Localizing Grasp Affordances in 3-D Points Clouds Using Taubin Quadric Fitting Andreas ten Pas and Robert Platt

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Perception for Grasping

- Enveloping grasp affordances circled in cyan
- Enveloping grasp affordances localized by our algorithm





Enveloping Grasp Affordances as Cylindrical Shells

Affordances correspond to robot hand geometry





Evaluation Process







Ground Truth



- Enveloping Grasp Affordance (EGA) conditions
 - 1. Points that lie on the object surface must be contained within a cylinder with radius no larger than the capture radius.
 - 2. This cylinder must be contained within a cylindrical shell that is clear of points and at least as thick as the finger thickness.

Grasp Affordance Perception Pipeline

- 1. Sample neighborhoods from the point cloud.
- 2. Filter out occluded neighborhoods.
- 3. Taubin quadric fitting and curvature calculation.
- 4. Filter out neighborhoods that validate the 1st EGA condition.
- 5. Cylinder fitting to those sets that satisfy the 2nd EGA condition.

Taubin Quadric Fitting

- ► Quadric fit to a curved surface
- ► Quadric fit to a corner surface





► Implicit quadric equation:

 $f(c, x) = c_1 x_1^2 + c_2 x_2^2 + c_3 x_3^2 + c_4 x_1 x_2 + c_5 x_2 x_3 + c_6 x_1 x_3 + c_7 x_1 + c_8 x_2 + c_9 x_3 + c_{10} = 0$

Grasp Affordances

Results: Precision in Cluttered Real-World Environments

► Dataset



(a) Mugs

(b) Cleaning1

(d) Cleaning2 (c) Kitchen1

(e) Household1









(h) Kitchen3

(i) Luggage (j) Cleaning3

Precision for Taubin (blue), PCA (green), and Normals (red)



min
$$\sum_{i=1}^{n} f(c, x^i)^2 = c^T M c$$

Cylinder Fitting

Cylindrical shell Cylinder fitted to the object surface





- **Object** Surface
- Project the point neighborhood onto the plane orthogonal to the curvature axis
- ► Find the best-fit circle:

min $\sum_{x \to 1} ((\bar{x}^i - h_x)^2 + (\bar{y}^i - h_y)^2 - r^2)^2$

- Start with cylinder radius
- Iteratively increase shell radius
- ► Keep shell thickness = finger thickness
- Stop when a radius is found where few points are within the shell thickness

Results: Practical Running Time

Average runtime for Taubin, PCA, and Normals



Conclusions

- Very accurate
- ► Fast enough to be applied to real-world scenarios

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