CS1800 Day 17

Admin:

- HW5 due today
- HW6 released today
- "Extra" video on BFS / DFS (piazza post 440)
- might end few mins early today, feel free to hang out if you have BFS / DFS or Dijkstra questions

Content:

Searching through all the nodes in a graph:

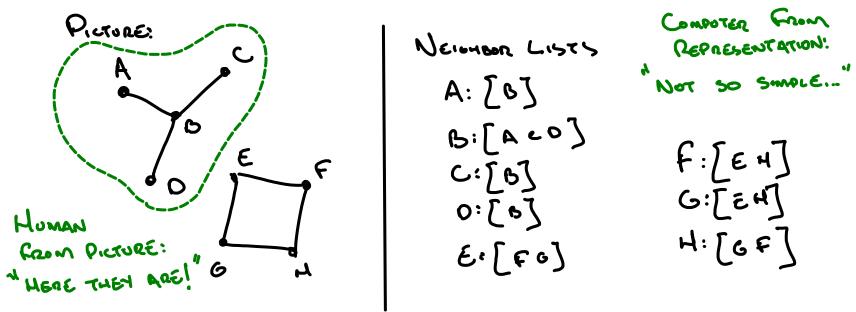
- Breadth First Search (BFS)
- Depth First Search (DFS)

Finding the shortest path between two nodes in a weighted graph:

- Dijkstra's Algorithm

Searching a graph: (BFS & DFS intro)

Goal: Using a computer, walk (order) to all nodes which are connected to node A



Depth First Search: Inuition & Animation

Approach: "visit an adjacent, unvisited node as long as possible, then backup one edge and look for another vertex to visit, using a depth first search."

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gif source: https://www3.cs.stonybrook.edu/~skiena/combinatorica/animations/search.html

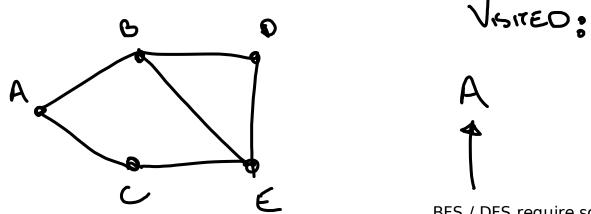
Breadth First Search: Intuition & Animation

Approach: "Visit all the vertices adjacent to the starting vertex, then do a breadth first search from each of those vertices."

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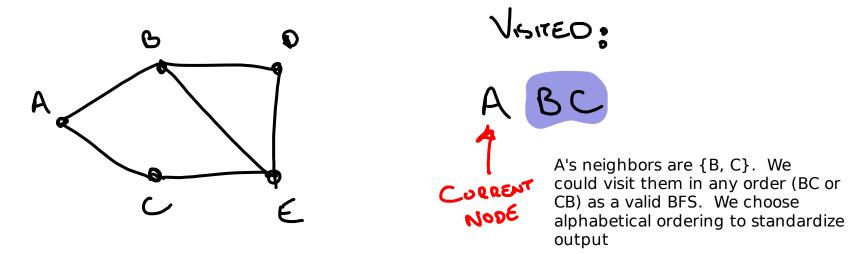
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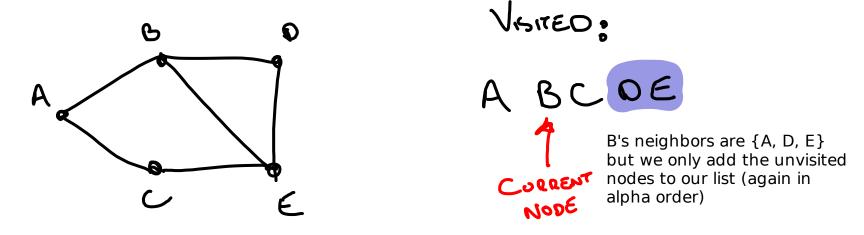
BFS / DFS require some starting node be given, where the search is initialized.

Approach: "Visit all the vertices adjacent to the starting vertex, then do a breadth first search from each of those vertices."



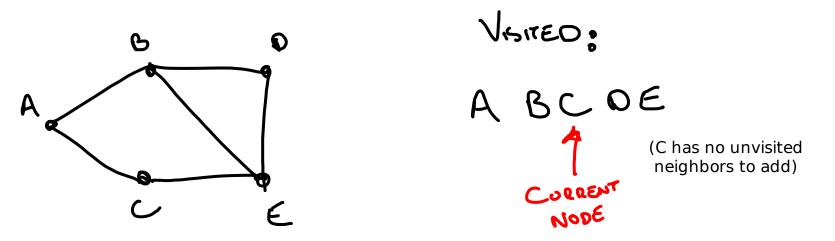
Breadth First Search: Example

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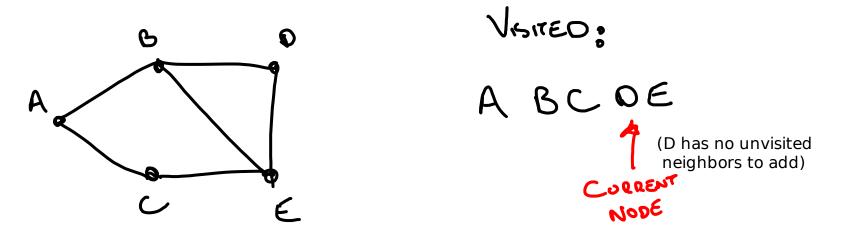
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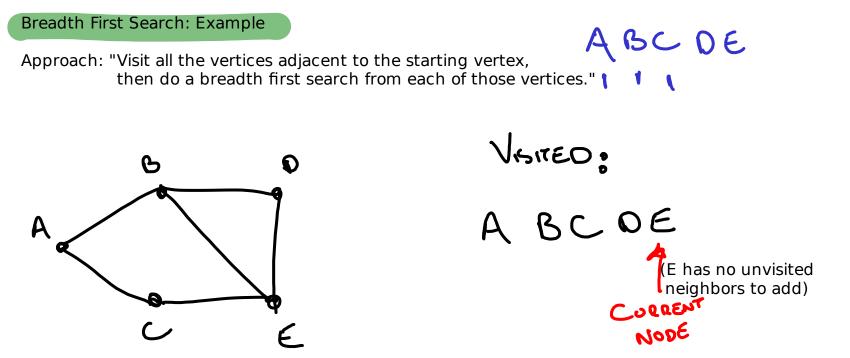


Looking at the picture, you can tell we're done. The computer doesn't know ... must finish BFS on visited list Breadth First Search: Example

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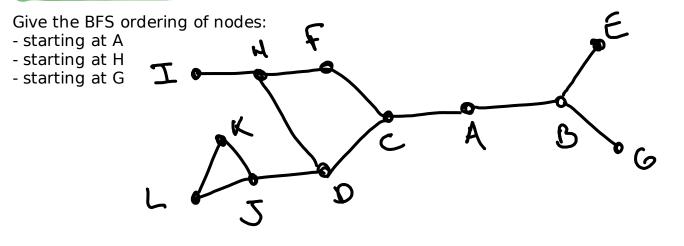


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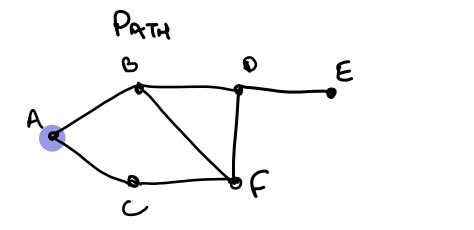
In Class Activity: Breadth First Search



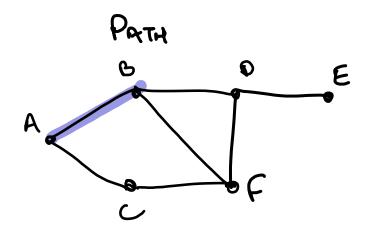
BFS start @ a: ABCE GDFH JIKL BFS start @ h: HDFI CJAK LBEG BFS start @ g: GBAE CDFH JIKL

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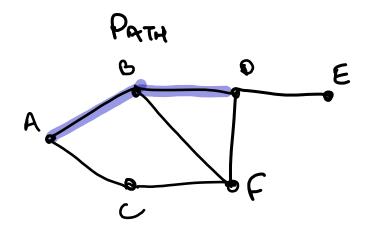
VISITED:

AB

A has two unvisited neighbors {B, C}

Again, we choose to visit the one which is alphabetically first

then backup one edge and look for another vertex to visit, using a depth first search."

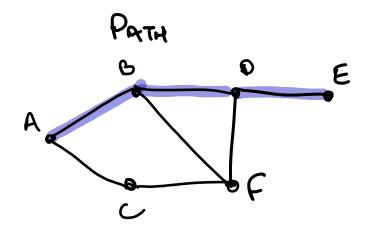


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B has two unvisited neighbors {D, F}, we choose the one which is alphabetically first.

then backup one edge and look for another vertex to visit, using a depth first search."

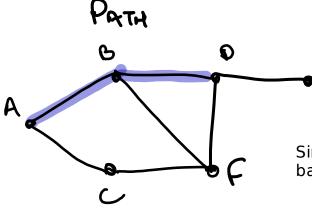


VISITED: ABOE

D has two unvisited neighbors {E, F}, we choose the one which is alphabetically first.

F.

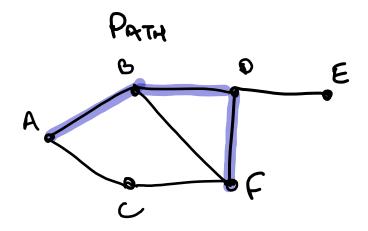
then backup one edge and look for another vertex to visit, using a depth first search."



VISITED: ABOE

Since E has no unvisited neighbors, we backup our path and repeat the DFS process

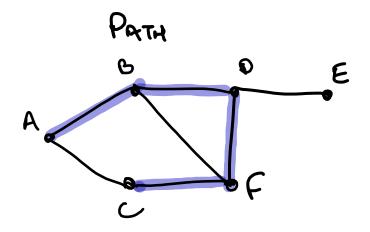
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VISITED: ABOEF

D has 1 unvisited neighbor {F}

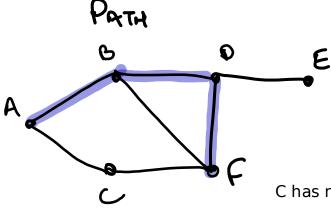
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VISITED: ABOEFC

F has 1 unvisited neighbor {C}

then backup one edge and look for another vertex to visit, using a depth first search."

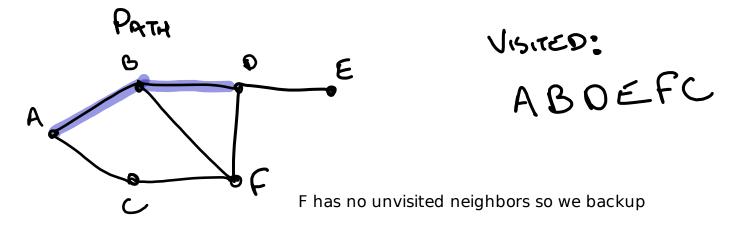


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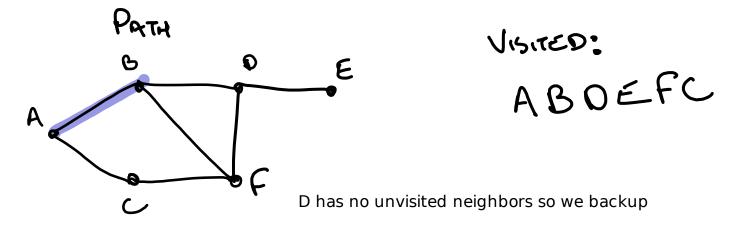
C has no unvisited neighbors so we backup

(You can tell from the picture we're done ... the computer can't)

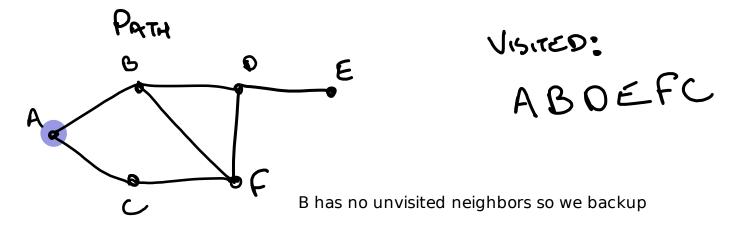
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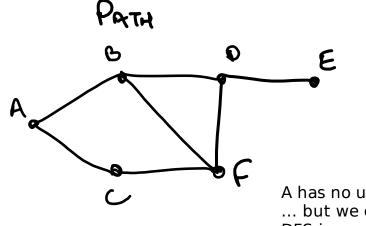
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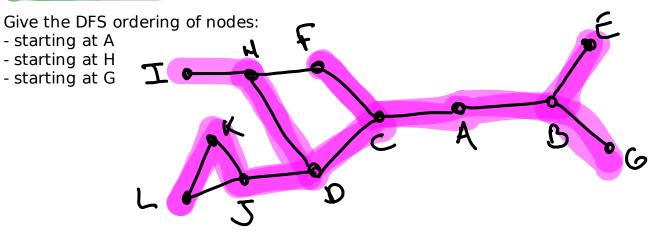
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VISITED: ABOEFC

A has no unvisited neighbors so we backup but we can't backup as A was our starting node. DFS is complete

In Class Activity: Depth First Search

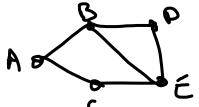


DFS start @ a: ABEG CDHF IJKL DFS start @ h: HDCA BEGF JKLI DFS start @ g: GBAC DHFI JKLE

BFS / DFS: Why did we do this again?

- BFS/DFS gives you the largest, connected subgraph

- "What are all the cities I can get to taking flights from only one airline?"
- computer can tell if a graph is connected
- one run gives a connected component ... repeat again for others
- DFS detects cycles in a graph
 - cycle exists if and only if we bump into a neighbor which has already been visited
- BFS orders all nodes from nearest to furthest starting point



BES ORDERING: ABCDE PATH LENGTH FROMA: 01122

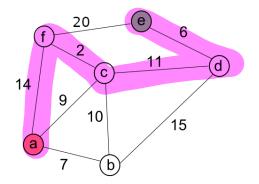
- Comp Sci Education:

- They're very similar to many other graph algorithms
- They can be built recursively (a function which calls itself). super useful pattern

Shortest Path Problem

What path (sequence of unique, adjacent edges) has the lowest total weight from a to e?

Motivation: Suppose each node is a location and the edges weights are times to travel between the location. The shortest path gets us from a to e quickest

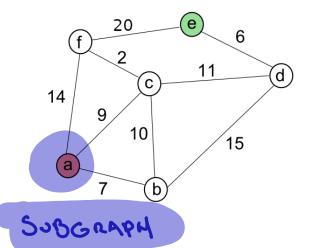


An example path (not shortest):

What path (sequence of unique, adjacent edges) has the lowest total weight from a to e? (Assumes all edge weights are non-negative)

Approach: - Track shortest path from a, potentially through a subgraph, to all other nodes

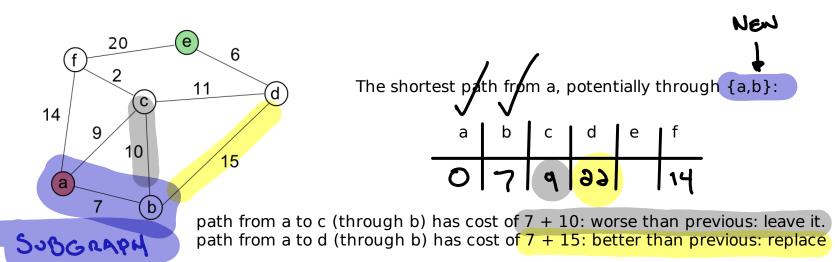
- Add node to subgraph with shortest path weight
- Stop when there is no node outside subgraph with lowest weight to destination



The 7 above tells us we can get from a to b at a cost of 7

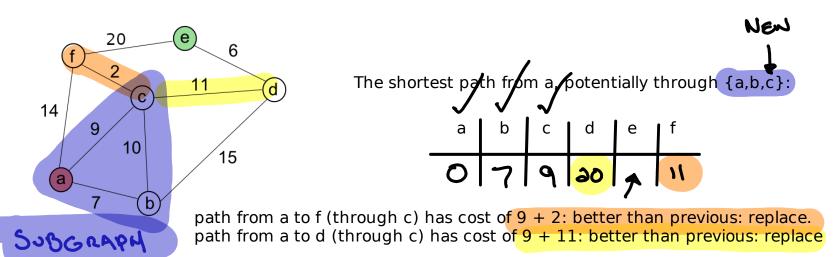
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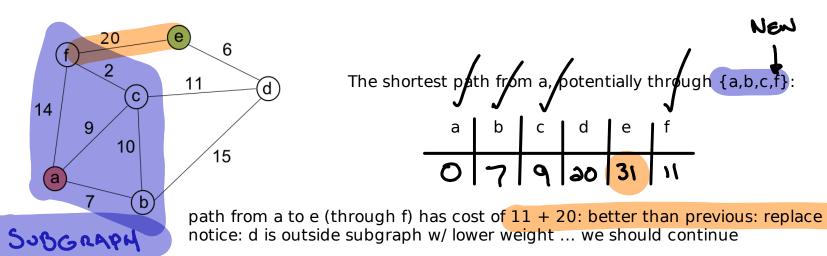
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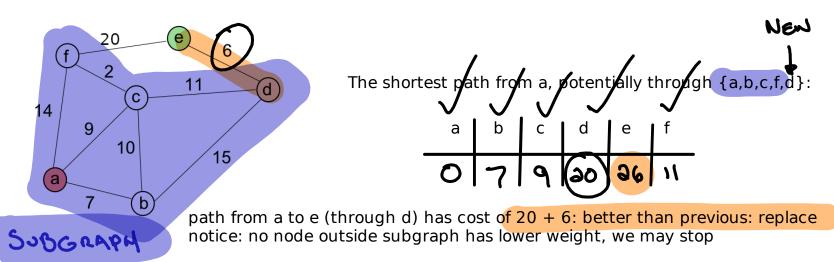
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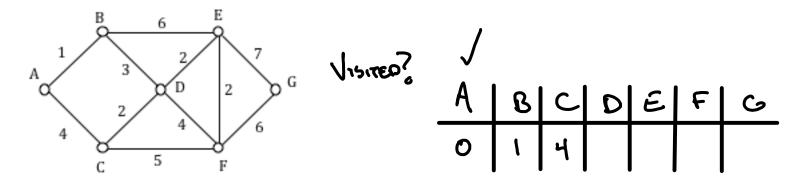
In this example, we visited all nodes but our destintion.

In others, we needn't visit all nodes but our destination. (stopping early = less computation = faster runtime = good news!) In Class Activity: Dijkstra's Algorithm

Find the shortest path weight from A to G.

Please write out each step of your algorithm (erasing work makes it tough to find errors!)

- clearly label nodes which nodes are in the "sub-graph" (those you've visited)
- write path weight from starting node to all others through the subgraph (i.e. previous table)



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