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## Day 16 — Summary — Completion of a Vector Space

- 1.  $\mathbb{R}$  can be defined as the set of equivalence classes of Cauchy sequences of  $\mathbb{Q}$ . This is called the completion of  $\mathbb{Q}$ .
- 2. The completion of a normed vector space is defined as the set of equivalence classes of Cauchy sequences of elements in the space. The completion is a complete normed vector space.