13 November 2014 Analysis I Paul E. Hand hand@rice.edu

HW 11

Due: Nov 18 in class. Justify all of your work.

- 1. Evaluate $\sum_{n=1}^{\infty} n^2/2^n$. Justify the important steps of your calculation.
- 2. IX.6.5
- 3. IX.7.1
- 4. IX.7.4
- 5. Prove that every piecewise constant function $f : [0,1] \to \mathbb{R}$ can be approximated arbitrarily well (in the sense of an L_1 norm) by a continuous function. (A piecewise constant function is the same as a step map, as defined on page 249 in the book). Is the same statement true if approximation is understood in the L^{∞} sense?
- 6. If you were going to present Theorem X.3.1 (page 252) as an in-class presentation, write down the notes of what you would say.