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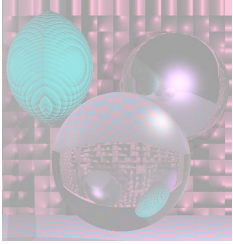
# CS 5310

# Graduate Computer Graphics

Prof. Harriet Fell

Spring 2011

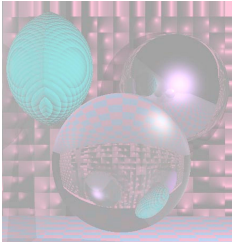
Lecture 1 – January 19, 2011



# Course Overview - Topics

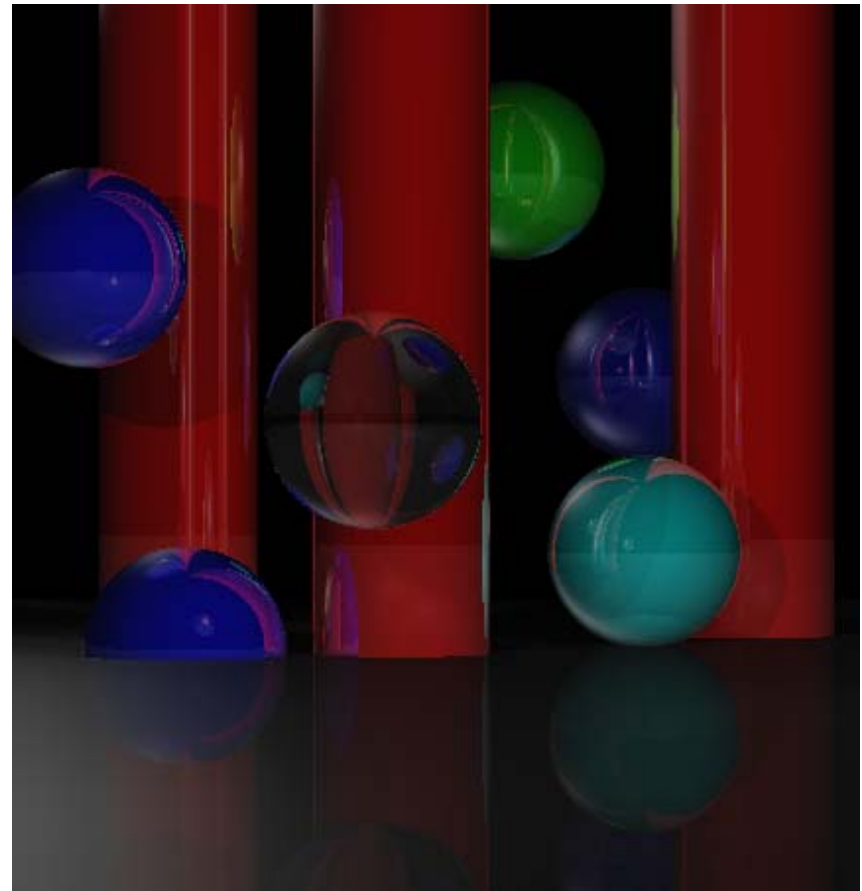
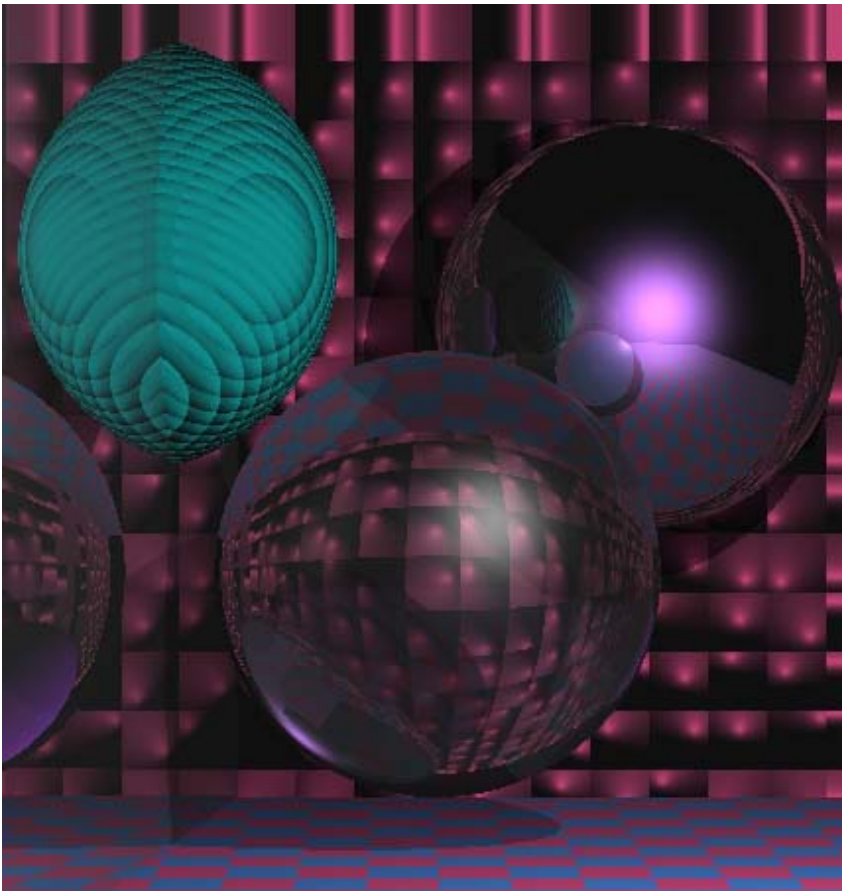
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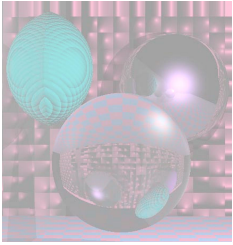
- Emphasis on rendering realistic images.
- Fundamentals of 2- and 3- dimensional computer graphics
  - 2-dimensional algorithms for drawing lines and curves, anti-aliasing, filling, and clipping
  - Using ray-tracing to render 3-dimensional scenes
    - composed of spheres, polygons, quadric surfaces, and bi-cubic surfaces
  - Techniques for adding texture to surfaces using texture and bump maps, noise, and turbulence
- Other topics as time permits



# Sample Images

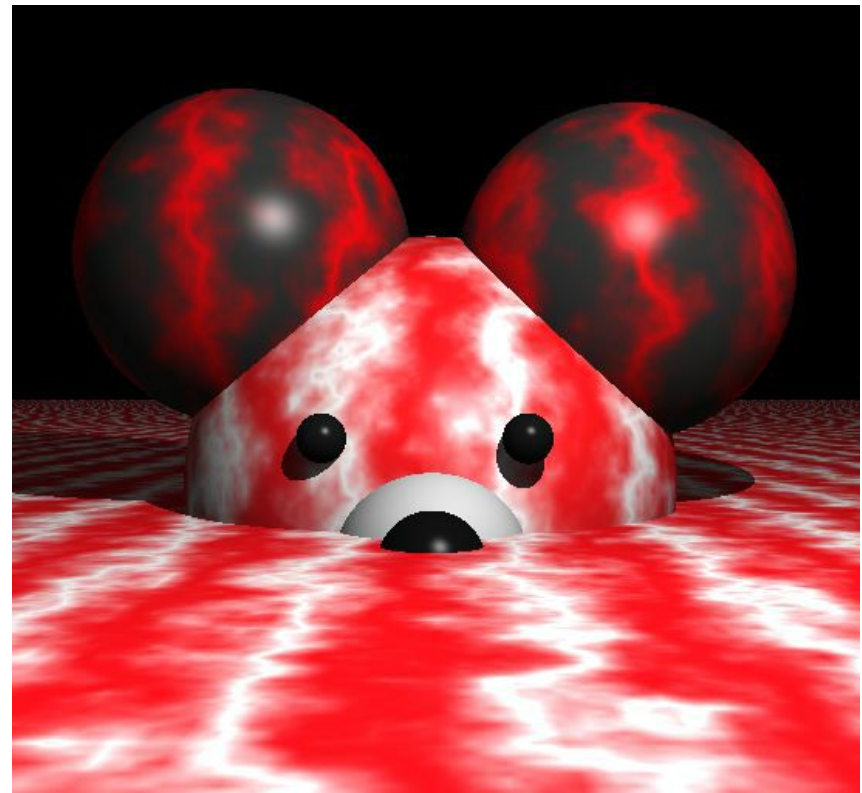
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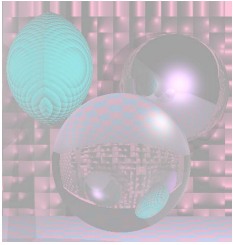




# Sample Images

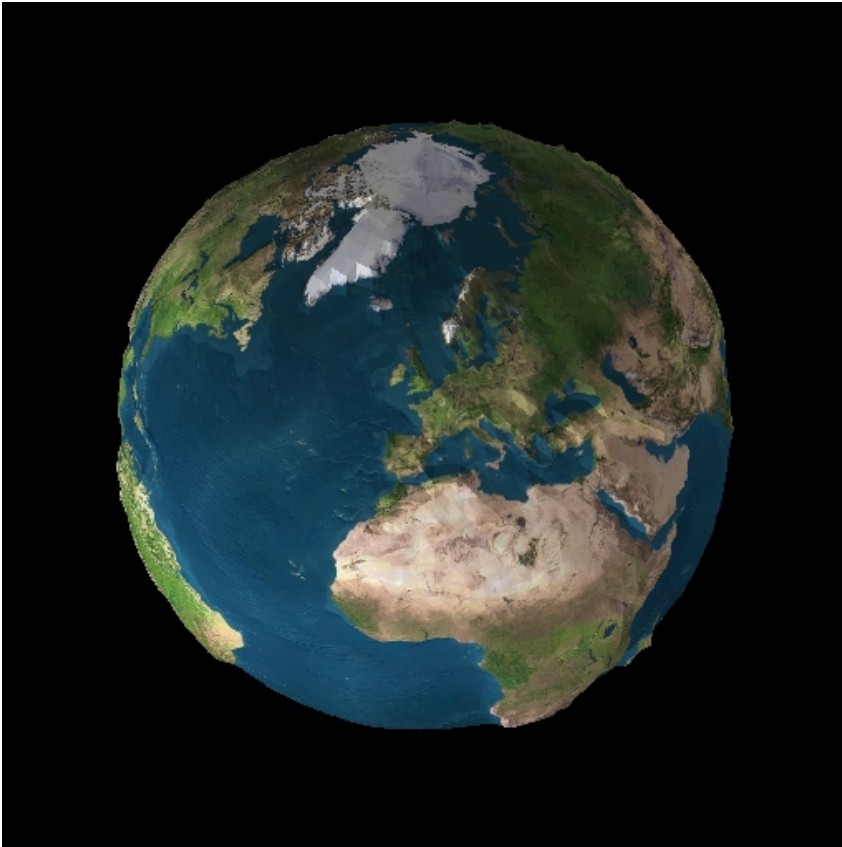
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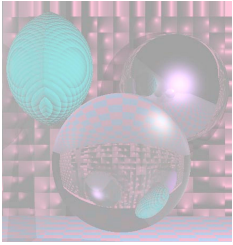




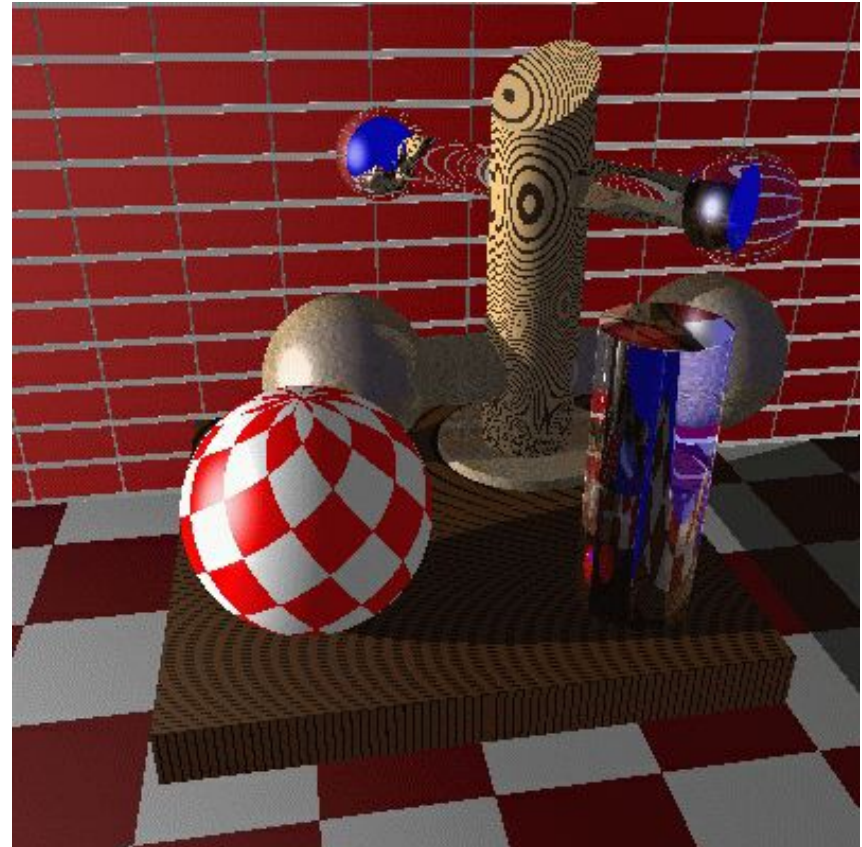
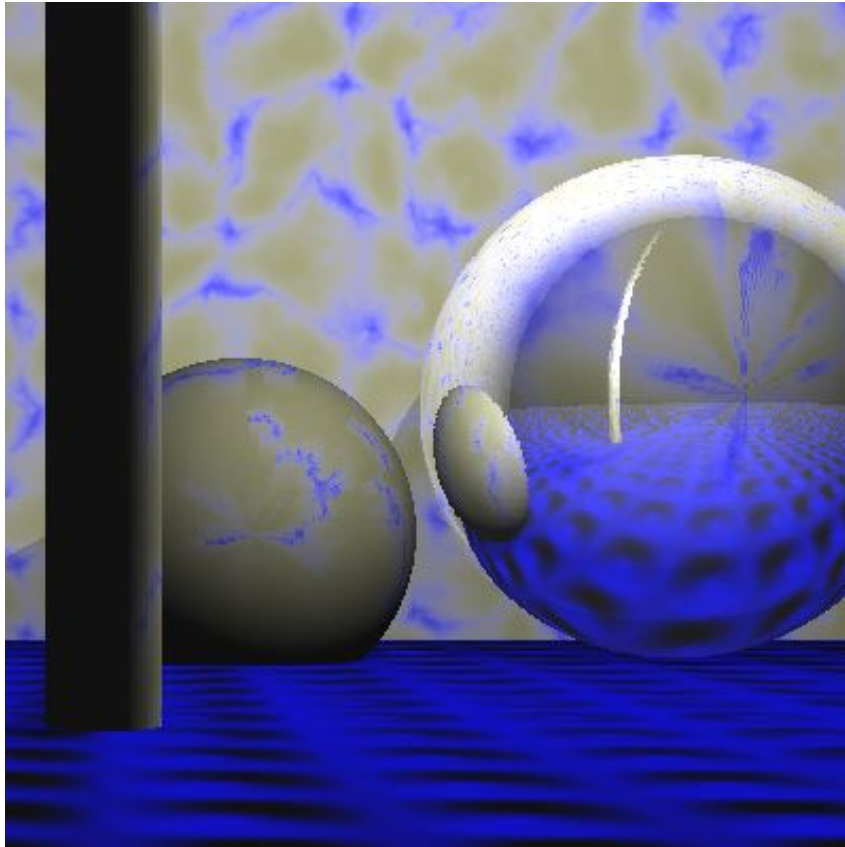
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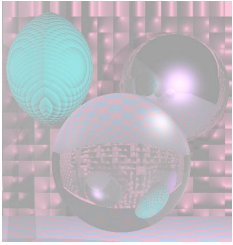
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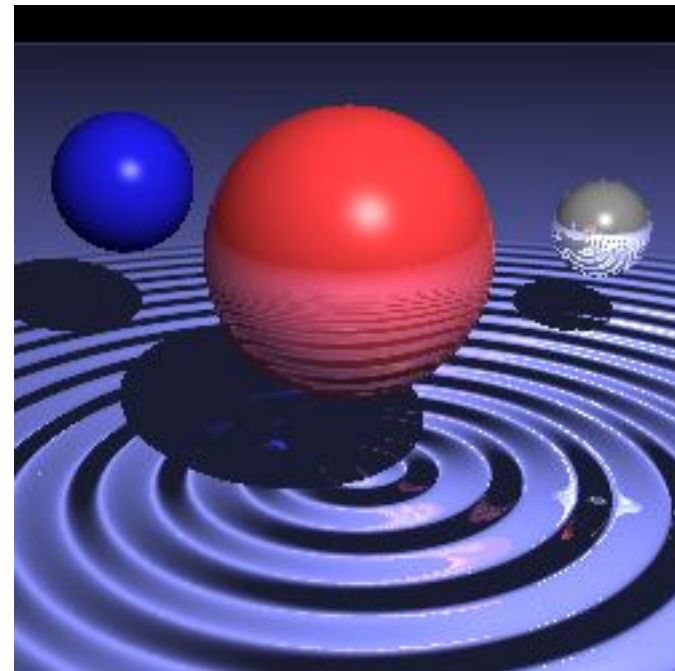
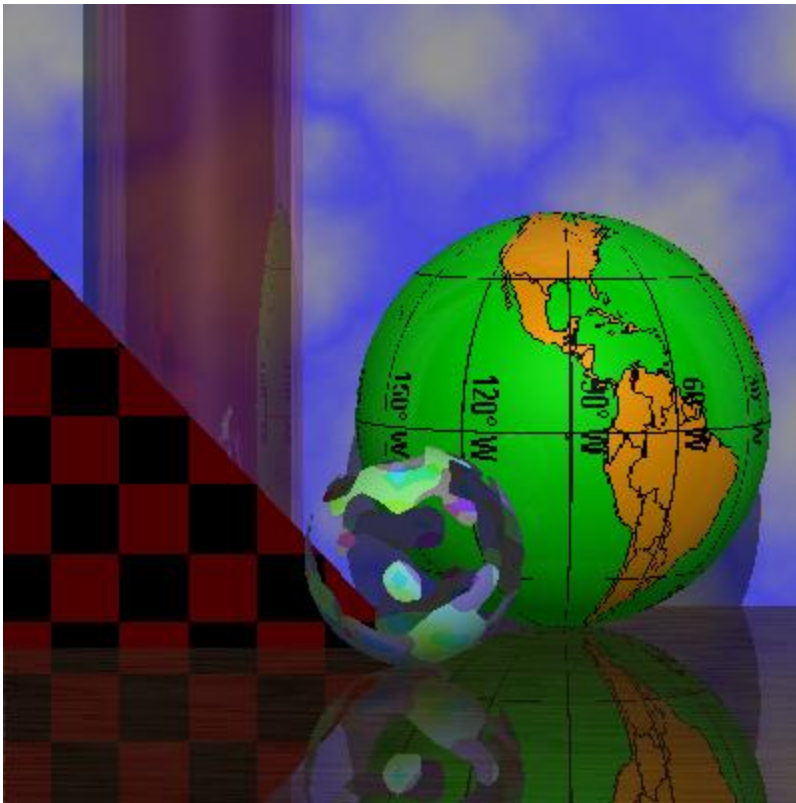
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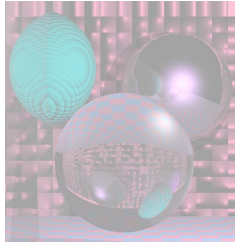




# Sample Images

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# Course Overview - Organization

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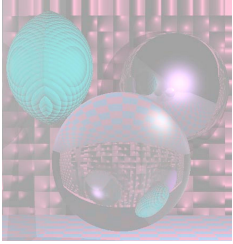
- **Texts:**

- Peter Shirley, *et al.* *Fundamentals of Computer Graphics, 2nd Edition*, A K Peters, 2005
- Alan Watt, *3D Computer Graphics, 3rd Edition*, Addison Wesley, 1999.

- **Grading**

- Assignment 0: 10%
- Assignment 1: 15%
- Assignment 2: 15%
- Assignment 3: 10%
- Assignment 4: 10%
- Exam: 25%
- Project and Presentation: 15%

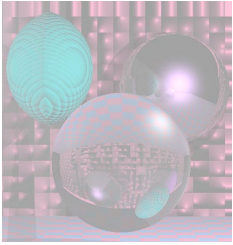




# Early History

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- <http://accad.osu.edu/~waynec/history/timeline.html>
- [http://sophia.javeriana.edu.co/~ochavarr/computer\\_graphics\\_history/historia/](http://sophia.javeriana.edu.co/~ochavarr/computer_graphics_history/historia/)
- 1801 Joseph-Marie Jacquard invented an automatic loom using punched cards to control patterns in the fabrics. The introduction of these looms caused the riots against the replacement of people by machines.
- 1941 First U.S. regular TV broadcast,  
1st TV commercial (for Bulova watches)
- 1948 Transistors
- 1949 Williams tube (CRT storage tube)



# Jacquard Loom

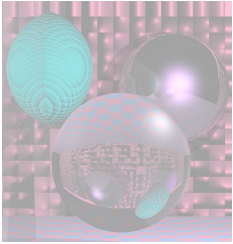


From Wikipedia.org

January 20, 2011

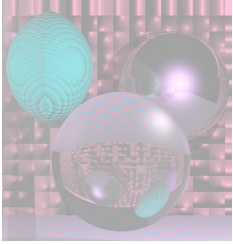
©College of Computer and Information Science, Northeastern University

10



# Early TV

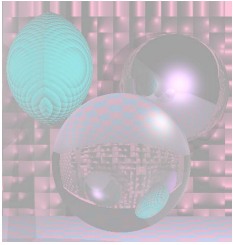




# History – the 50s

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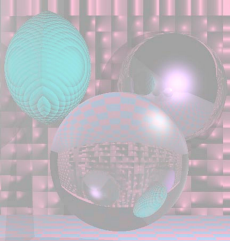
- 1951 Graphics display, Whirlwind computer
- 1954 color TV
- 1955 Light Pen, SAGE- Lincoln Lab
- 1958 Graphics Console, TX-1 MIT
- 1958 John Whitney Sr. uses analog computer to make art



# 1951 Graphics display, Whirlwind computer

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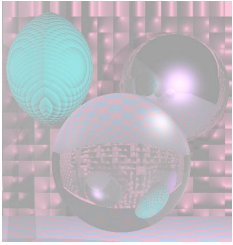




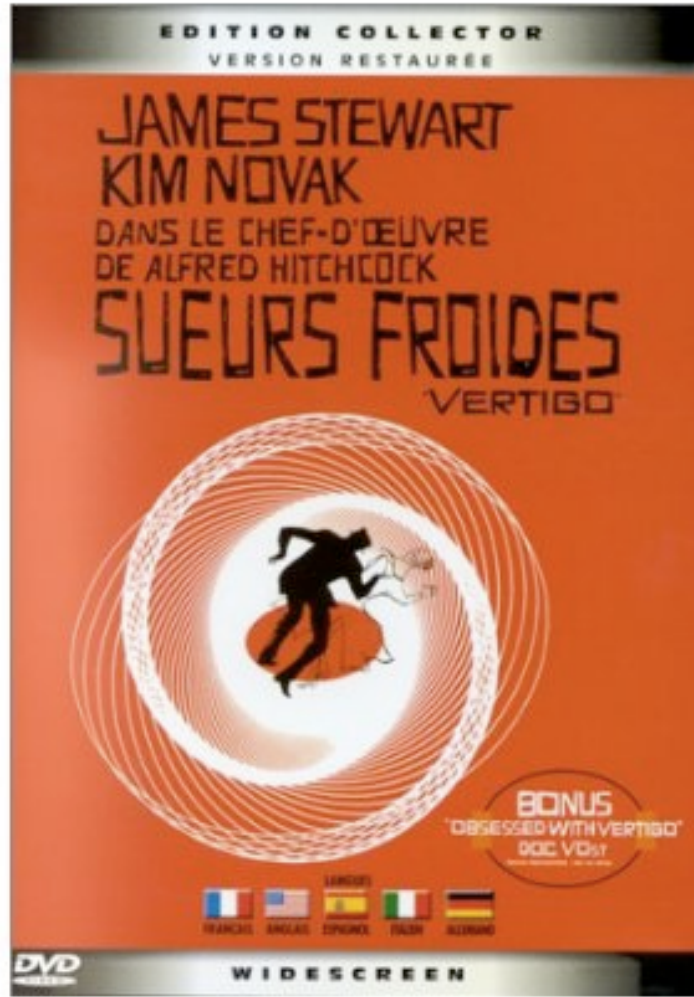
# SAGE

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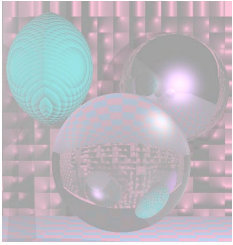




# John Whitney Sr. 1958 CG



## Vertigo Start Titles

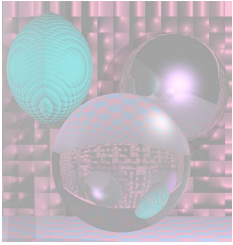


# History - the 60s

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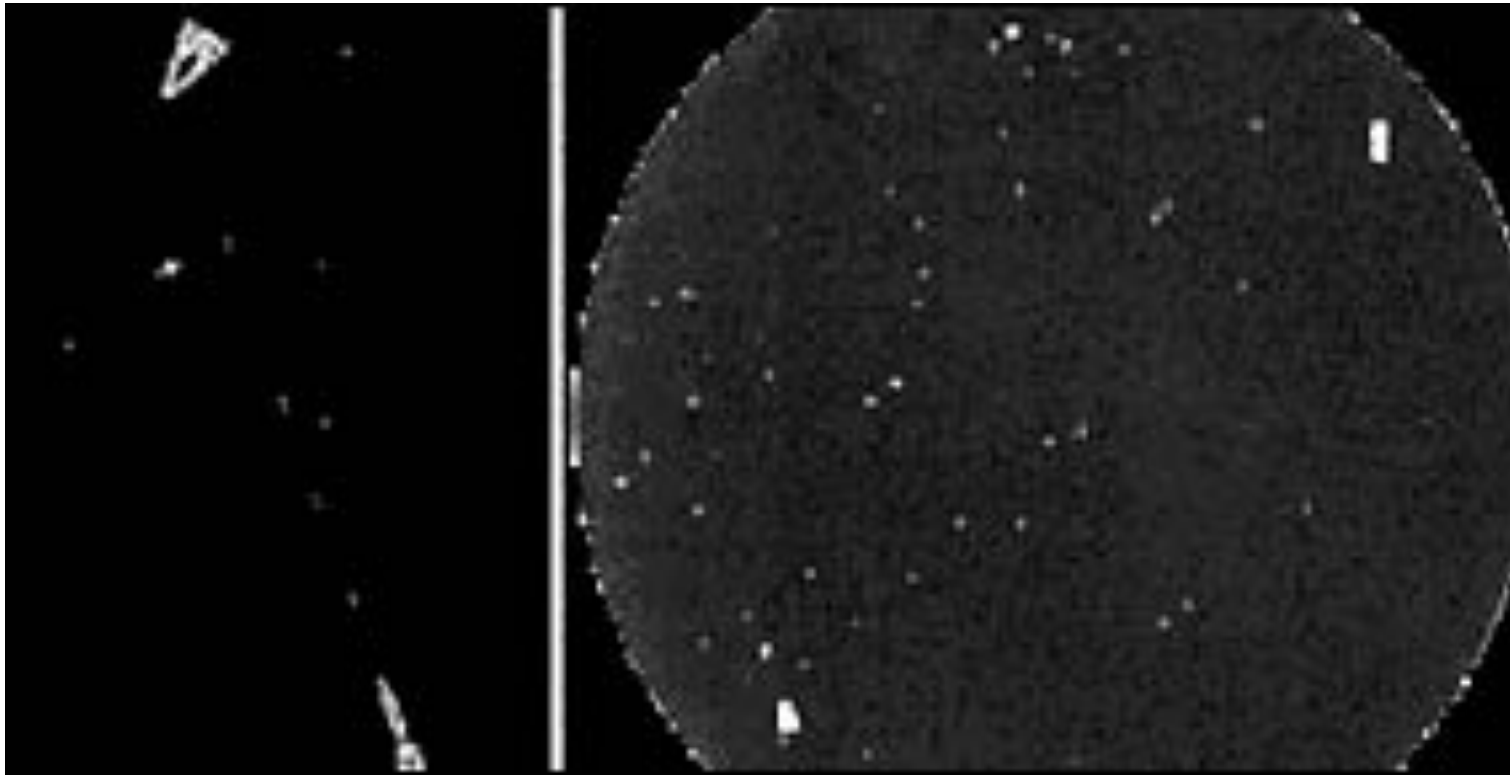
- 1961 Spacewars, 1st video game, Steve Russell, MIT for PDP-1
- **1963** Sketchpad, Ivan Sutherland, MIT
- 1963 Mouse invented, Doug Englebart, SRI
- 1963 Roberts hidden line algorithm, MIT
- 1965 Bresenham Algorithm for plotting lines, IBM
- 1966 Odyssey, home video game, Ralph Baer,
  - Sanders Assoc, is 1st consumer CG product
- 1967 Full-color, real-time, interactive flight simulator for NASA - Rod Rougelet, GE

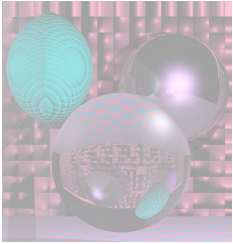




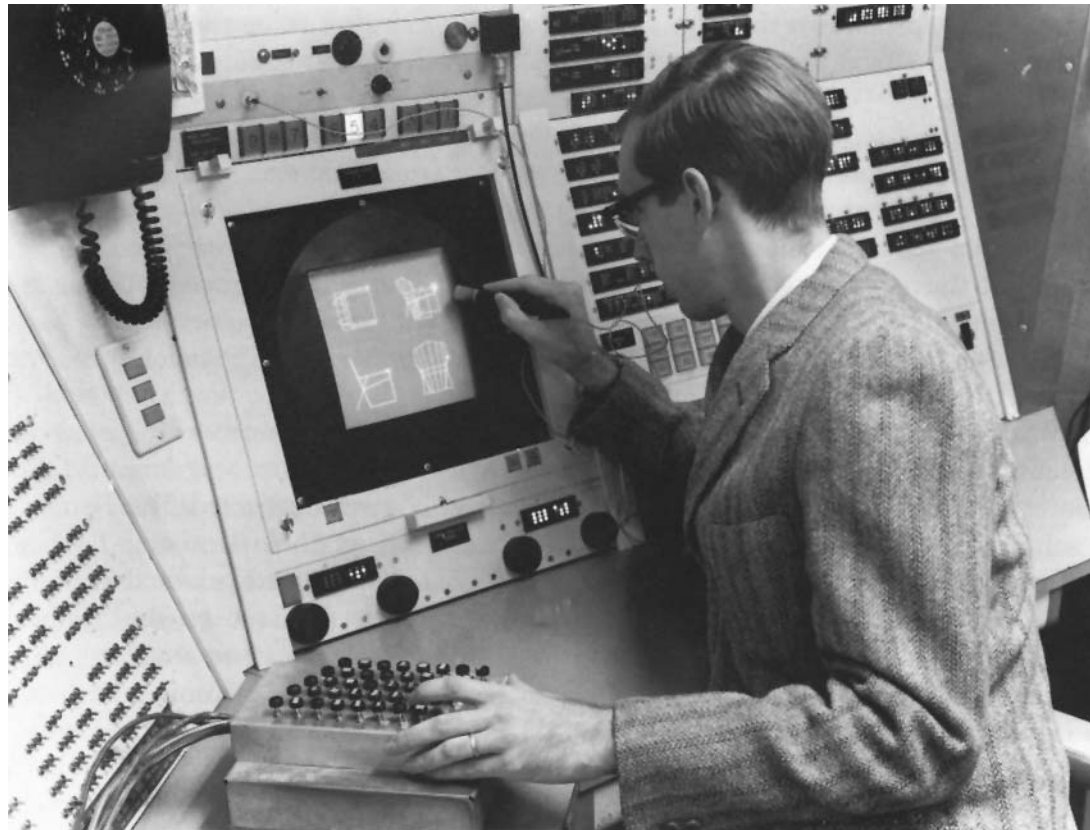
# Spacewars

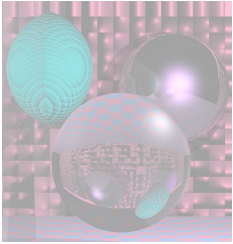
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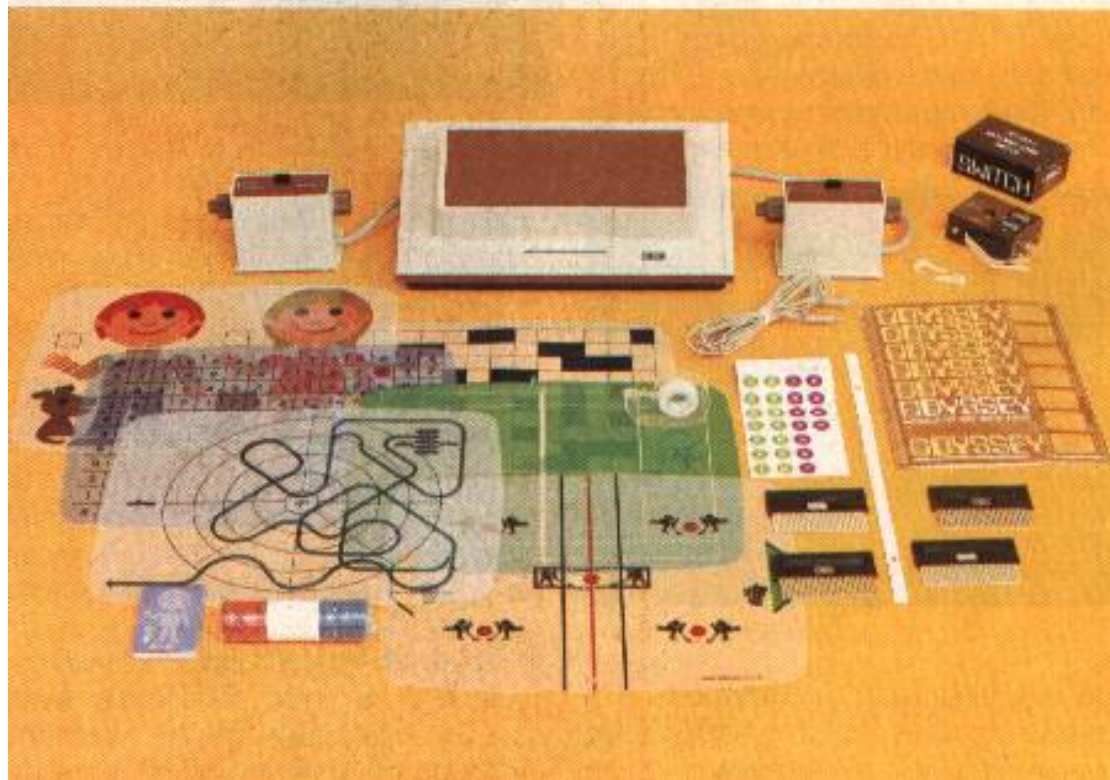
# Ivan Sutherland & Sketchpad System on TX-2 at MIT(1963)



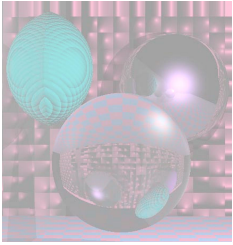


# Odyssey

The very first home videogame, Odyssey, used Laner-created transparent overlays in lieu of computer-generated graphics.

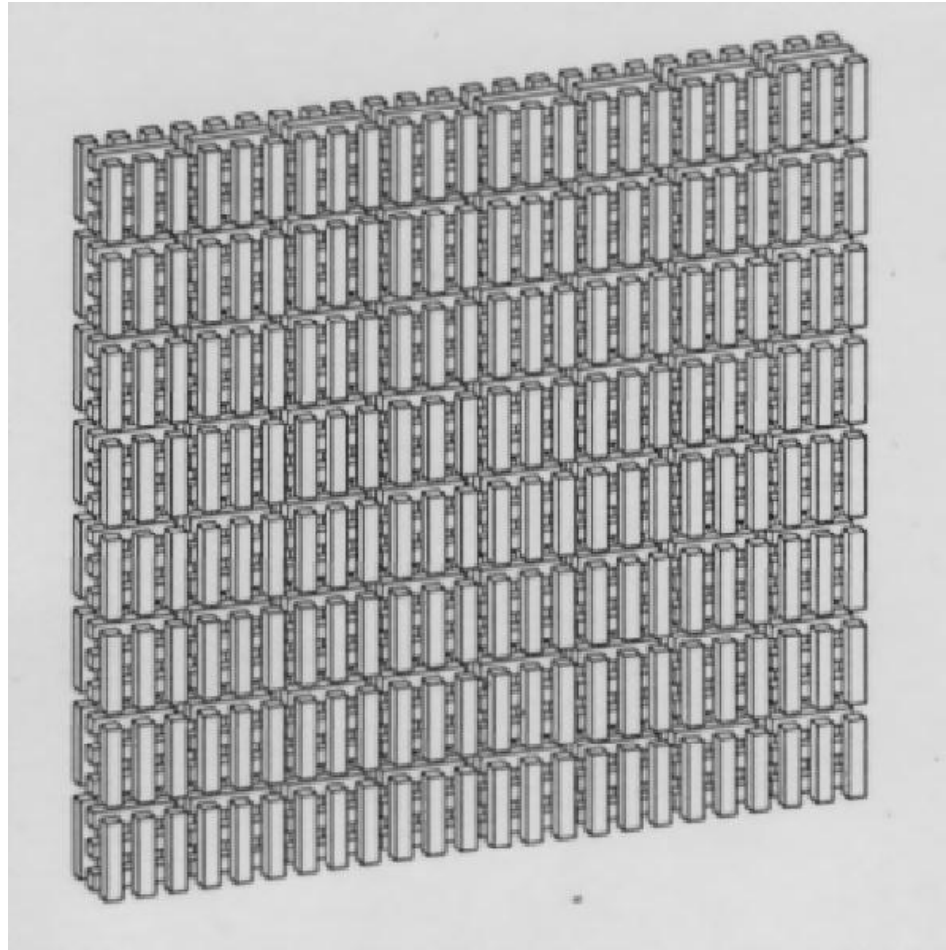


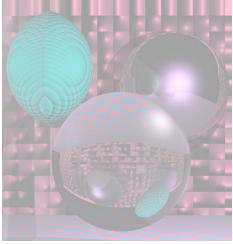
<http://gamesmuseum.pixesthesia.com/history/gen1/pong/>



# Roberts Hidden Line Algorithm Block scene (576 blocks)

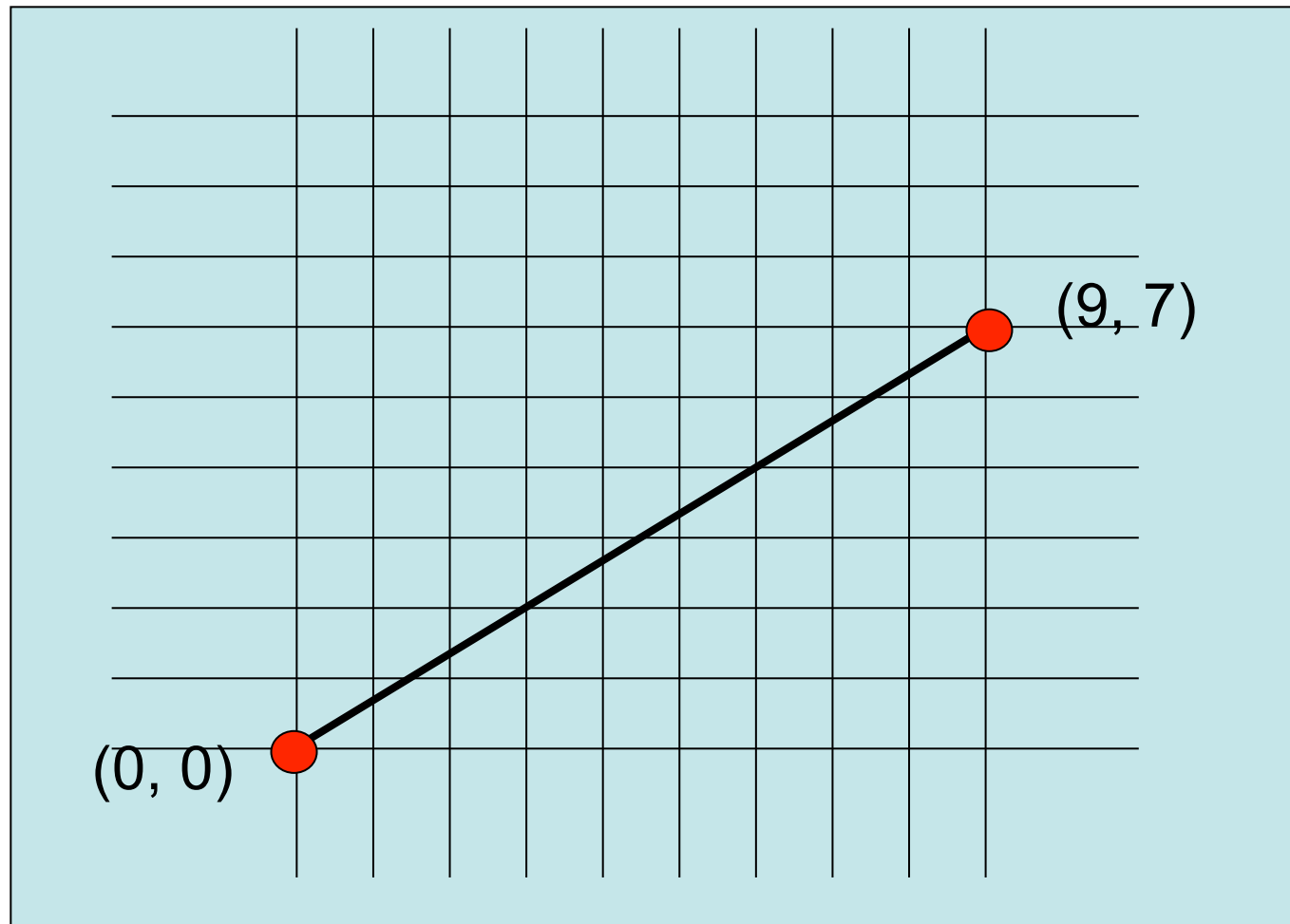
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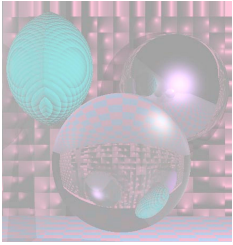




# Bresenham Line Algorithm

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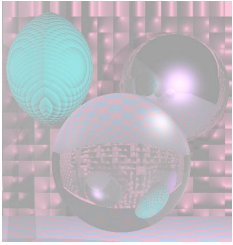




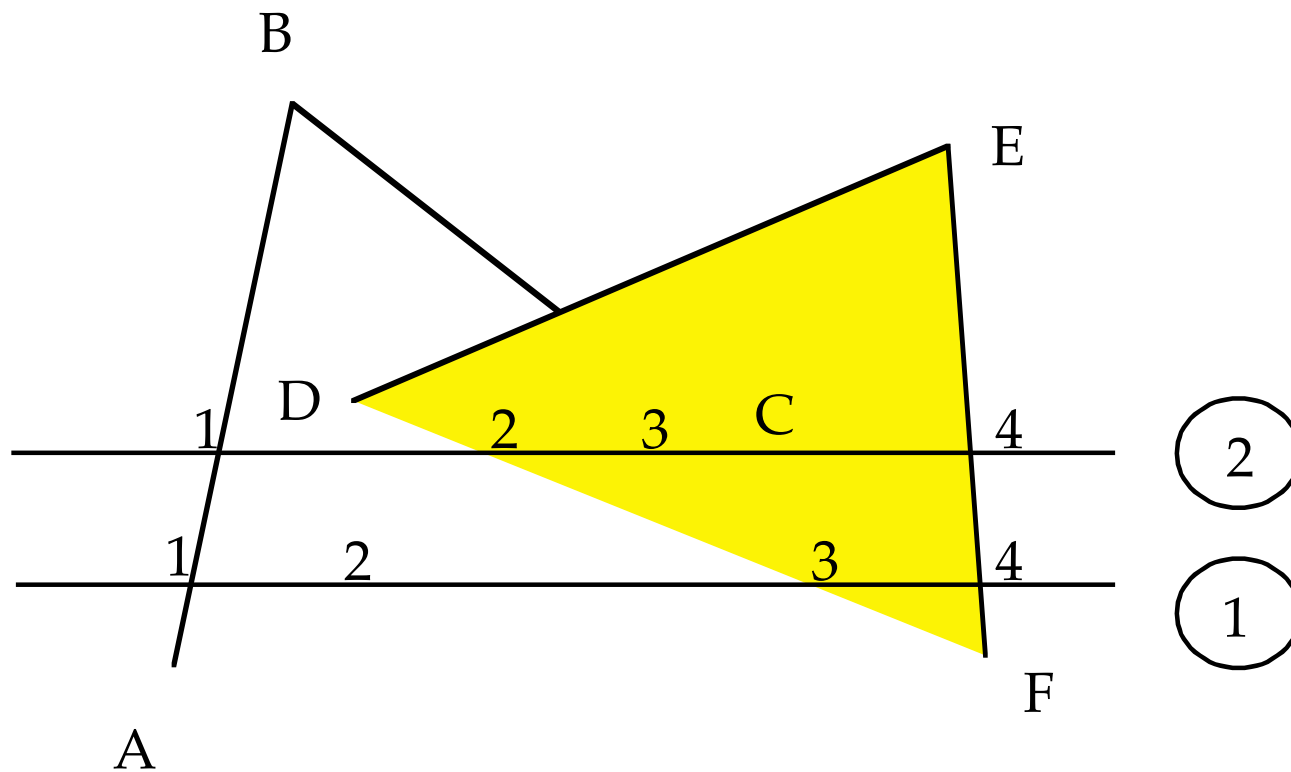
# History – the 70s

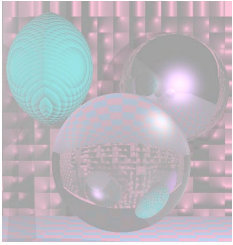
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- **1970s**      **Utah dominated - algorithm development**
- 1970 [Watkins algorithm for visible surfaces](#)
- 1970 [Bezier free-form curve](#) representation
- 1971 [Gouraud shading](#)
- 1973 Principles of Interactive Computer Graphics (Newman and Sproull)
- 1974 Addressable cursor in a graphics display terminal - DEC VT52
- 1974 z-buffer developed by Ed Catmull (Univ of Utah)
- 1975 [Phong shading](#)
- 1975 [Fractals](#) - Benoit Mandelbrot (IBM)
- 1978 [Bump mapping](#), Blinn
- 1979 George Lucas starts Lucasfilm
  - with Ed Catmull, Ralph Guggenheim, and Alvy Ray Smith

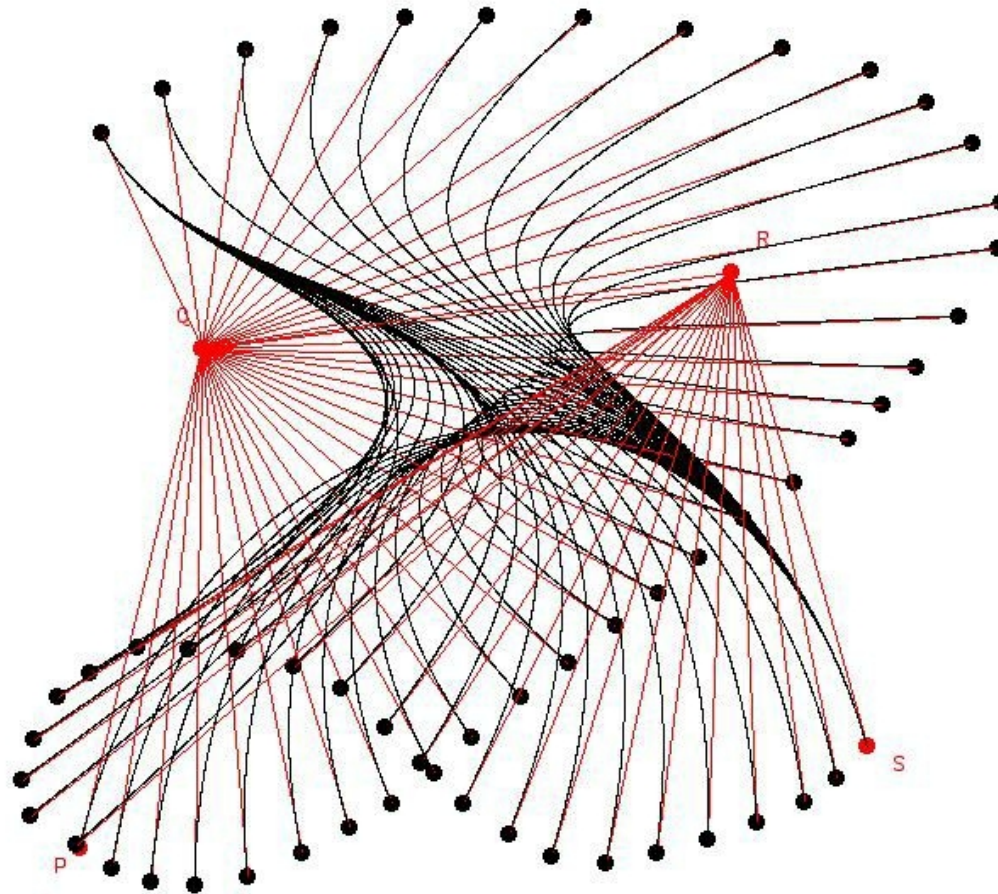


# Watkins Scan-Line Algorithm

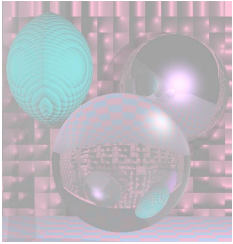




# Bezier Curves

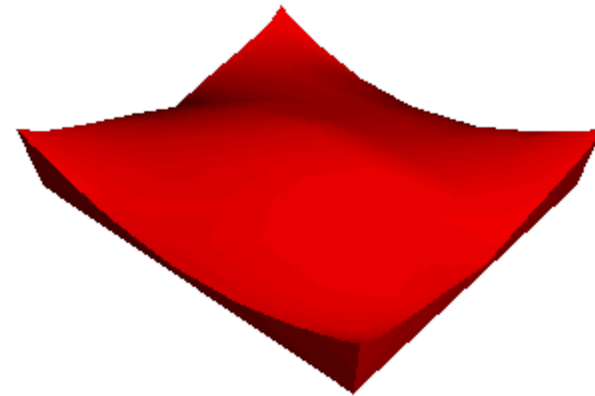
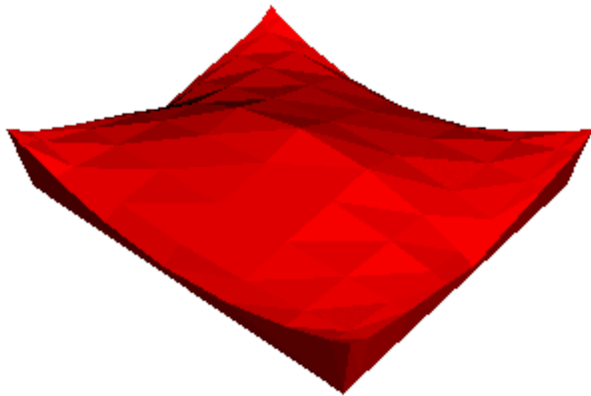




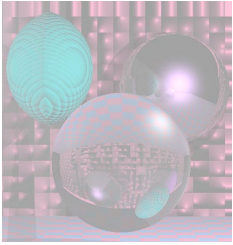


# Gouraud Shading

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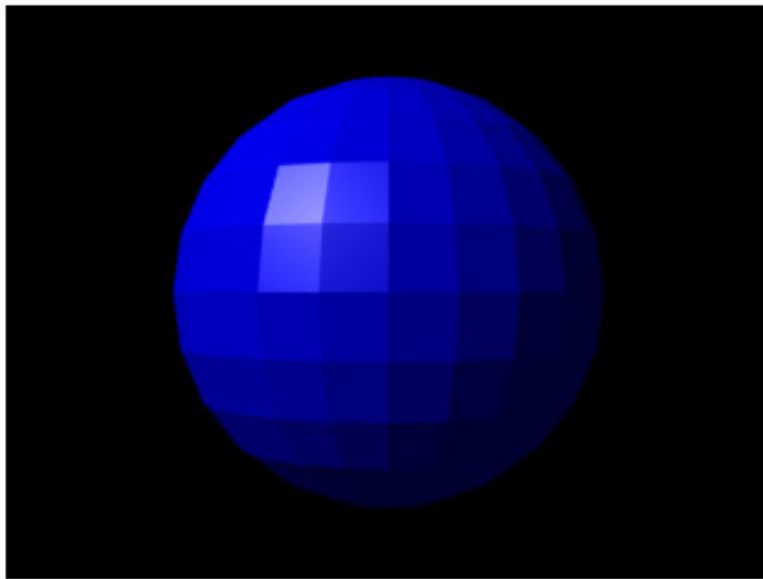


[http://freespace.virgin.net/hugo.elias/graphics/x\\_polygo.htm](http://freespace.virgin.net/hugo.elias/graphics/x_polygo.htm)

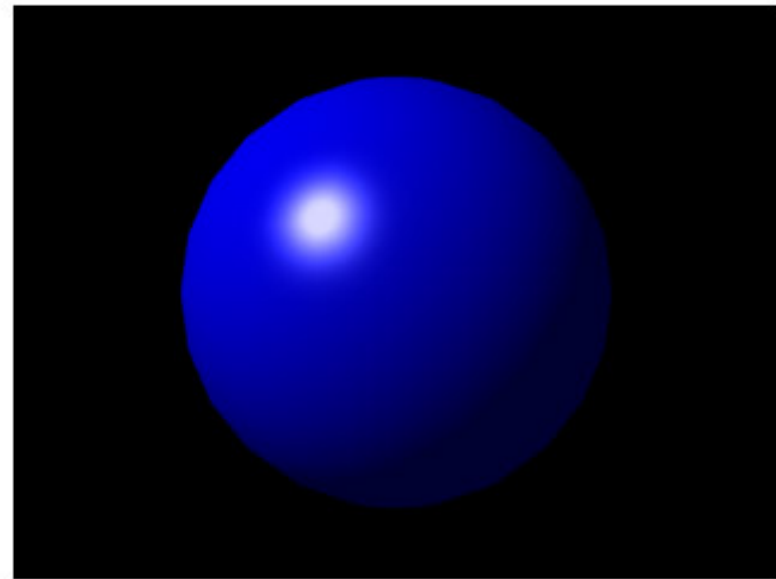


# Phong Shading

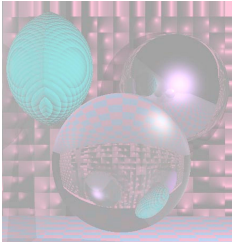
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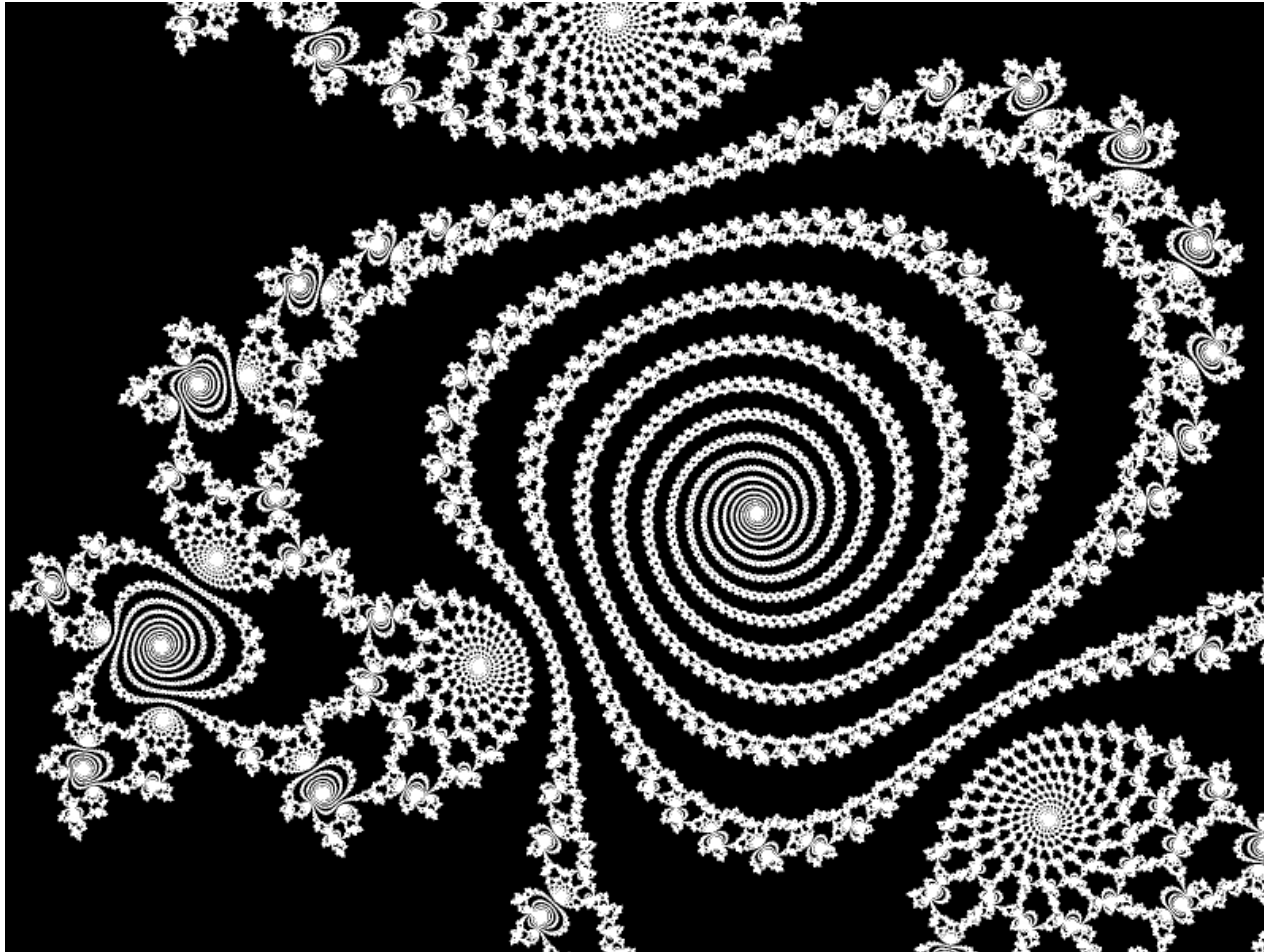
FLAT SHADING

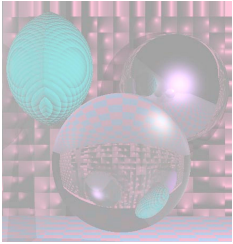


PHONG SHADING



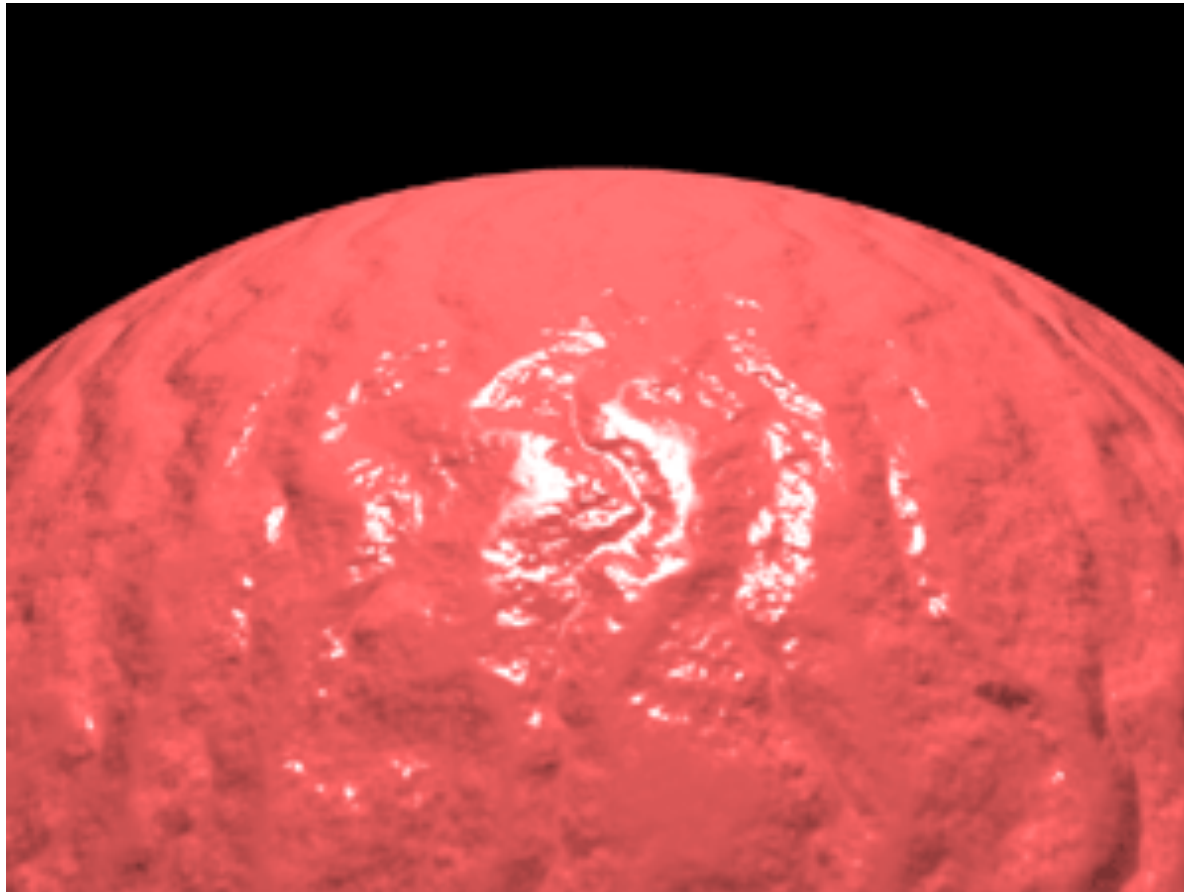
# Fractals



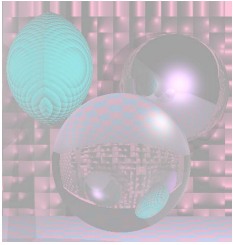


# Bump Map

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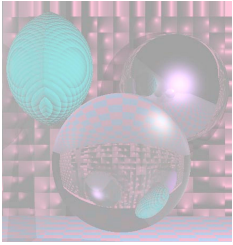
## Bump Maps in PovRay



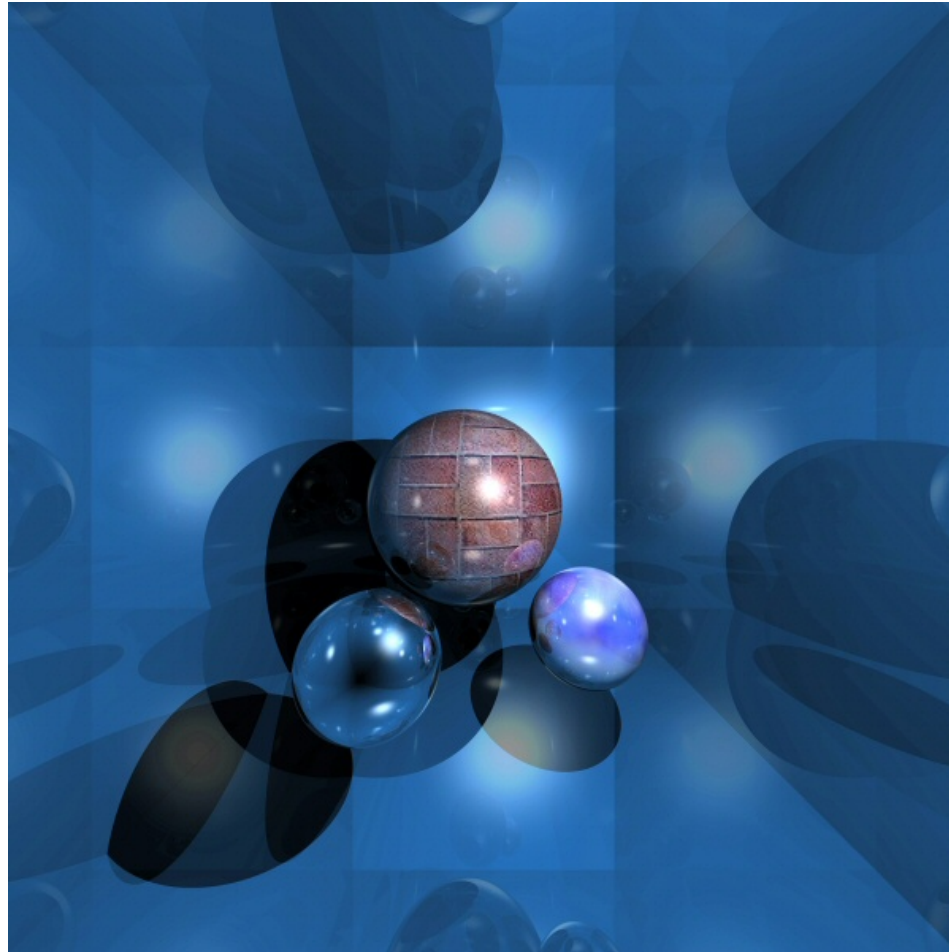
# History - the 80s

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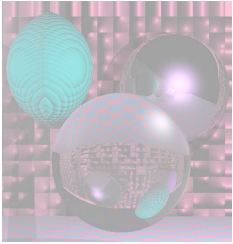
- **1980s Cheaper machines, memory - quest for realism**
- 1980 [Ray Tracing](#), Turner Whitted, Bell Labs
- 1981 IBM introduces the first IBM PC (16 bit 8088 chip)
- 1982 Data Glove, Atari
- 1984 [Macintosh](#) computer
  - introduced with Clio award winning commercial during Super Bowl
- 1985 [Perlin Noise](#)
- 1986 GIF format (CompuServe)
- 1988 [Who Framed Roger Rabbit](#) live action & animation



# Whitted Ray-Tracing

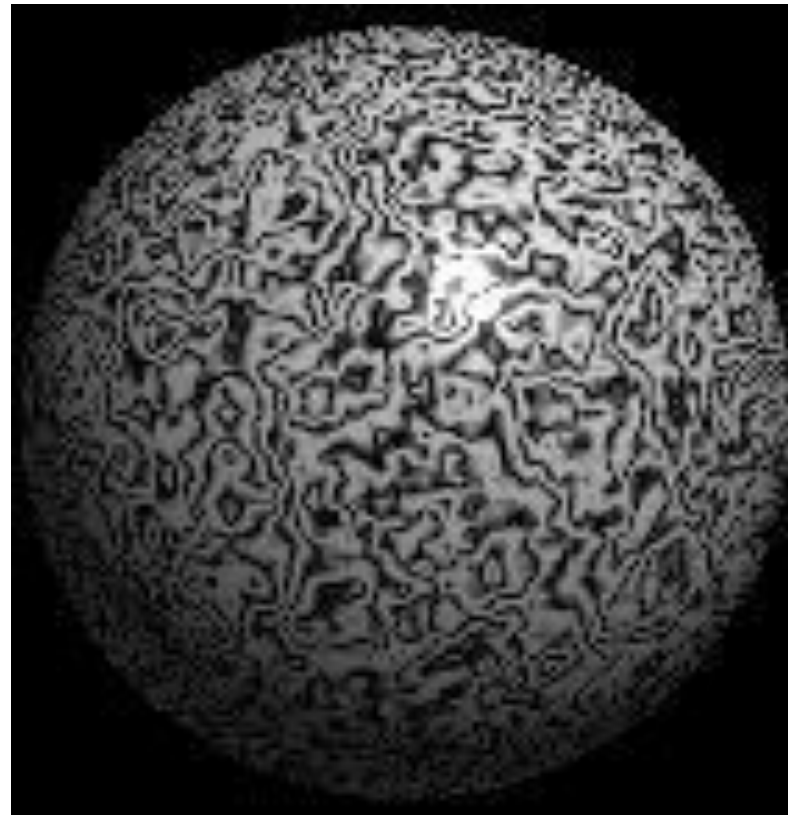
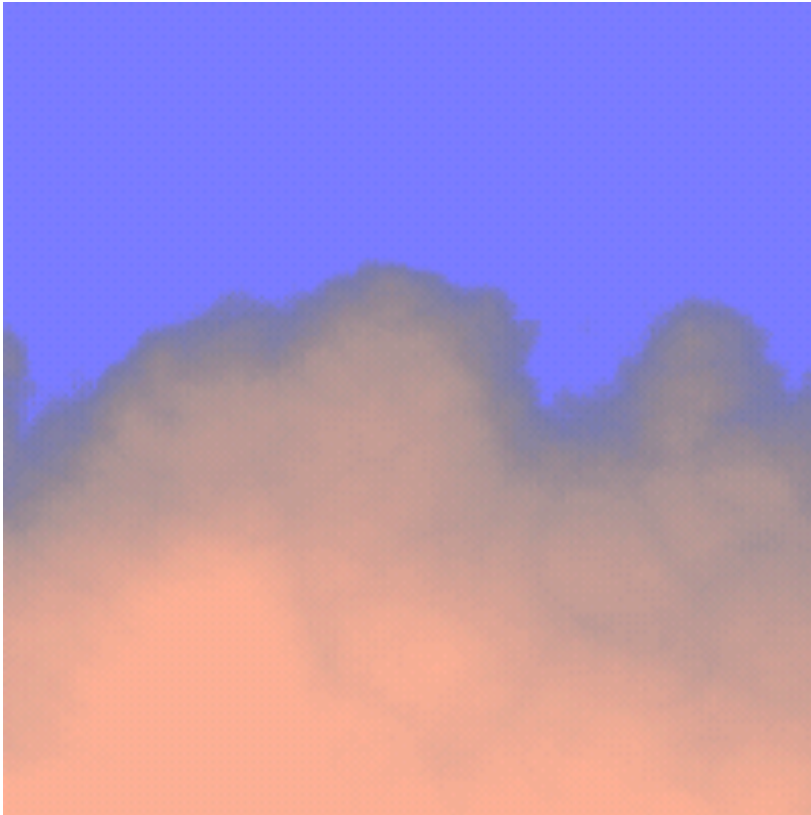


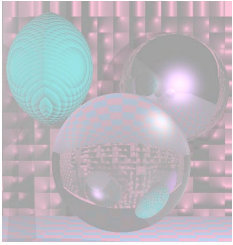
[http://en.wikipedia.org/wiki/Ray\\_tracing](http://en.wikipedia.org/wiki/Ray_tracing)



# Perlin Noise

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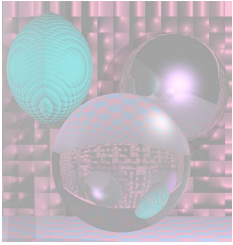


# Who Framed Roger Rabbit

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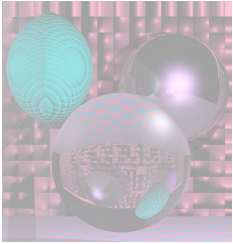




# History- the 90s

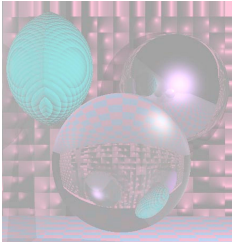
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- **1990s Visualization, Multimedia, the Net**
- 1991 JPEG/MPEG
- 1993 Myst, Cyan
- 1994 U.S. Patent to Pixar
  - for creating, manipulating and displaying images
- 1995 Toy Story, Pixar
- 1995 Internet 2 unveiled
- 1997 DVD technology unveiled
- 1998 XML standard
- 1999 deaths



# Myst

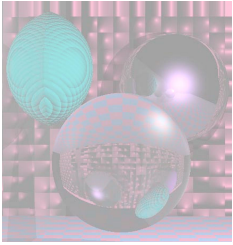




# Toy Story

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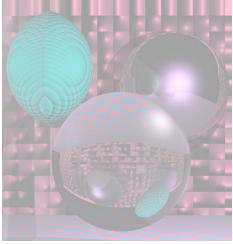




# Recent History

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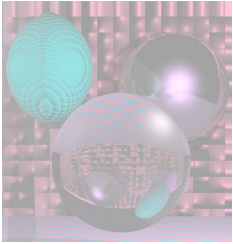
- **2000s Virtual Reality, Animation Reality**
- 2001 Significant Movies
  - Final Fantasy, Square)
  - Monsters Inc, Pixar
  - Harry Potter, A.I., Lord of the Rings, Shrek, PDI
  - The Mummy, ILM
  - Tomb Raider, Cinesite
  - Jurassic Park III, Pearl Harbor, ILM
  - Planet of the Apes, Asylum
- 2001 Microsoft xBox and Nintendo Gamecube
- 2001, 2002, 2003 [Lord of the Rings](#)
  - [Gollum](#)



# from Lord of the Rings

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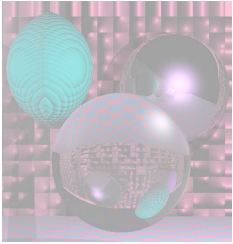
- **Motion Capture Technology**
  - Andy Serkis "played" Gollum by providing his voice and movements on set, as well as performing within a motion capture suit.
- **SKIN**
  - Christopher Hery, Ken McGaugh and Joe Letteri received a 2003 Academy Award, Scientific or Technical for implementing the BSSRDF (Bidirectional Surface Scattering Reflection Distribution Function) technique used for Gollum's skin in a production environment. Henrik Wann Jensen, Stephen Robert Marschner, and Pat Hanrahan, who developed BSSRDF, won another the same year.
- **MASSIVE**
  - a computer program developed by WETA to create automatic battle sequences rather than individually animate every soldier. Stephen Regelous developed the system in 1996, originally to create crowd scenes in *King Kong*.



# Time for a Break

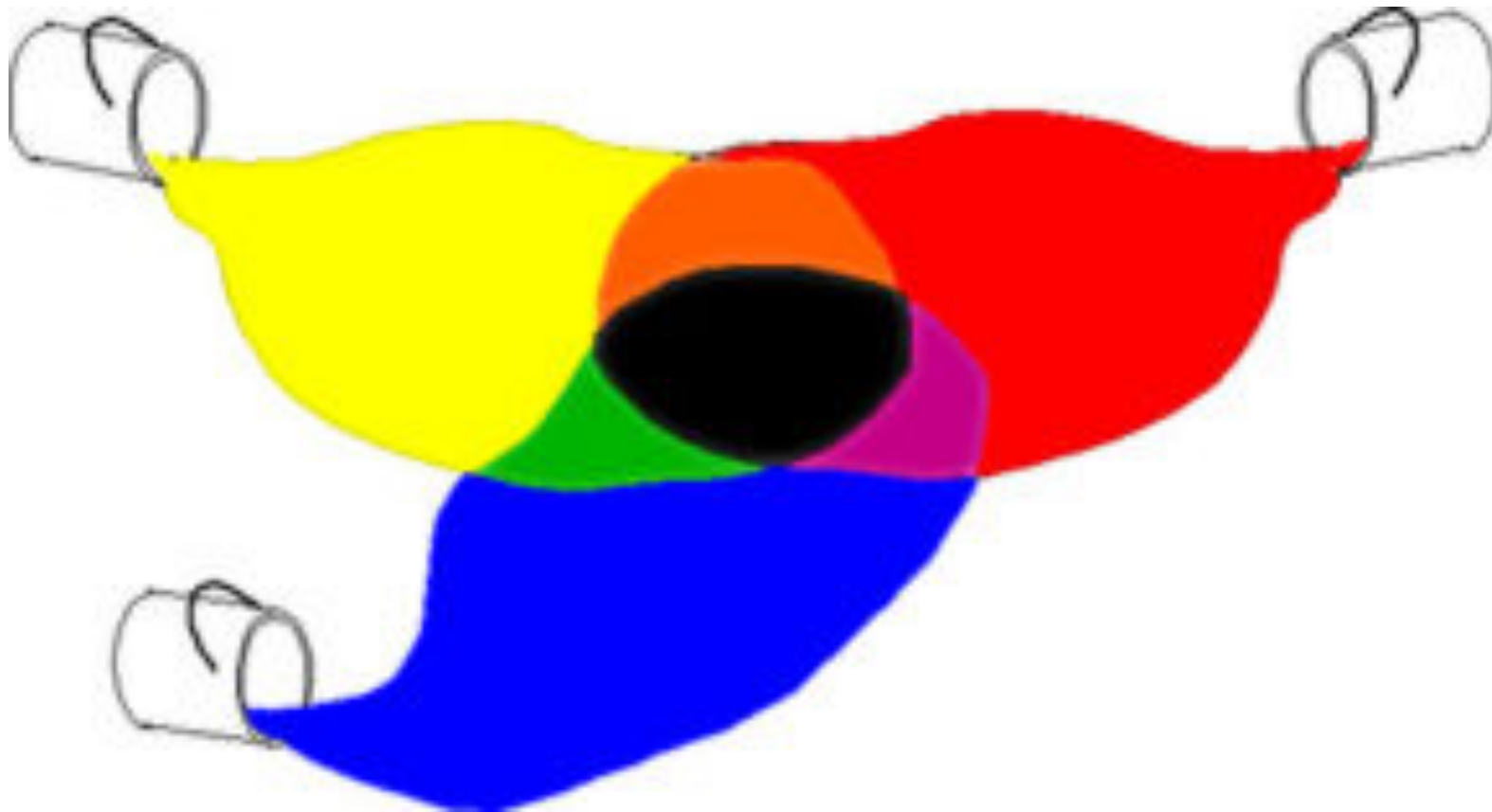
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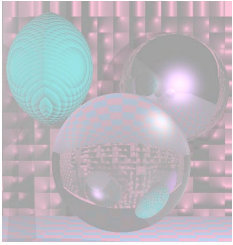


# Color

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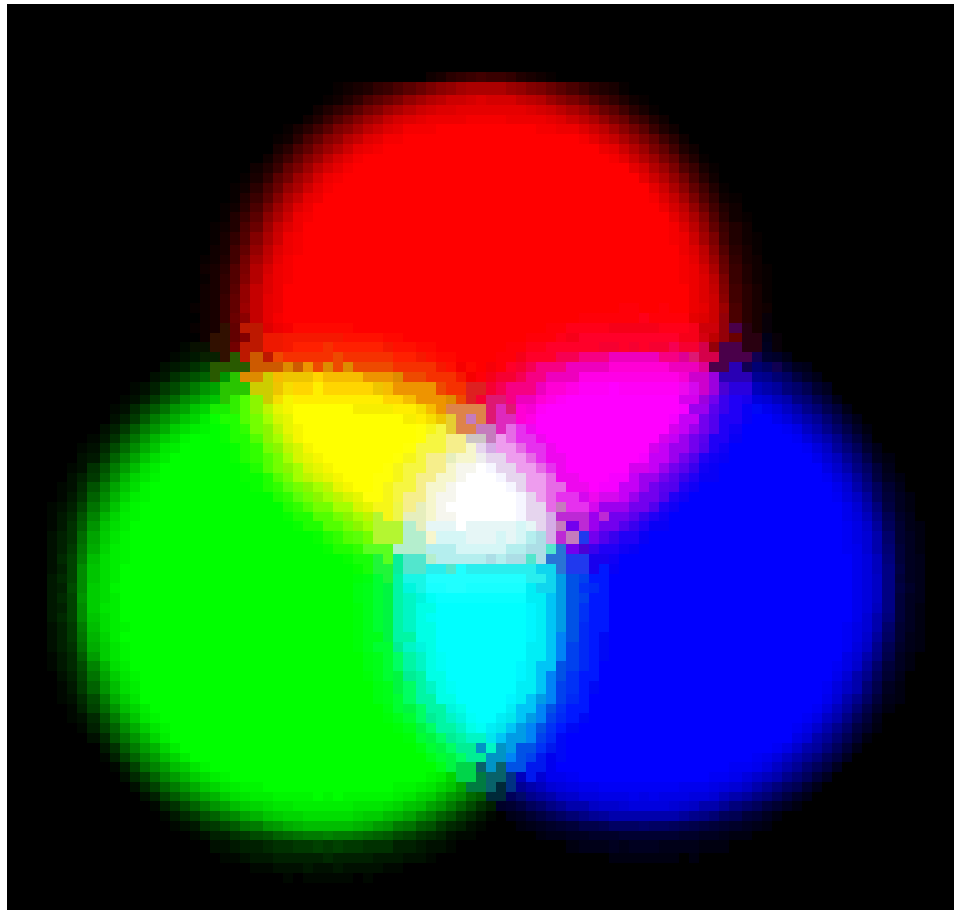


[www.thestagecrew.com](http://www.thestagecrew.com)

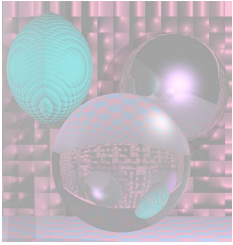


# Red, Green, and Blue Light

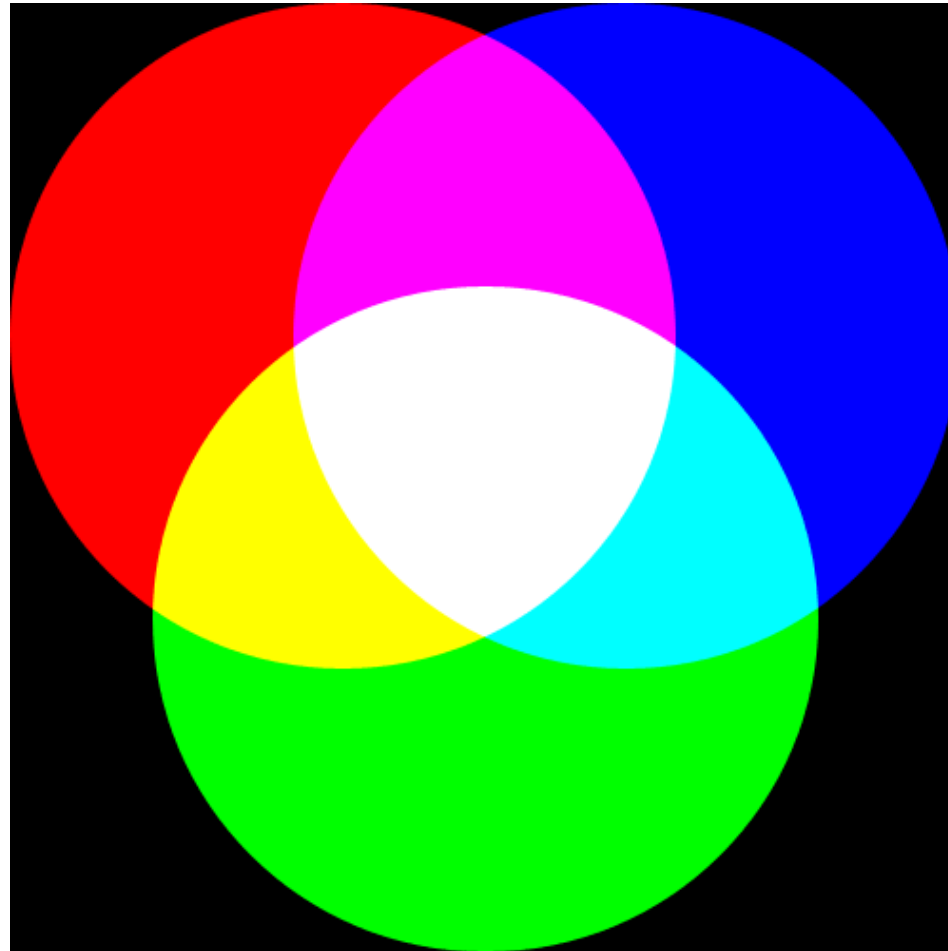
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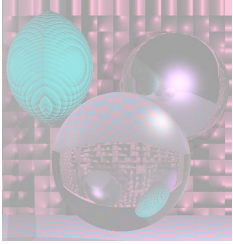




# Adding R, G, and B Values



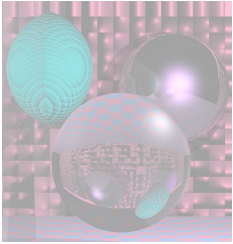
<http://en.wikipedia.org/wiki/RGB>



# From the Hubble

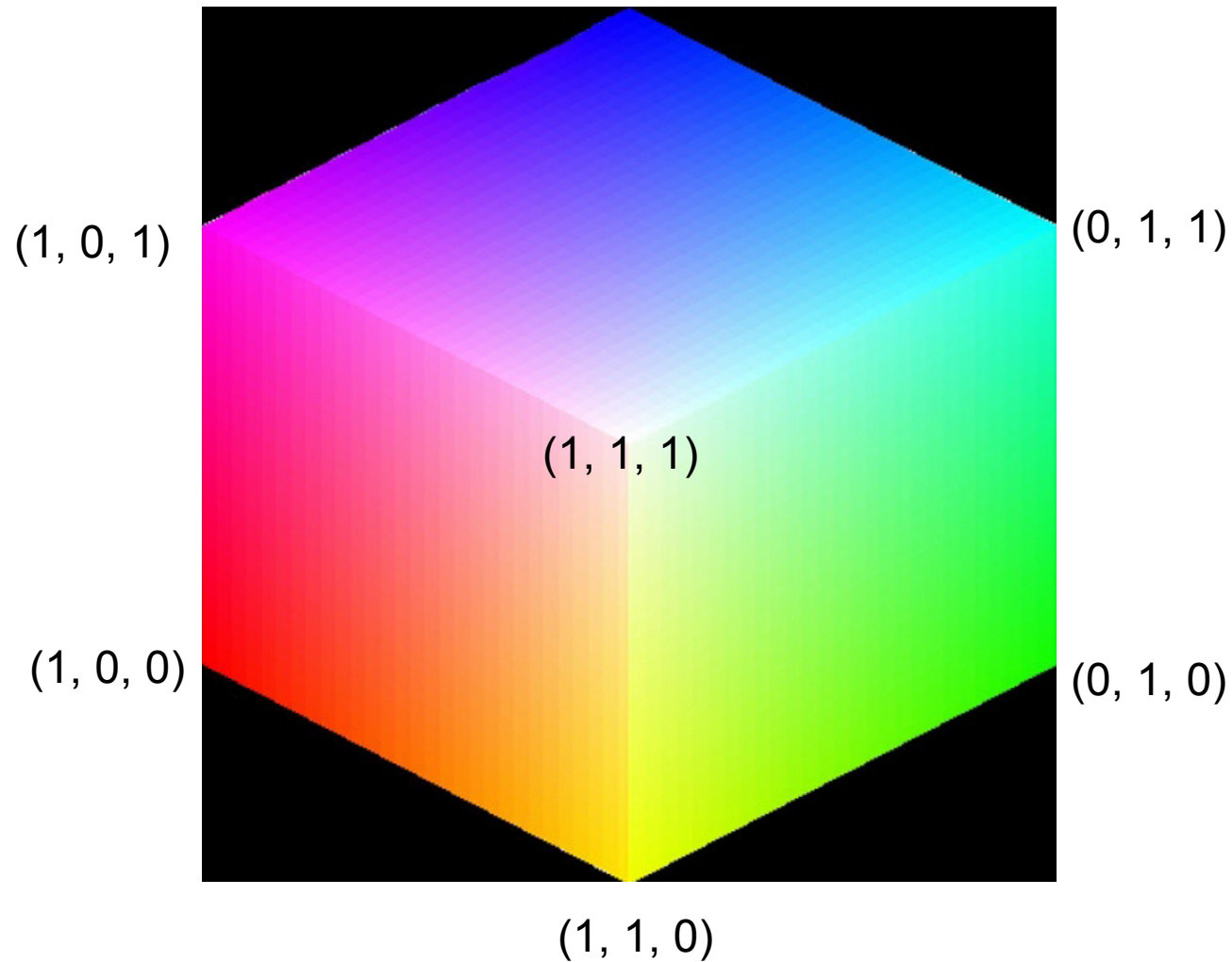
[Hubble Site Link](#)

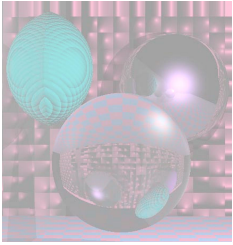




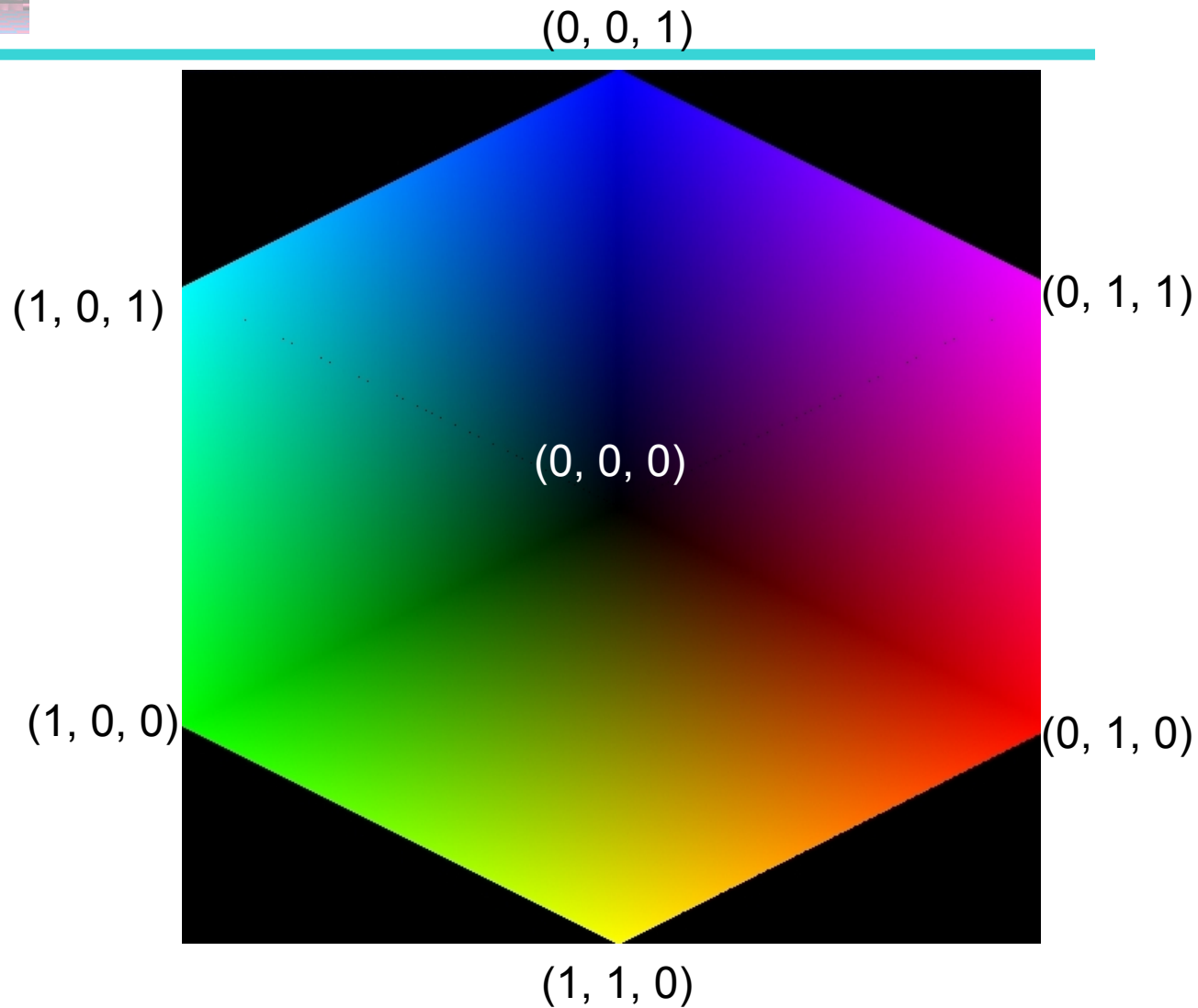
# RGB Color Cube

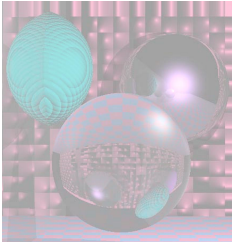
$(0, 0, 1)$





# RGB Color Cube The Dark Side





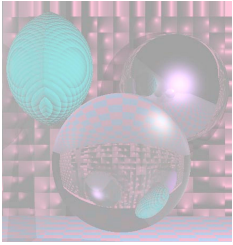
# Doug Jacobson's RGB Hex Triplet Color Chart

**RGB Hex Triplet Color Chart**  
*E-mail-ware...What a concept!*

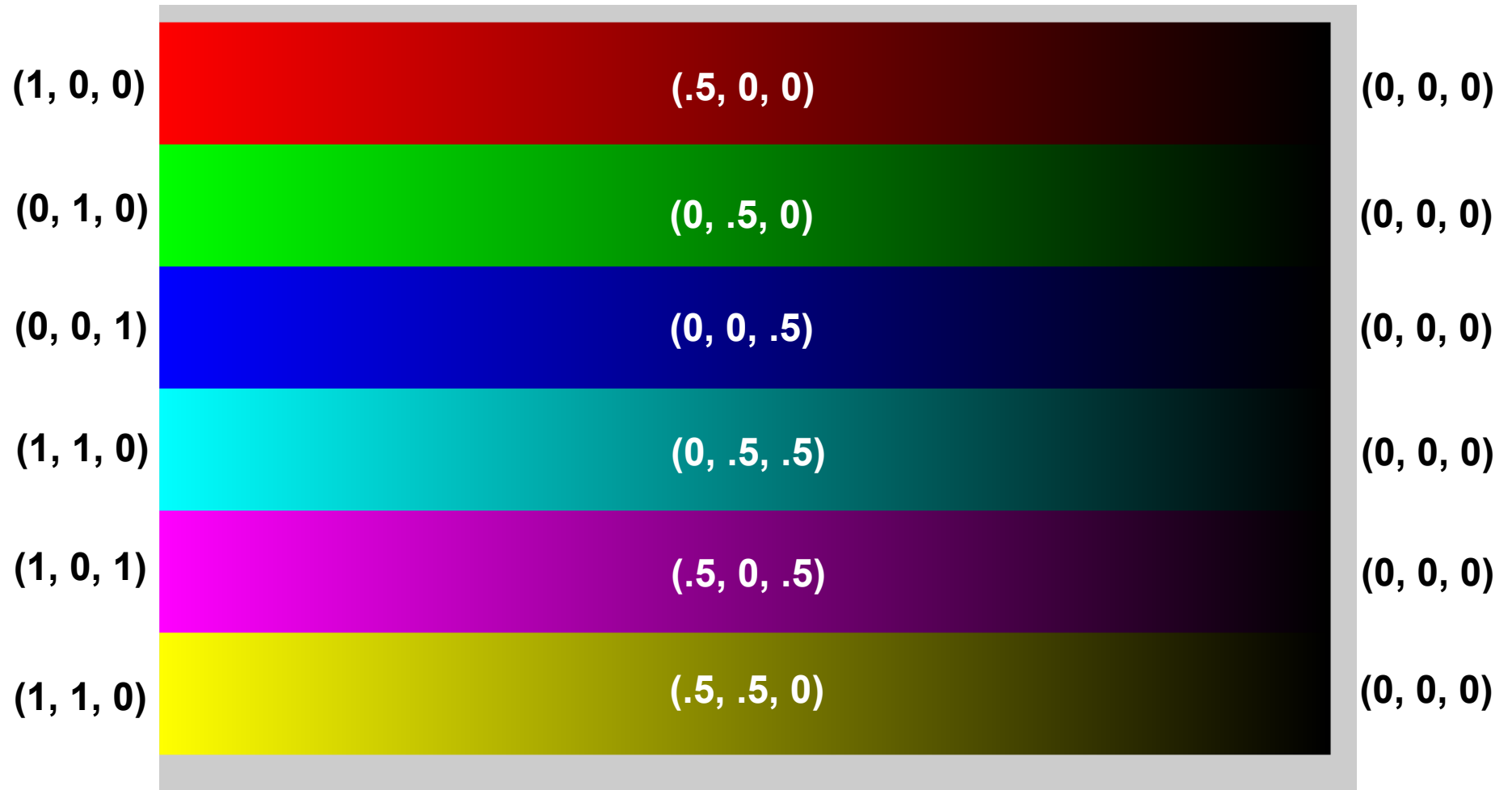
*If you find this chart helpful, send mail to Doug and say "Thanks!".  
 jacobson@phoenix.net*

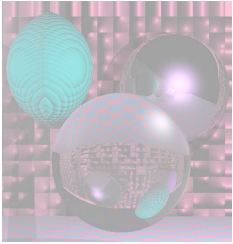
	FFFFFF	FFCCFF	FF99FF	FF66FF	FF33FF	FF00FF	
EEEEEE	FFFFCC	FFCCCC	FF99CC	FF66CC	FF33CC	FF00CC	
DDDDDD	FFFF99	FFCC99	FF9999	FF6699	FF3399	FF0099	
CCCCCC	FFFF66	FFCC66	FF9966	FF6666	FF3366	FF0066	00FF00
BBBBBB	FFFF33	FFCC33	FF9933	FF6633	FF3333	FF0033	00EE00
AAAAAA	FFFF00	FFCC00	FF9900	FF6600	FF3300	FF0000	00DD00
999999	CCFFFF	CCCCFF	CC99FF	CC66FF	CC33FF	CC00FF	00CC00
888888	CCFFCC	CCFFCC	CC99CC	CC66CC	CC33CC	CC00CC	00BB00
777777	CCFF99	CCFF99	CC9999	CC6699	CC3399	CC0099	00AA00
666666	CCFF66	CCFF66	CC9966	CC6666	CC3366	CC0066	009900
555555	CCFF33	CCFF33	CC9933	CC6633	CC3333	CC0033	008800
444444	CCFF00	CCFF00	CC9900	CC6600	CC3300	CC0000	007700
333333	99FFFF	99CCFF	9999FF	9966FF	9933FF	9900FF	006600
222222	99FFCC	99CCCC	9999CC	9966CC	9933CC	9900CC	005500
111111	99FF99	99CC99	999999	996699	993399	990099	004400
000000	99FF66	99CC66	999966	996666	993366	990066	003300
FF0000	99FF33	99CC33	999933	996633	993333	990033	002200
EE0000	99FF00	99CC00	999900	996600	993300	990000	001100
DD0000	66FFFF	66CCFF	6699FF	6666FF	6633FF	6600FF	0000FF
CC0000	66FFCC	66CCCC	6699CC	6666CC	6633CC	6600CC	0000EE
BB0000	66FF99	66CC99	669999	666699	663399	660099	0000DD
AA0000	66FF66	66CC66	669966	666666	663366	660066	0000CC
990000	66FF33	66CC33	669933	666633	663333	660033	0000BB
880000	66FF00	66CC00	669900	666600	663300	660000	0000AA
770000	33FFFF	33CCFF	3399FF	3366FF	3333FF	3300FF	000099
660000	33FFCC	33CCCC	3399CC	3366CC	3333CC	3300CC	000088
550000	33FF99	33CC99	339999	336699	333399	330099	000077
440000	33FF66	33CC66	339966	336666	333366	330066	000066
330000	33FF33	33CC33	339933	336633	333333	330033	000055
220000	33FF00	33CC00	339900	336600	333300	330000	000044
110000	00FFFF	00CCFF	0099FF	0066FF	0033FF	0000FF	000033
	00FFCC	00CCCC	0099CC	0066CC	0033CC	0000CC	000022
	00FF99	00CC99	009999	006699	003399	000099	000011
	00FF66	00CC66	009966	006666	003366	000066	
	00FF33	00CC33	009933	006633	003333	000033	
	00FF00	00CC00	009900	006600	003300	000000	

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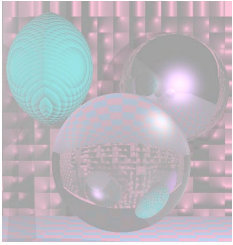
# Making Colors Darker





# Getting Darker, Left to Right

```
for (int b = 255; b >= 0; b--){  
    c = new Color(b, 0, 0); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 50, 3, 150);  
    c = new Color(0, b, 0); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 200, 3, 150);  
    c = new Color(0, 0, b); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 350, 3, 150);  
    c = new Color(0, b, b); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 500, 3, 150);  
    c = new Color(b, 0, b); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 650, 3, 150);  
    c = new Color(b, b, 0); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 800, 3, 150);  
}
```

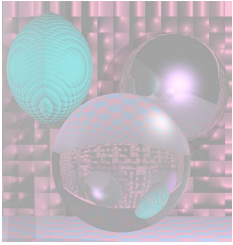


# Gamma Correction

---

- Generally, the displayed intensity is not linear in the input ( $0 \leq a \leq 1$ ).
- $\text{dispIntensity} = (\text{maxIntensity})a^\gamma$
- To find  $\gamma$ 
  - Find  $a$  that gives you .5 intensity
  - Solve  $.5 = a^\gamma$
  - $\gamma = \frac{\ln(.5)}{\ln(a)}$





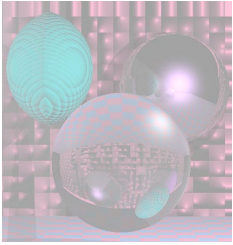
# Gamma Correction



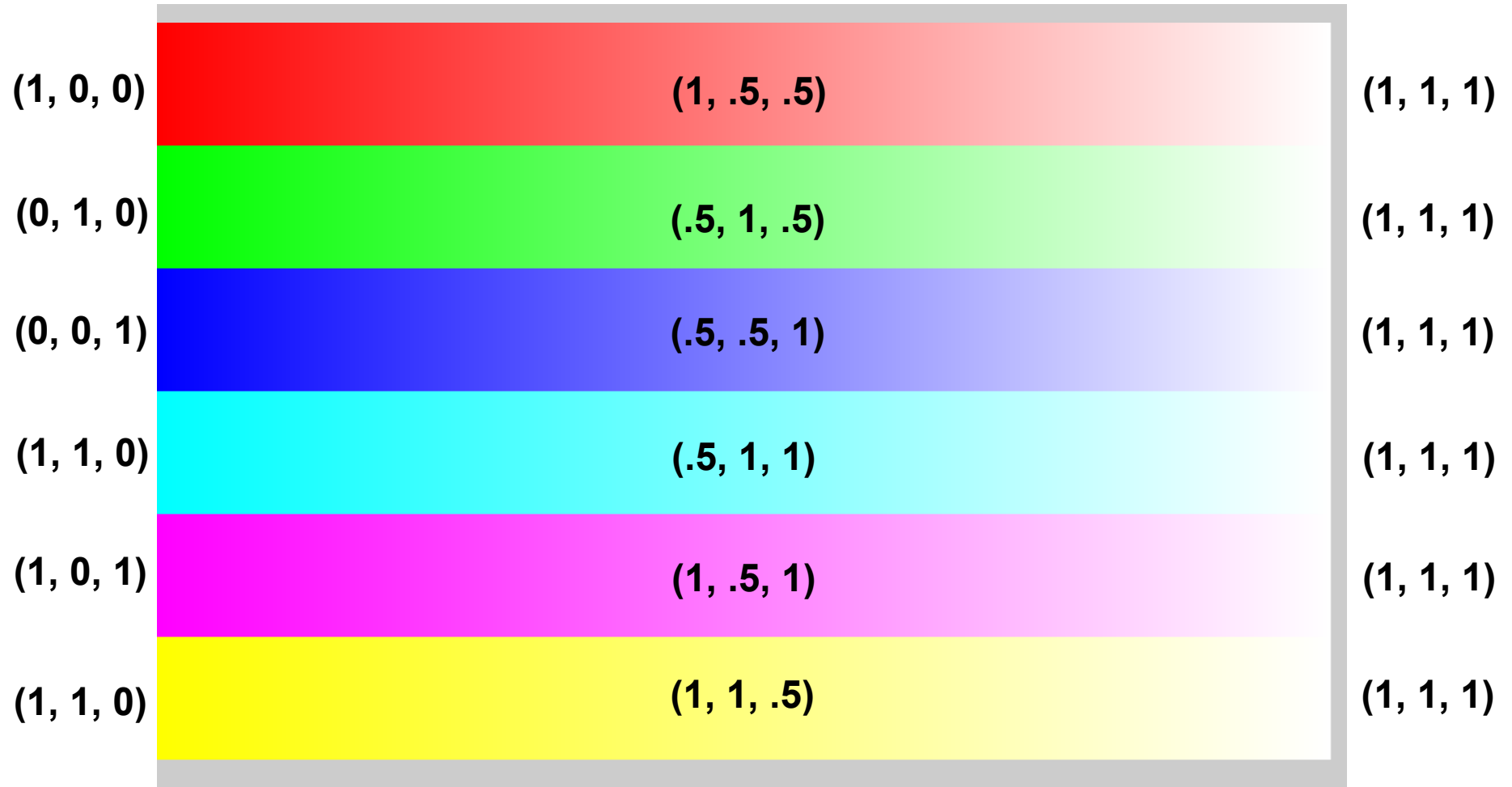
half black half red

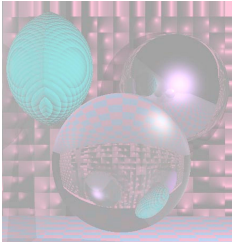
(127, 0, 0)

- Gamma



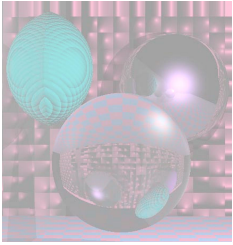
# Making Pale Colors





# Getting Paler, Left to Right

```
for (int w = 0; w < 256; w++){  
    c = new Color(255, w, w); g.setPaint(c);  
    g.fillRect(3*w, 50, 3, 150);  
    c = new Color(w, 255, w); g.setPaint(c);  
    g.fillRect(3*w, 200, 3, 150);  
    c = new Color(w, w, 255); g.setPaint(c);  
    g.fillRect(3*w, 350, 3, 150);  
    c = new Color(w, 255, 255); g.setPaint(c);  
    g.fillRect(3*w, 500, 3, 150);  
    c = new Color(255,w, 255); g.setPaint(c);  
    g.fillRect(3*w, 650, 3, 150);  
    c = new Color(255, 255, w); g.setPaint(c);  
    g.fillRect(3*w, 800, 3, 150);  
}
```

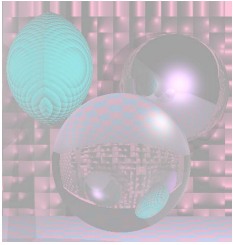


# Portable Pixmap Format (ppm)

---

A "magic number" for identifying the file type.

- A ppm file's magic number is the two characters "P3".
- Whitespace (blanks, TABs, CRs, LFs).
- A width, formatted as ASCII characters in decimal.
- Whitespace.
- A height, again in ASCII decimal.
- Whitespace.
- The maximum color value again in ASCII decimal.
- Whitespace.
- Width \* height pixels, each 3 values between 0 and maximum value.
  - start at top-left corner; proceed in normal English reading order
  - three values for each pixel for red, green, and blue, resp.
  - 0 means color is off; maximum value means color is maxxed out
  - characters from "#" to end-of-line are ignored (comments)
  - no line should be longer than 70 characters



# ppm Example

---

P3

# feep.ppm

4 4

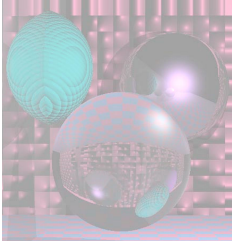
15

```
0 0 0 0 0 0 0 0 0 15 0 15
0 0 0 0 15 7 0 0 0 0 0 0
0 0 0 0 0 0 0 15 7 0 0 0
15 0 15 0 0 0 0 0 0 0 0 0
```

```

private void saveImage() {
    String outFileFileName = "my.ppm";
    File outFile = new File(outFileFileName);
    int clrR, clrG, clrB;
    try {
        PrintWriter out = new PrintWriter(new BufferedWriter(new FileWriter(outFile)));
        out.println("P3");
        out.print(Integer.toString(xmax-xmin+1)); System.out.println(xmax-xmin+1);
        out.print(" ");
        out.println(Integer.toString(ymax-ymin+1)); System.out.println(ymax-ymin+1);
        out.println("255");
        for (int y = ymin; y <= ymax; y++){
            for (int x = xmin; x <= xmax; x++) {
                // compute clrR, clrG, clrB
                out.print(" "); out.print(clrR);
                out.print(" "); out.print(clrG);
                out.print(" "); out.println(clrB);
            }
        }
        out.close();
    } catch (IOException e) {
        System.out.println(e.toString());
    }
}

```

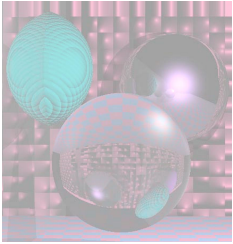


# Math Basics

---

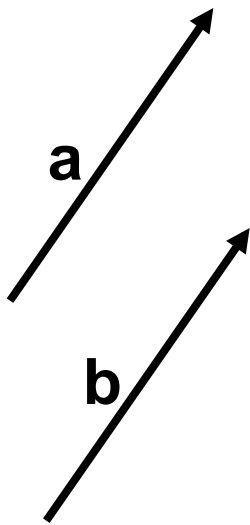
(All Readings from Shirley)

- Sets and Mappings – 2.1
- Quadratic Equations – 2.2
- Trigonometry – 2.3
- Vectors – 2.4
- 2D Parametric Curves – 2.6
- 3D Parametric Curves – 2.8
- Linear Interpolation – 2.10
- Triangles – 2.11



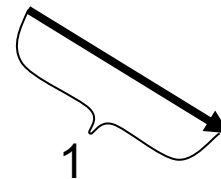
# Vectors

- A *vector* describes a length and a direction.



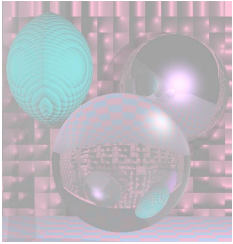
$$\mathbf{a} = \mathbf{b}$$

- a zero length vector

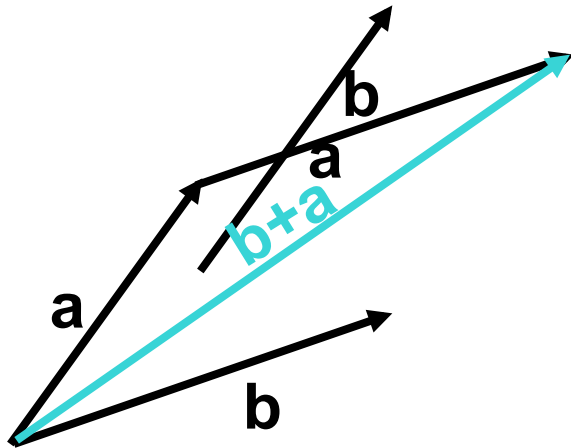


a unit vector

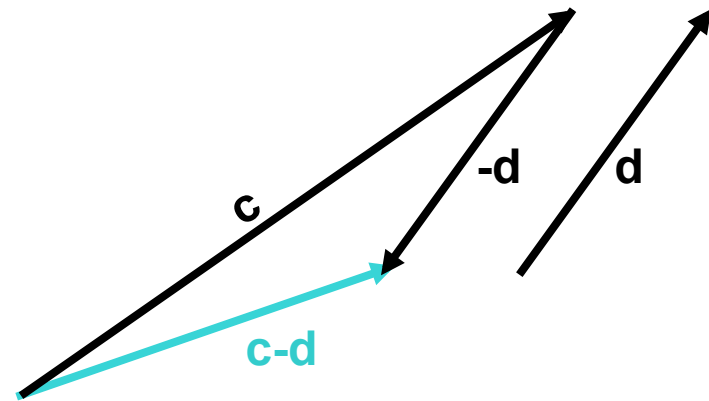




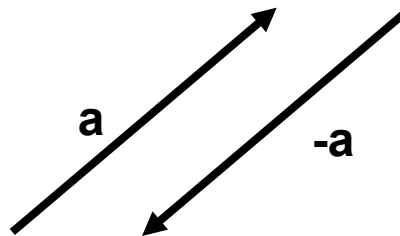
# Vector Operations

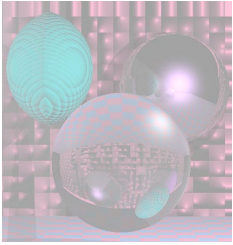


Vector Sum



Vector Difference





# Cartesian Coordinates

---

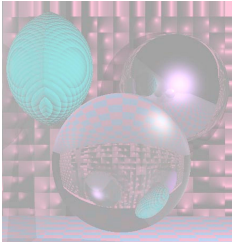
- Any two non-zero, non-parallel 2D vectors form a *2D basis*.
- Any 2D vector can be written uniquely as a linear combination of two 2D basis vectors.
- $\mathbf{x}$  and  $\mathbf{y}$  (or  $\mathbf{i}$  and  $\mathbf{j}$ ) denote unit vectors parallel to the  $x$ -axis and  $y$ -axis.
- $\mathbf{x}$  and  $\mathbf{y}$  form an *orthonormal* 2D basis.

$$\mathbf{a} = x_a \mathbf{x} + y_a \mathbf{y}$$

$$\mathbf{a} = (x_a, y_a) \quad \text{or} \quad \mathbf{a} = \begin{bmatrix} x_a \\ y_a \end{bmatrix}$$

$$\text{or } \mathbf{a} = (a_x, a_y)$$

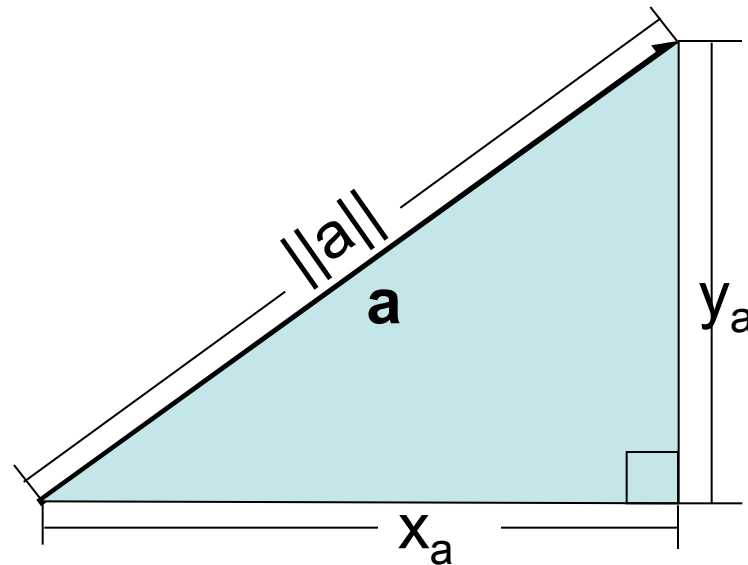
- $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$  form an *orthonormal* 3D basis.

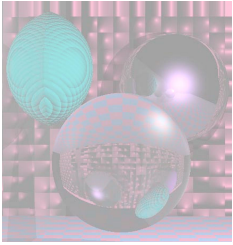


# Vector Length

Vector  $\mathbf{a} = (x_a, y_a)$

$$\text{Length}(\mathbf{a}) = \text{Norm}(\mathbf{a}) = \|\mathbf{a}\| = \sqrt{x_a^2 + y_a^2}$$





# Dot Product

## Dot Product

$$\mathbf{a} = (x_a, y_a) \quad \mathbf{b} = (x_b, y_b)$$

$$\mathbf{a} \cdot \mathbf{b} = x_a x_b + y_a y_b$$

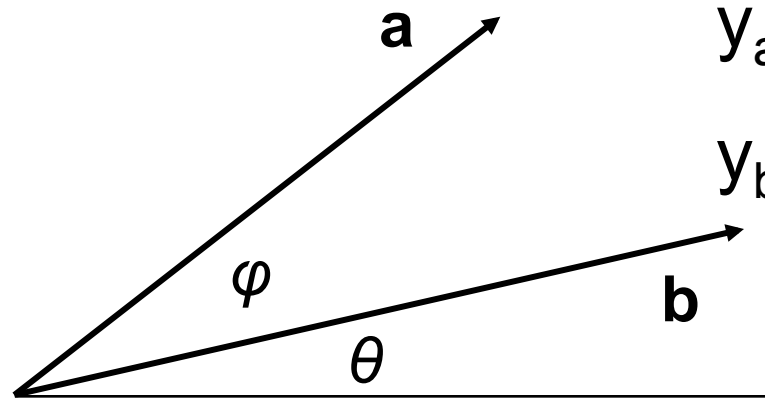
$$\mathbf{a} \cdot \mathbf{b} = \|\mathbf{a}\| \cdot \|\mathbf{b}\| \cos(\varphi)$$

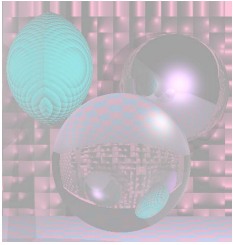
$$x_a = \|\mathbf{a}\| \cos(\theta + \varphi)$$

$$x_b = \|\mathbf{b}\| \cos(\theta)$$

$$y_a = \|\mathbf{a}\| \sin(\theta + \varphi)$$

$$y_b = \|\mathbf{b}\| \sin(\theta)$$





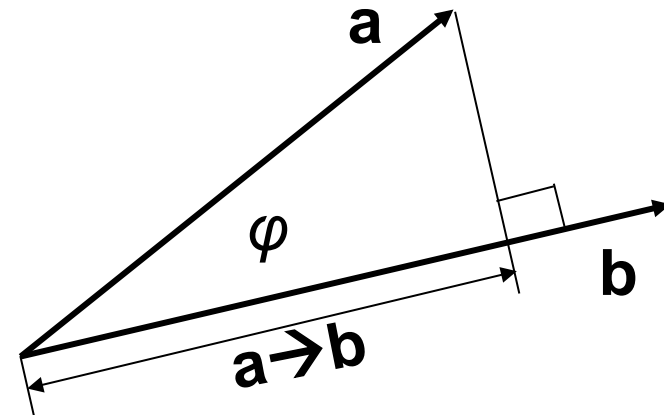
# Projection

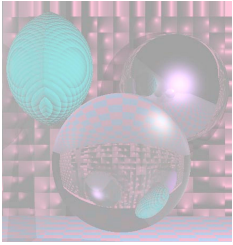
$$\mathbf{a} = (x_a, y_a) \quad \mathbf{b} = (x_b, y_b)$$

$$\mathbf{a} \cdot \mathbf{b} = \|\mathbf{a}\| \cdot \|\mathbf{b}\| \cos(\varphi)$$

The length of the projection of  $\mathbf{a}$  onto  $\mathbf{b}$  is given by

$$\mathbf{a} \rightarrow \mathbf{b} = \|\mathbf{a}\| \cos(\varphi) = \frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{b}\|}$$





# 3D Vectors

---

This all holds for 3D vectors too.

$$\mathbf{a} = (x_a, y_a, z_a)$$

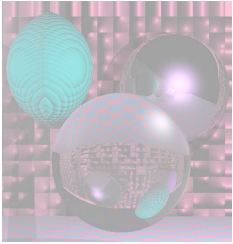
$$\mathbf{b} = (x_b, y_b, z_b)$$

$$\text{Length}(\mathbf{a}) = \text{Norm}(\mathbf{a}) = \|\mathbf{a}\| = \sqrt{x_a^2 + y_a^2 + z_a^2}$$

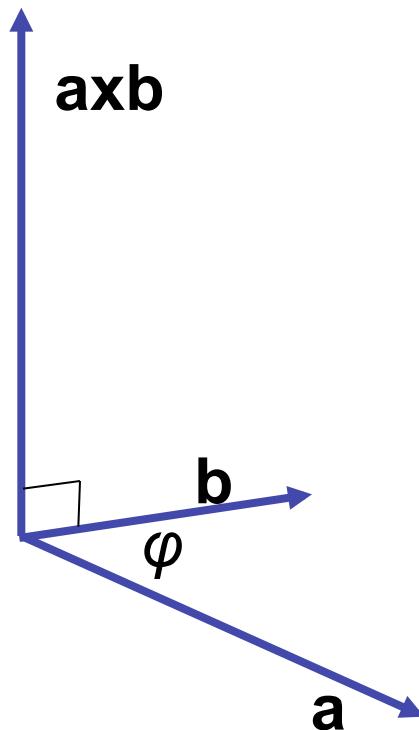
$$\mathbf{a} \cdot \mathbf{b} = x_a x_b + y_a y_b + z_a z_b$$

$$\mathbf{a} \cdot \mathbf{b} = \|\mathbf{a}\| \cdot \|\mathbf{b}\| \cos(\varphi)$$

$$\mathbf{a} \rightarrow \mathbf{b} = \|\mathbf{a}\| \cos(\varphi) = \frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{b}\|}$$



# Vector Cross Product



$$\|\mathbf{a} \times \mathbf{b}\| = \|\mathbf{a}\| \|\mathbf{b}\| \sin \varphi$$

$\mathbf{axb}$  is perpendicular to  $\mathbf{a}$  and  $\mathbf{b}$ .

Use the right hand rule to determine the direction of  $\mathbf{axb}$ .

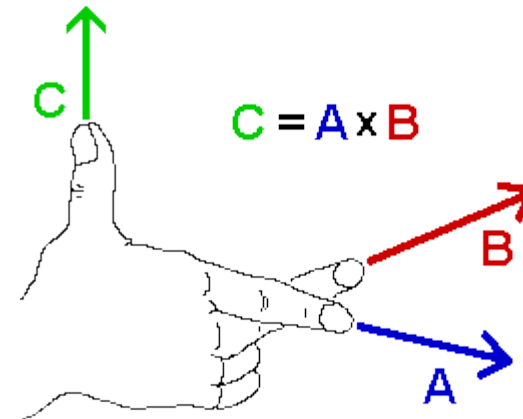
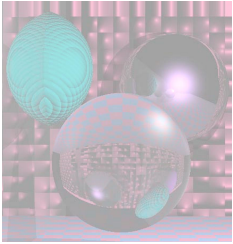
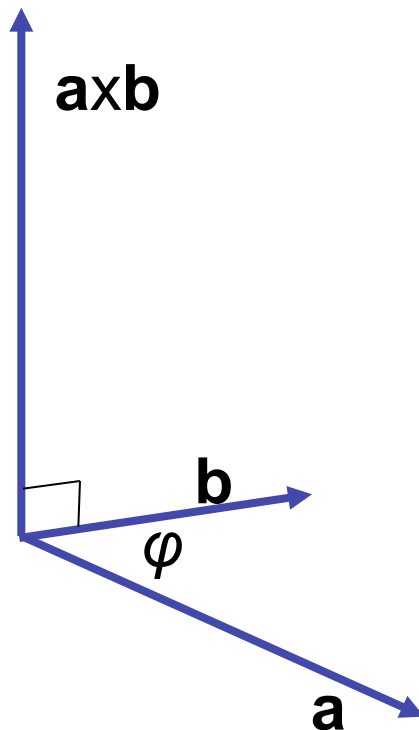


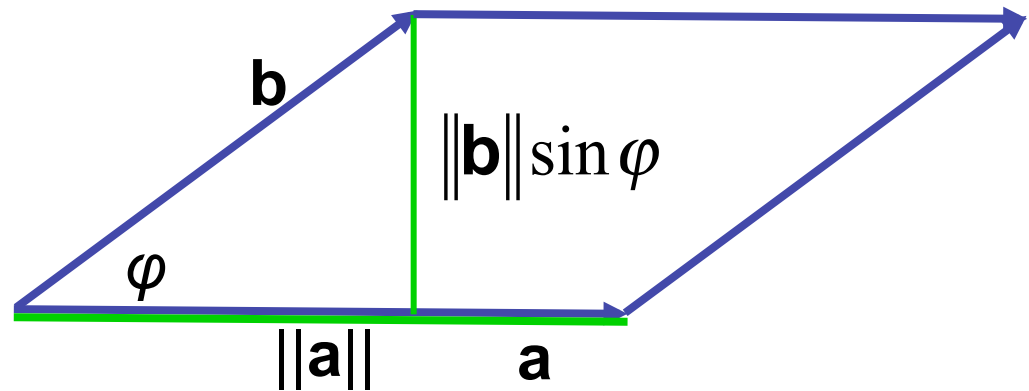
Image from [www.physics.udel.edu](http://www.physics.udel.edu)



# Cross Product and Area

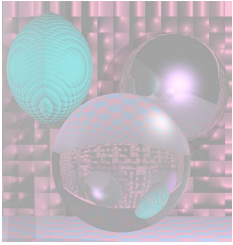


$$\|\mathbf{a} \times \mathbf{b}\| = \|\mathbf{a}\| \|\mathbf{b}\| \sin \varphi$$



$\|\mathbf{a}\| \times \|\mathbf{b}\| = \text{area of the parallelogram.}$



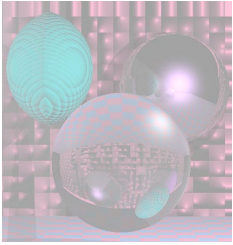


# Computing the Cross Product

---

$$\mathbf{a} \times \mathbf{b} = \begin{vmatrix} i & j & k \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

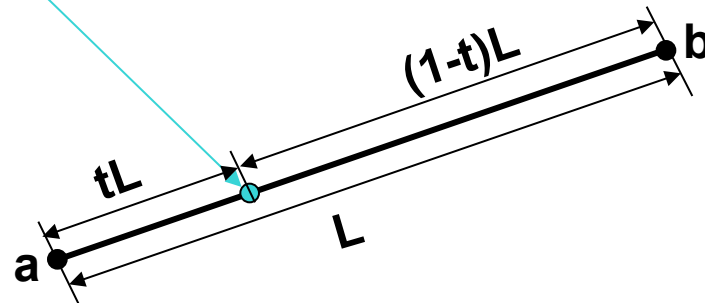
$$= (a_y b_z - a_z b_y) i + (a_z b_x - a_x b_z) j + (a_x b_y - a_y b_x) k$$

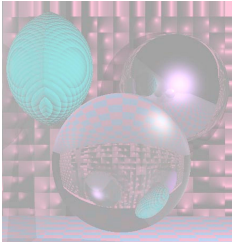


# Linear Interpolation

- **LERP**: /lerp/, vi.,n.
  - Quasi-acronym for Linear Interpolation, used as a verb or noun for the operation.
  - “Bresenham's algorithm lerps incrementally between the two endpoints of the line.”

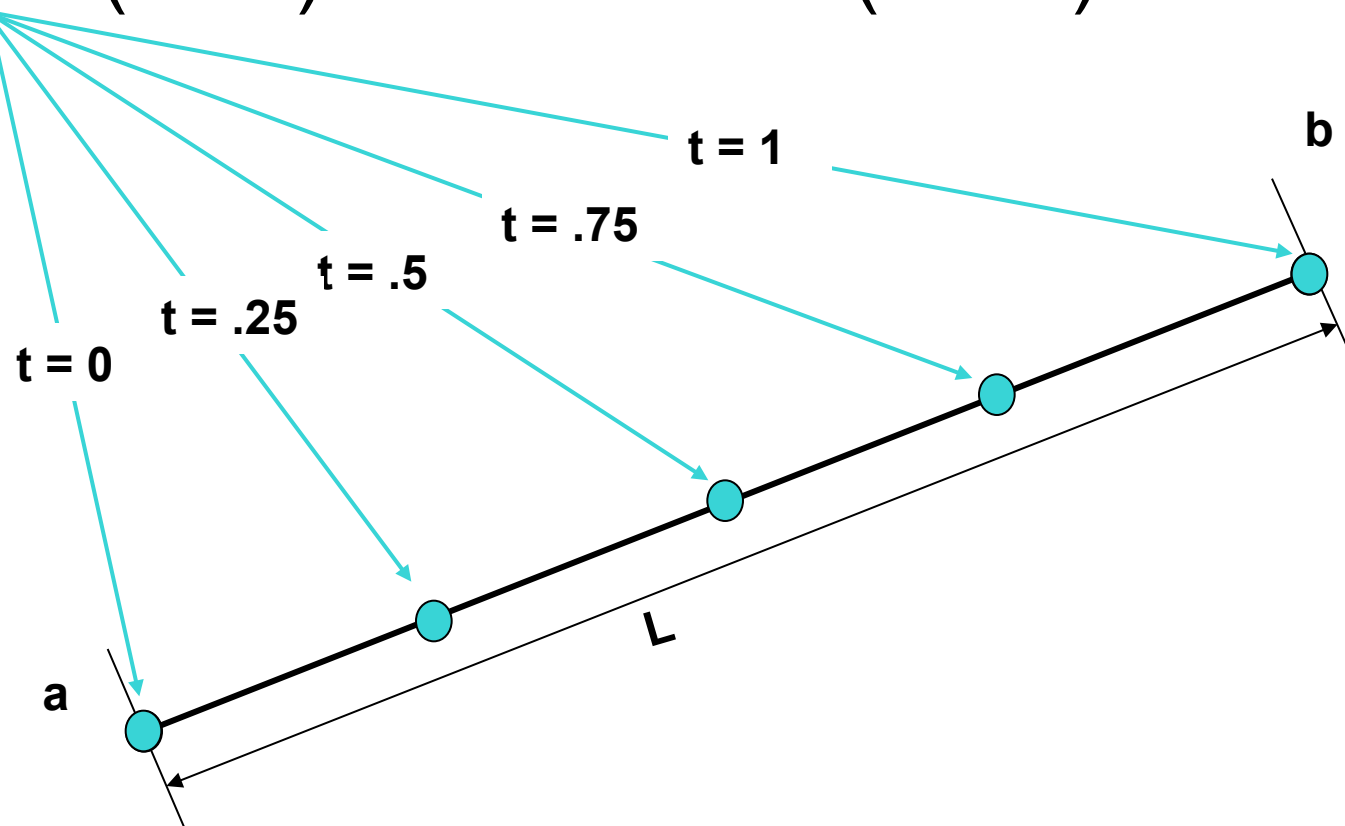
$$p = (1 - t) a + t b = a + t(b - a)$$

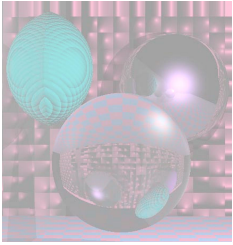




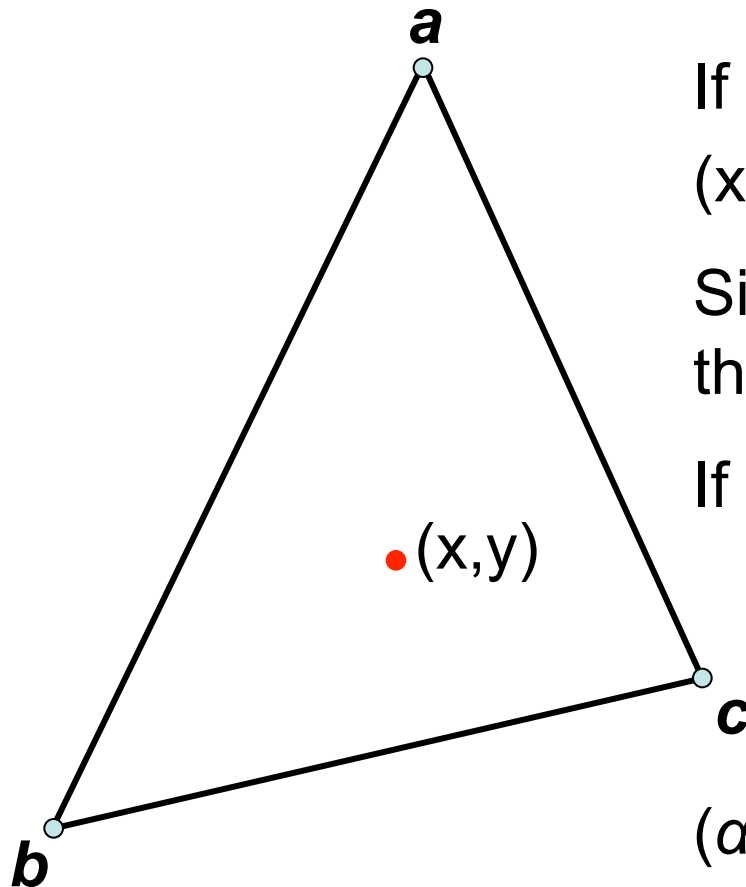
# Lerping

$$p = (1 - t) a + t b = a + t(b - a)$$





# Triangles



If  $(x, y)$  is on the edge  $ab$ ,  
 $(x, y) = (1 - t) a + t b = a + t(b - a)$ .

Similar formulas hold for points on the other edges.

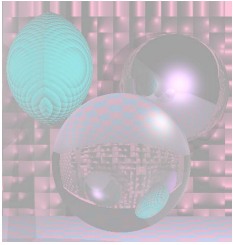
If  $(x, y)$  is in the triangle:

$$(x, y) = \alpha a + \beta b + \gamma c$$

$$\alpha + \beta + \gamma = 1$$

$(\alpha, \beta, \gamma)$  are the

*Barycentric coordinates* of  $(x, y)$ .



# Triangles

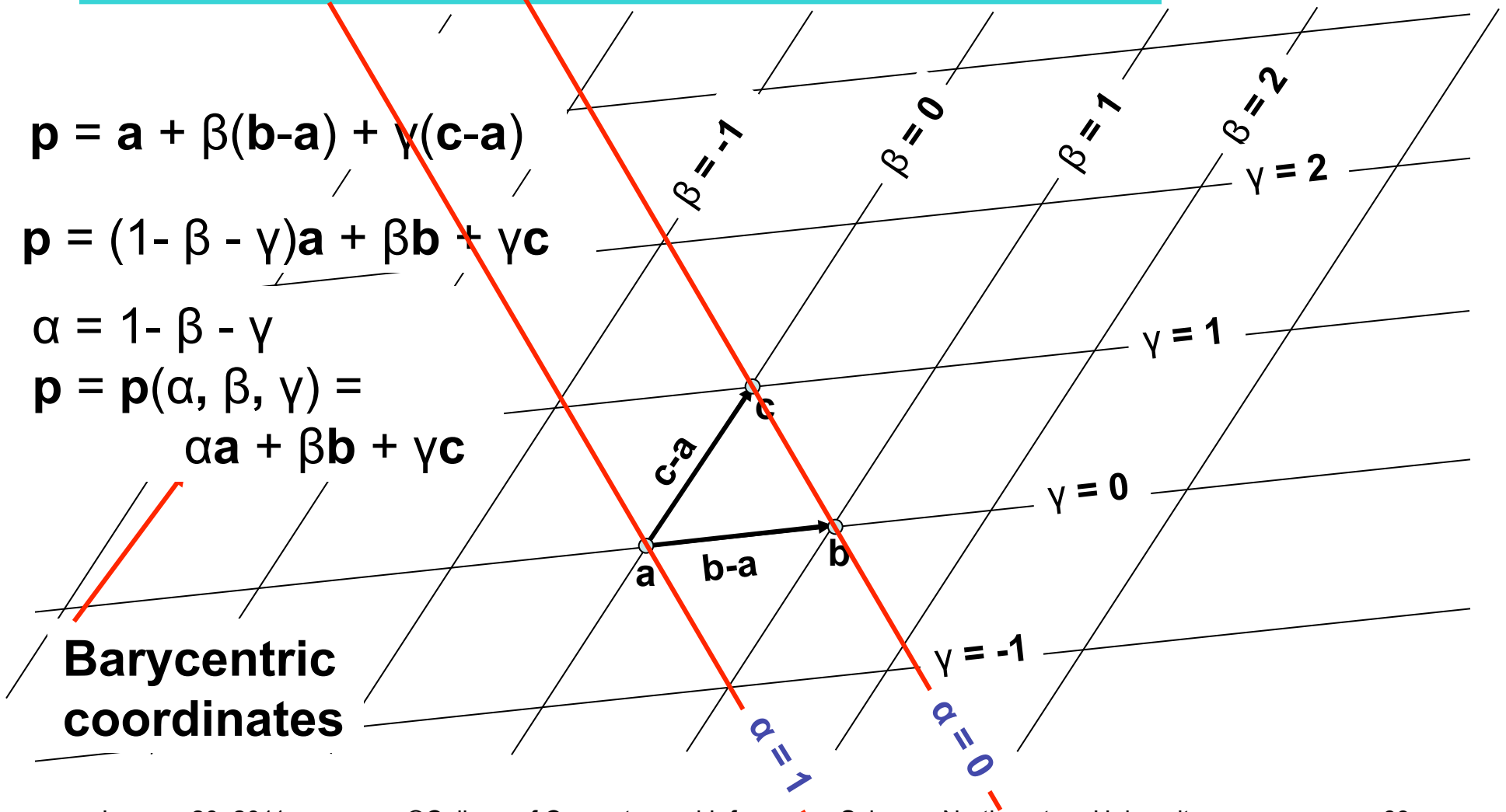
$$\mathbf{p} = \mathbf{a} + \beta(\mathbf{b}-\mathbf{a}) + \gamma(\mathbf{c}-\mathbf{a})$$

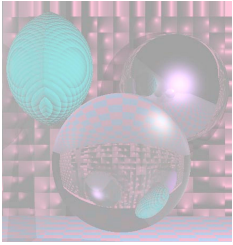
$$\mathbf{p} = (1 - \beta - \gamma)\mathbf{a} + \beta\mathbf{b} + \gamma\mathbf{c}$$

$$\alpha = 1 - \beta - \gamma$$

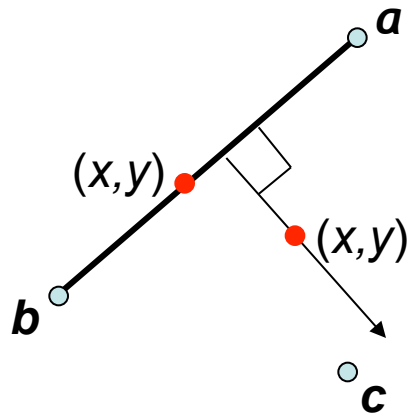
$$\mathbf{p} = \mathbf{p}(\alpha, \beta, \gamma) = \alpha\mathbf{a} + \beta\mathbf{b} + \gamma\mathbf{c}$$

**Barycentric  
coordinates**





# Computing Barycentric Coordinates

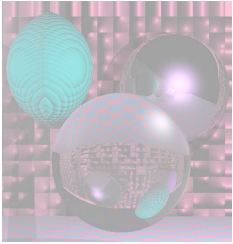


$$\frac{y - y_a}{x - x_a} = \frac{y_b - y_a}{x_b - x_a}$$

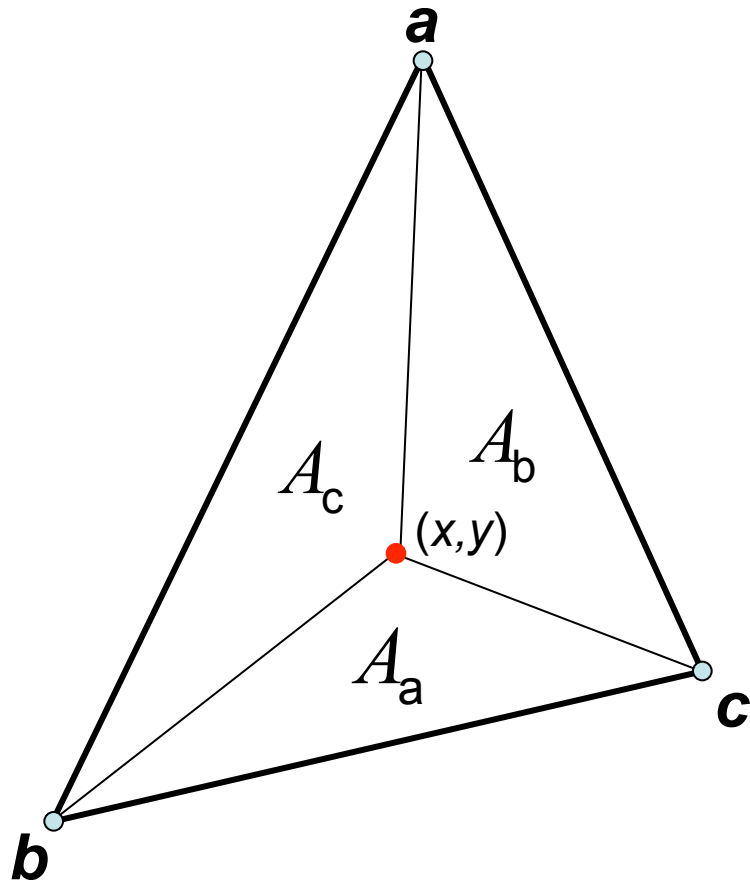
$$(y - y_a)(x_b - x_a) - (y_b - y_a)(x - x_a) = 0$$

$$f_{ab}(x, y) = (y - y_a)(x_b - x_a) - (y_b - y_a)(x - x_a)$$

$$\gamma = \frac{f_{ab}(x, y)}{f_{ab}(x_c, y_c)}$$



# Barycentric Coordinates as Areas



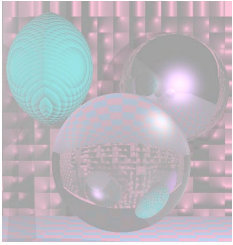
$$\alpha = A_a / A$$

$$\beta = A_b / A$$

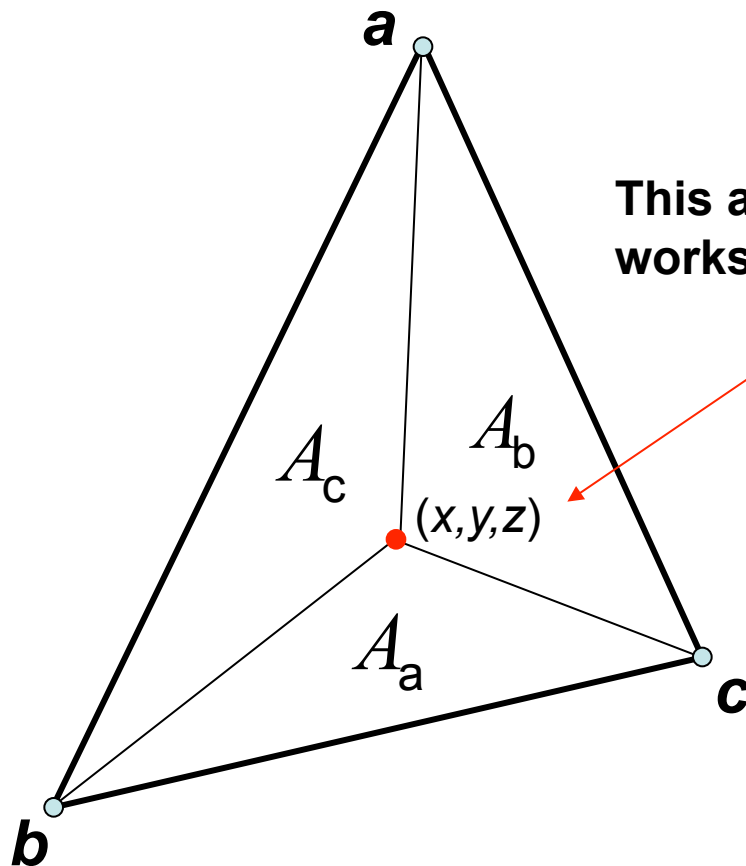
$$\gamma = A_c / A$$

where  $A$  is the area of the triangle.

$$\alpha + \beta + \gamma = 1$$



# 3D Triangles



This all still works in 3D.

$$\alpha = A_a / A$$

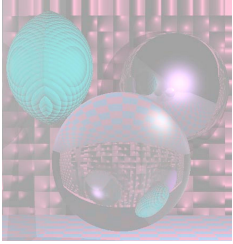
$$\beta = A_b / A$$

$$\gamma = A_c / A$$

where  $A$  is the area of the triangle.

$$\alpha + \beta + \gamma = 1$$





# Assignment 0

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- You will choose a programming platform for the quarter and familiarize yourself with RGB color and the ppm format. In part, this assignment is to ensure that you have a method of submitting your work so that I can:
  - read the code
  - compile (or interpret) the code
  - run the code to produce a file in ppm format.
- Sample Program
- You will write your own 3D vector tools (e.g. as a JAVA class) that you will use for your later programming assignments.