### DS 4400

### Machine Learning and Data Mining I

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# Logistics

- HW3 is due on Friday, February 22
- Project proposal due on Tuesday 02/26
  - 1 page description of your project, including problem statement, dataset, and ML algorithms
- Week of February 25
  - Lecture on 02/26 taught by Lisa Friedland
  - Lecture on 02/28 canceled

# **Summary Decision Trees**

- Representation: decision trees
- Bias: prefer small decision trees
- Search algorithm: greedy
- Heuristic function: information gain or information content or others
- Overfitting / pruning

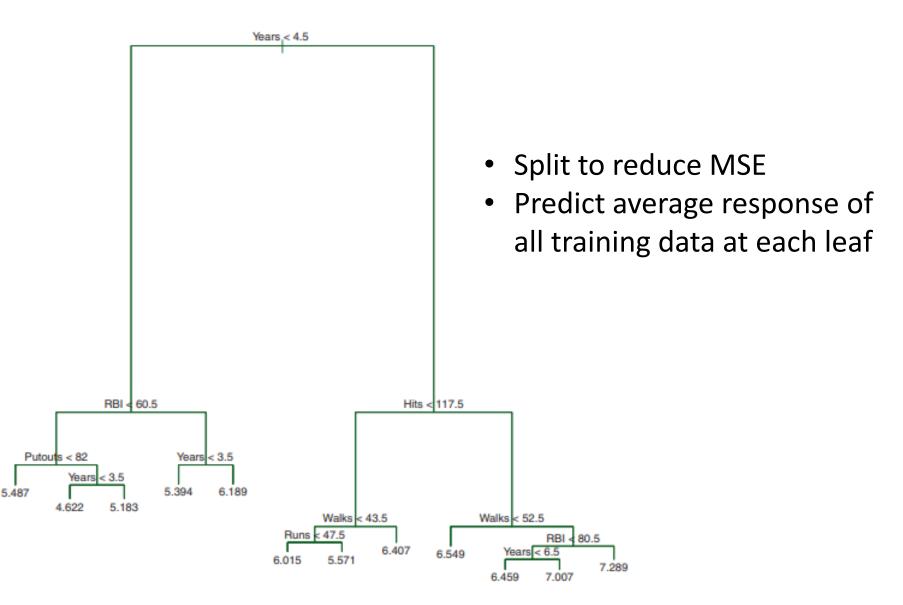
Strengths

- Fast to evaluate
- Interpretable
- Generate rules
- Supports categorical and numerical data

Weaknesses

- Overfitting
- Splitting method might not be optimal
- Accuracy is not always high
- Batch learning

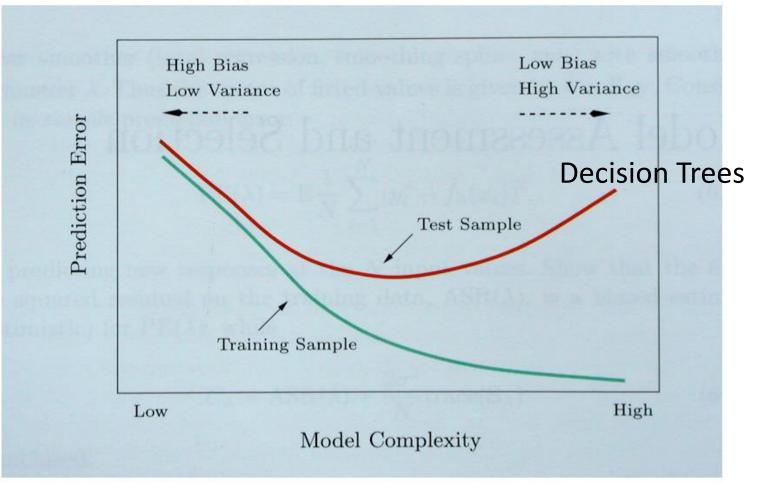
### **Regression Trees**



# Outline

- Ensemble learning
  - Combine multiple classifiers to reduce model variance and improve accuracy
- Bagging
  - Bootstrap samples
  - Random Forests
- Boosting
  - AdaBoost

### **Bias/Variance Tradeoff**



Hastie, Tibshirani, Friedman "Elements of Statistical Learning" 2001

How to reduce variance of single decision tree?

## **Ensemble Learning**

Consider a set of classifiers  $h_1$ , ...,  $h_L$ 

**Idea:** construct a classifier  $H(\mathbf{x})$  that combines the individual decisions of  $h_1, ..., h_L$ 

- e.g., could have the member classifiers vote, or
- e.g., could use different members for different regions of the instance space

Successful ensembles require diversity

- Classifiers should make different mistakes
- Can have different types of base learners

# **Build Ensemble Classifiers**

- Basic idea
  - Build different "experts", and let them vote
- Advantages
  - Improve predictive performance
  - Easy to implement
  - No too much parameter tuning
- Disadvantages
  - The combined classifier is not transparent and interpretable
  - Not a compact representation

# **Practical Applications**

**Goal:** predict how a user will rate a movie

- Based on the user's ratings for other movies
- and other peoples' ratings
- with no other information about the movies



This application is called "collaborative filtering"

Netflix Prize: \$1M to the first team to do 10% better then Netflix' system (2007-2009)

Winner: BellKor's Pragmatic Chaos – an ensemble of more than 800 rating systems

### **Netflix Prize**

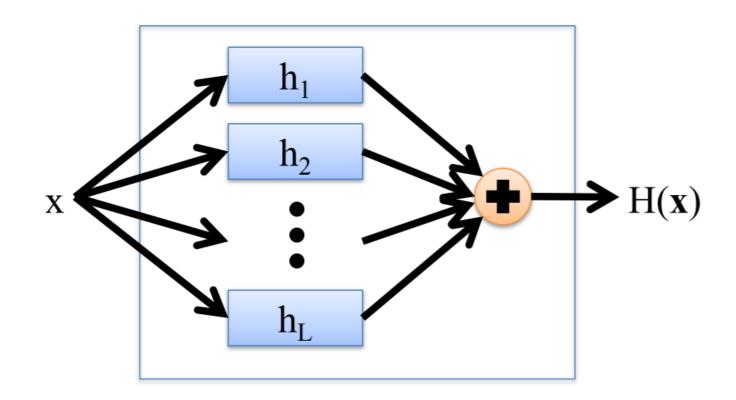
#### Machine learning competition with a \$1 million prize

Rank	Team Name	Best Score	1/2 Improvement	Last Submit Tin	
1	The Ensemble	0.8553	10.10	2009-07-26 18:38	
2	Delinur a magillacciolitada	0.000-4	10.09	2009-07-26 18:18	
Gra	nd Prize - RMSE <= 0.8563				
3	Grand Prize Team	0.8571	9.91	2009-07-24 13:07:	
4	Opera Solutions and Vandelay United	0.8573	9.89	2009-07-25 20:05	
5	Vandelav Industries !	0.8579	9.83	2009-07-26 02:49	
6	PragmaticTheory	0.8582	9.80	2009-07-12 15:09:	
7	BellKor in BigChaos	0.8590	9.71	2009-07-26 12:57	
8	Dace	0.8603	9.58	2009-07-24 17:18	
9	Opera Solutions	0.8611	9.49	2009-07-26 18:02	
10	BellKor	0.8612	9.48	2009-07-26 17:19	
11	BioChaos	0.8613	9.47	2009-06-23 23:06	
12	Feeds2	0.8613	9.47	2009-07-24 20:06	
Pro	aress Prize 2008 - RMSE = 0.8616 -	Winning Team	: BellKor in BigCh	aos	
13	xiangliang	0.8633	9.26	2009-07-21 02:04	
14	Gravity	0.8634	9.25	2009-07-26 15:58	
15	Ces	0.8642	9.17	2009-07-25 17:42	
16	Invisible Ideas	0.8644	9.14	2009-07-20 03:26	
17	Just a guy in a garage	0.8650	9.08	2009-07-22 14:10	
18	Craig Carmichael	0.8656	9.02	2009-07-25 16:00	
19	J Dennis Su	0.8658	9.00	2009-03-11 09:41:	
20	acmehill	0.8659	8.99	2009-04-16 06:29	
Deel	ress Prize 2007 - RMSE = 0.8712 -	Winning Team	r KorBell		

Londorhoard

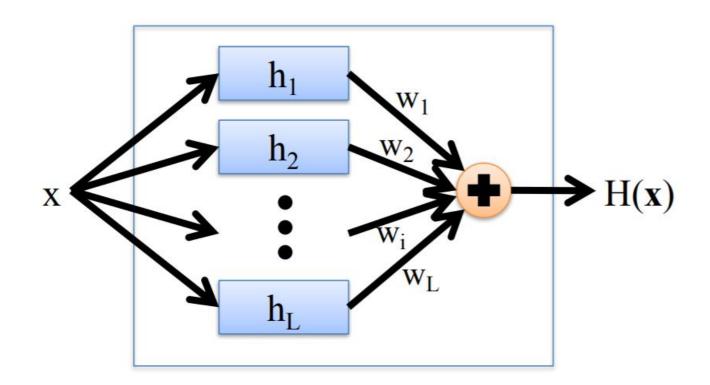


# **Combining Classifiers: Averaging**



Final hypothesis is a simple vote of the members

## Combining Classifiers: Weighted Averaging



 Coefficients of individual members are trained using a validation set

### Reduce error

- Suppose there are 25 base classifiers
- Each classifier has error rate,  $\mathcal{E} = 0.35$
- Assume independence among classifiers
- Probability that the ensemble classifier makes a wrong prediction:

## **Reduce Variance**

• Averaging reduces variance:

$$Var(\overline{X}) = \frac{Var(X)}{N}$$

(when predictions are **independent**)

Average models to reduce model variance

One problem:

only one training set

where do multiple models come from?

Assuming models are independent!

## How to Achieve Diversity

- Avoid overfitting
  - Vary the training data
- Features are noisy
  - Vary the set of features

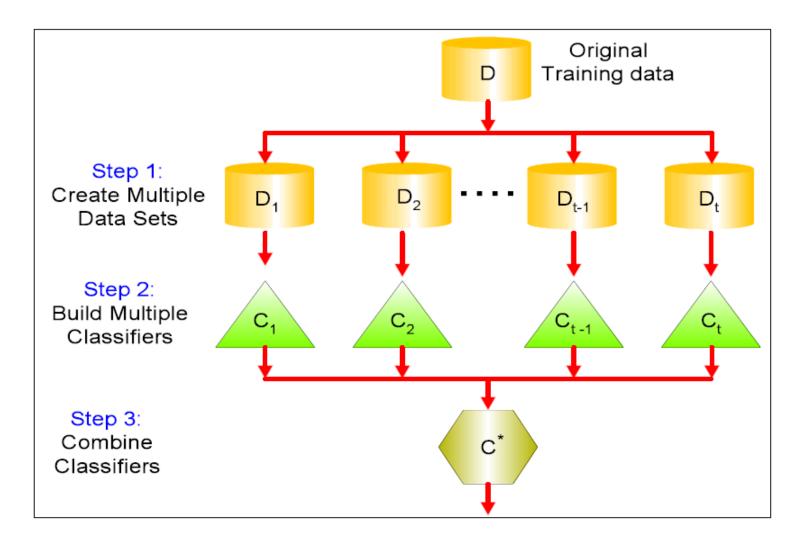
Two main ensemble learning methods

- Bagging (e.g., Random Forests)
- **Boosting** (e.g., AdaBoost)

# Bagging

- Leo Breiman (1994)
- Take repeated **bootstrap samples** from training set *D*
- Bootstrap sampling: Given set D containing N training examples, create D' by drawing N examples at random with replacement from D.
- Bagging:
  - Create k bootstrap samples  $D_1 \dots D_k$ .
  - Train distinct classifier on each  $D_i$ .
  - Classify new instance by majority vote / average.

### General Idea



#### **Majority Votes**

# Example of Bagging

Sampling with replacement

Data ID											
Original Data	1	2	3	4	5	6	7	8	9	10	
Bagging (Round 1)	7	8	10	8	2	5	10	10	5	9	
Bagging (Round 2)	1	4	9	1	2	3	2	7	3	2	
Bagging (Round 3)	1	8	5	10	5	5	9	6	3	7	

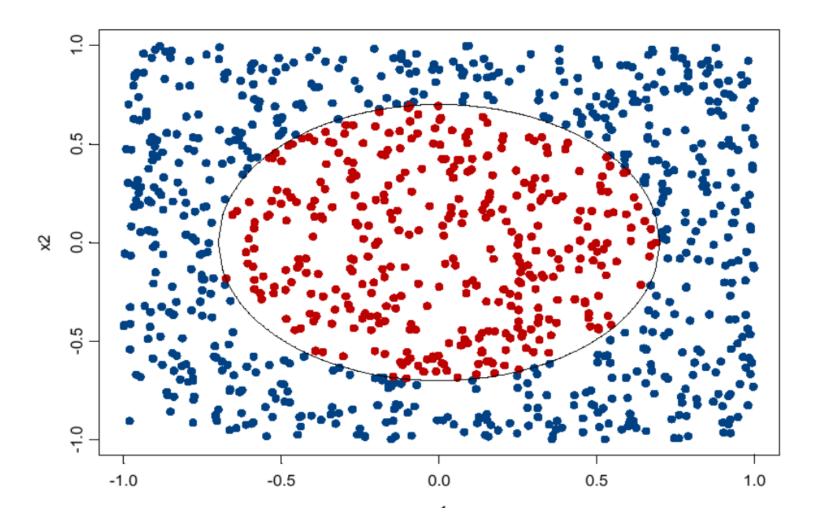
Training Data

- Sample each training point with probability 1/n
- Out-Of-Bag (OOB) observation: point not in sample
  - For each point: prob (1-1/n)<sup>n</sup>
  - About 1/3 of data
  - OOB error: error on OOB samples
- OOB average error
  - Compute across all models in Ensemble
  - Use instead of Cross-Validation error

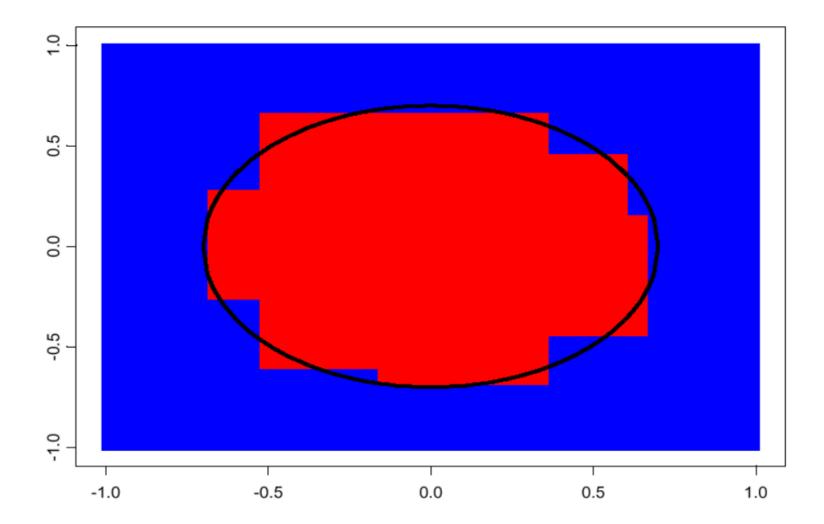
# Bagging

- Can be applied to multiple classification models
- Very successful for decision trees
  - Decision trees have high variance
  - Don't prune the individual trees, but grow trees to full extent
  - Precision accuracy of decision trees improved substantially
- OOB average error used instead of Cross Validation

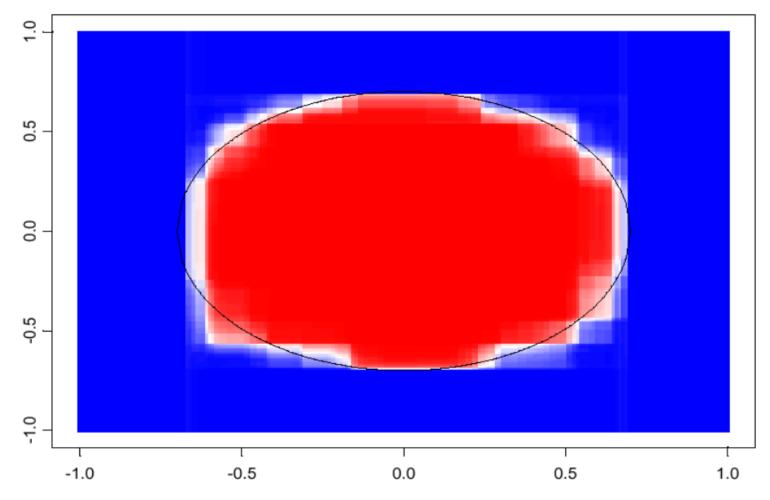
### **Example Distribution**



### **Decision Tree Decision Boundary**



### 100 Bagged Trees



shades of blue/red indicate strength of vote for particular classification

### **Random Forests**

- Ensemble method specifically designed for decision tree classifiers
- Introduce two sources of randomness: "Bagging" and "Random input vectors"
  - Bagging method: each tree is grown using a bootstrap sample of training data
  - Random vector method: At each node, best split is chosen from a random sample of *m* attributes instead of all attributes

## **Random Forests**

- Construct decision trees on bootstrap replicas
  - Restrict the node decisions to a small subset of features picked randomly for each node
- Do not prune the trees
  - Estimate tree performance on out-of-bootstrap data
- Average the output of all trees (or choose mode decision)

Trees are de-correlated by choice of random subset of features

### Random Forest Algorithm

- 1. For b = 1 to B:
  - (a) Draw a bootstrap sample  $\mathbf{Z}^*$  of size N from the training data.
  - (b) Grow a random-forest tree  $T_b$  to the bootstrapped data, by recursively repeating the following steps for each terminal node of the tree, until the minimum node size  $n_{min}$  is reached.
    - i. Select m variables at random from the p variables.
    - ii. Pick the best variable/split-point among the m.
    - iii. Split the node into two daughter nodes.
- 2. Output the ensemble of trees  $\{T_b\}_1^B$ .

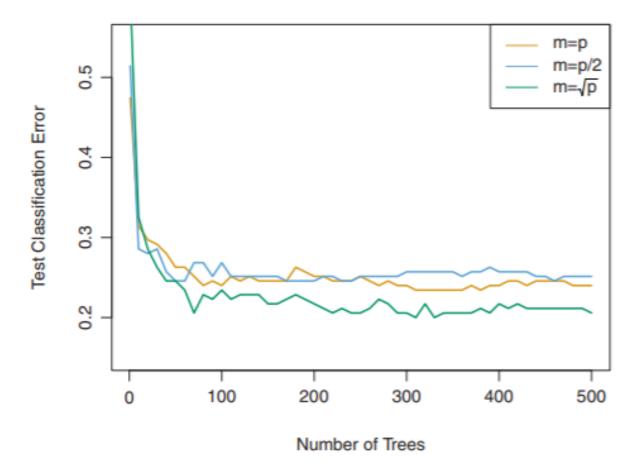
To make a prediction at a new point x:

Regression:  $\hat{f}_{rf}^B(x) = \frac{1}{B} \sum_{b=1}^B T_b(x).$ 

Classification: Let  $\hat{C}_b(x)$  be the class prediction of the *b*th random-forest tree. Then  $\hat{C}^B_{\rm rf}(x) = majority \ vote \ \{\hat{C}_b(x)\}^B_1$ .

#### If m=p, this is equivalent to Bagging

# **Effect of Number of Predictors**



- p = total number of predictors; m = predictors chosen in each split
- Random Forests uses  $m = \sqrt{p}$

## Variable Importance

- Ensemble of trees looses somewhat interpretability of decision trees
- Which variables contribute mostly to prediction?
- Random Forests computes a Variable
  Importance metric

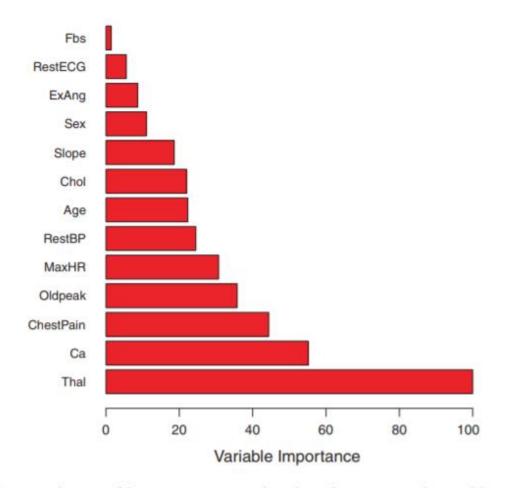
# Gini index

- Take a node of decision tree
- Let  $p_i$  be the fraction of examples from class i
- Measures the "purity" of the node
  - If node has most examples from one class, Gini index is low
- What is the probability that a random example is mis-classified at that node?

$$-\sum_{i=1}^k p_i(1-p_i)$$

Close to Information Gain

### Variable Importance Plots



**FIGURE 8.9.** A variable importance plot for the Heart data. Variable importance is computed using the mean decrease in Gini index, and expressed relative to the maximum.

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# Acknowledgements

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  - Andrew Ng
  - Eric Eaton
  - David Sontag
- Thanks!