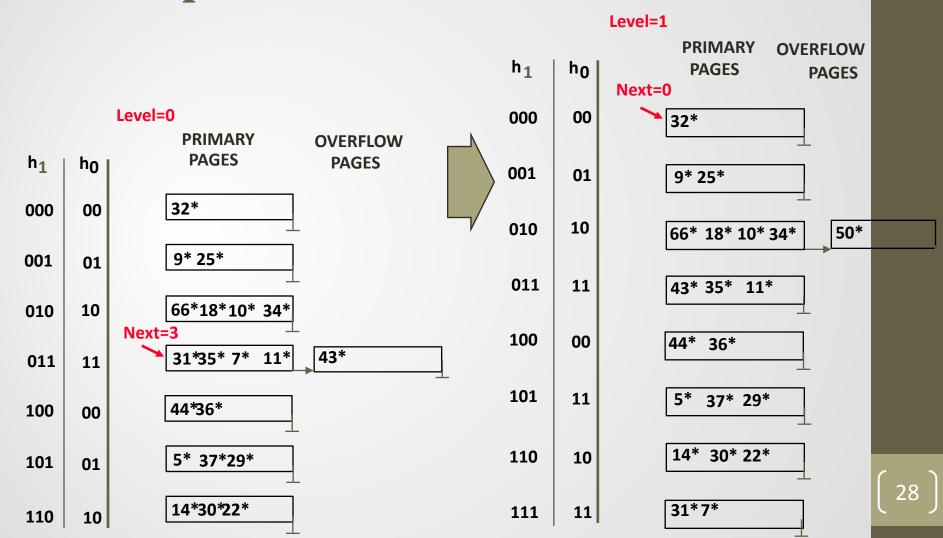
- Insert: Find bucket by applying h_{Level} / h_{Level+1}:
 - If bucket to insert into is full:
 - Add overflow page and insert data entry.
 - (Maybe) Split Next bucket and increment Next.
- Can choose any criterion to `trigger' split.
- Since buckets are split round-robin, long overflow chains don't develop!
- Doubling of directory in Extendible Hashing is similar; switching of hash functions is *implicit* in how the # of bits examined is increased.

Example of Linear Hashing

On split, h_{level+1} is used to redistribute entries.



Example: End of a Round



LH Described as a Variant of EH

- The two schemes are actually quite similar:
 - Begin with an EH index where directory has N elements.
 - Use overflow pages, split buckets round-robin.
 - First split is at bucket 0. (Imagine directory being doubled at this point.) But elements <1,N+1>, <2,N+2>, ... are the same. So, need only create directory element N, which differs from 0, now.
 - When bucket 1 splits, create directory element N+1, etc.
- So, directory can double gradually. Also, primary bucket pages are created in order. If they are *allocated* in sequence too (so that finding i'th is easy), we actually don't need a directory! Voila, LH.

Hash index record

- As for any index, 3 alternatives for data entries
 k*:
 - Data record with key value k
 - <k, rid of data record with search key value k>
 - <k, list of rids of data records with search keyk>

Summary: Hash-Based Indexes

- Hash-based indexes: best for equality searches, cannot support range searches.
- Static Hashing can lead to long overflow chains.
- Extendible Hashing avoids overflow pages by splitting a full bucket when a new data entry is to be added to it. (*Duplicates may require overflow* pages.)
 - Directory to keep track of buckets, doubles periodically.
 - Can get large with skewed data; additional I/O if this does not fit in main memory.

Summary: Linear hashing

- Linear Hashing avoids directory by splitting buckets round-robin, and using overflow pages.
 - Overflow pages not likely to be long.
 - Duplicates handled easily.
 - Space utilization could be lower than Extendible Hashing, since splits not concentrated on `dense' data areas.
 - Can tune criterion for triggering splits to trade-off slightly longer chains for better space utilization.
- For hash-based indexes, a skewed data distribution is one in which the hash values of data entries are not uniformly distributed!