## CS1800

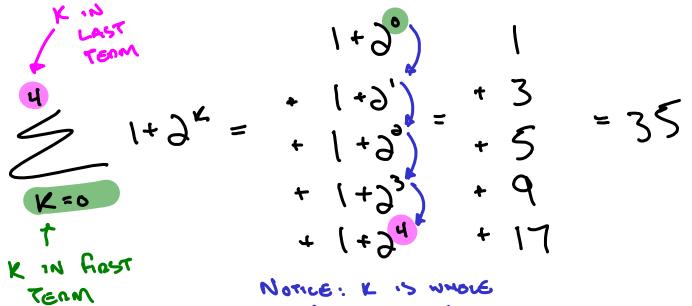
## Admin:

- hw7 due Friday
- exam2 due Friday
- recitation this week:
  - no quiz
  - focus on exam2 practice problems (available on website)

#### Content:

- Series & Sequences (Arithmetic, Geometric & Quadratic)
- Given a series, identify its type (may be none of the 3 above)
- Express the i-th term in a sequence
- Compute the partial sum of a series (Arithmetic & Geometric)

Summation Notation: a quick reminder



Notice: K is whole Nomber which Steps by 1 A sequence is an ordered list of objects (always numbers in this CS1800 unit)

A series is the sum of an infinite sequence of objects

$$1+3+3+4+5+6+...=$$

A partial sum (of a series) is the sum of part of a series

$$1+2+3+4 = \sum_{K=1}^{4} K = 10$$

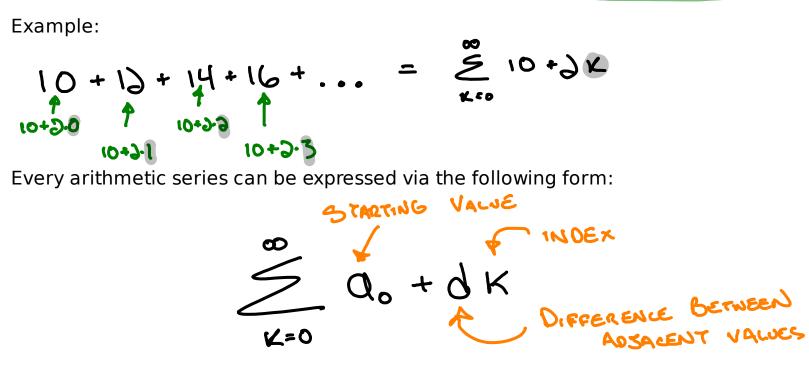
Arithmetic Sequence / Series: What it is (and how to identify it)

An arithmetic sequence's first difference (next term - current term) is constant:

To test if a sequence is arithmetic, compute first difference. If its constant then sequence is arithmetic.



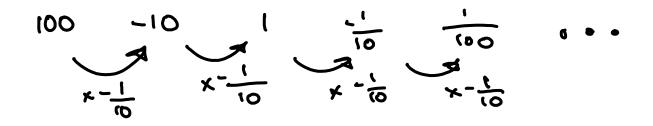
### Arithmetic Series / Partial Sum: What do they look like in summation notation?



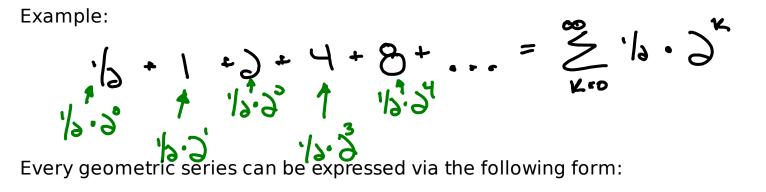
Geometric Sequences / Series: What it is (and how to identify it)

An Geometric sequence is one whose first ratio (next term / current term) is constant:

To test if a sequence is geometric, compare first ratio. If its constant then sequence is geometric.



#### Geometric Series / Partial Sum: What do they look like in summation notation?



Quadratic Series / Partial Sum: What is it? (i.e. what does it look like in sum notation?)

Every quadratic series can be expressed as:

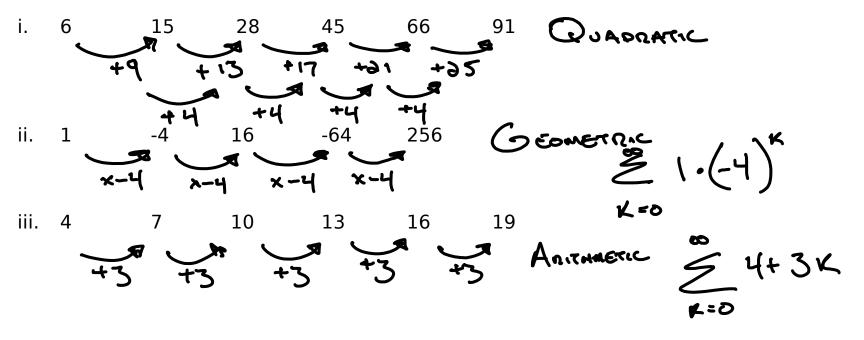
$$\begin{array}{c} & & & & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ &$$

Quadratic Sequences / Series: How to identify it

The second difference of a quadratic sequence is constant

410 6.251 DIFFERENCE チン SECOND DIFFERENCÉ

In Class Activity: Identify the type (arithmetic, geometric, quadratic) of each of the following sequences. If sequence is arithmetic or geometric, express its corresponding series in sum notation.



Quadratic Series: Given sequence, how to compute a, b, c in summation notation

$$6 = 0.0^{\circ} + 6.0 + c \implies c = 6$$
  $p = 2 + 6 = 7$ 

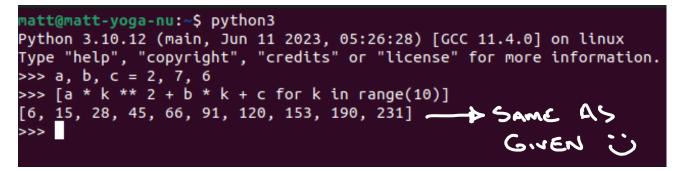
$$15 = 0 \cdot 1^{2} + b \cdot 1 + C = 2 \quad 9 = 0 + b$$

$$38 = 0.3 + 0.3 + 0 = = -33 = 40 + 30 = -7 = -30 + 0$$

$$=> || = \alpha + 9$$
  
$$=> \alpha = d$$

# Checking our work with python

(you needn't ever do the same for CS1800 ... but cute to see that you can using python)



If you're interested in doing the same and don't have python on your computer, check out "google colab" which allows you to run python code in the cloud.

## In Class Activity

Find the coefficients (a, b, c) which allow us to express the following series in summation notation (175 Ouroratic) Sax+bK+C  $1 + 3 + 7 + 13 + 21 + 31 + 43 + 57 + 73 + 91 + \dots$ 1240 ~ d= |+b=> 1= 0.03+b.0+c => c=1  $3 = a \cdot |^{2} + b \cdot |^{2} = 3 = a + b + |^{2} = 3 = a + b =$ 7= a· 3+ b· 2+ c => 7 = 4a+ 2b+ 1 => 6 = 4a+ 2b => 3=2a+b=a+a+b => 3= a+ 2= 2a=1

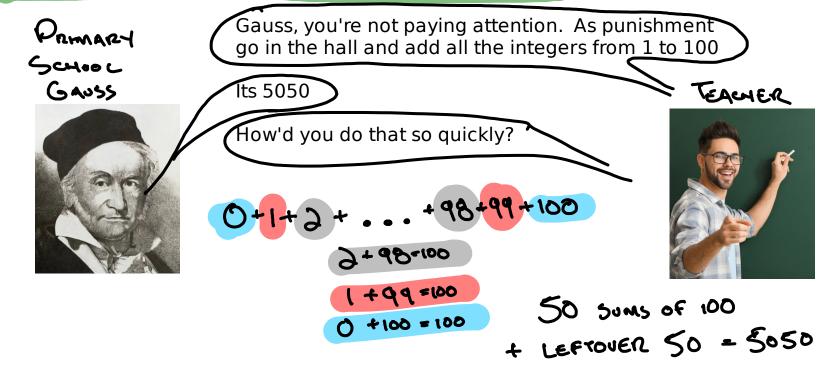
Up next: computing partial sums (arithmetic & geometric ... not quadratic)

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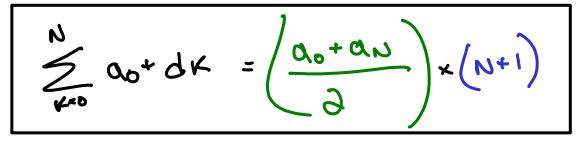
$$0+1+3+4 = 4$$
  $K = 7$   
 $K=0$   
 $K=0$   
 $K=0$   
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Computing Arithmetic Partial Series: motivation via tall tale



Computing Arithmetic Sums: A more generalizable expression

SMALL TEST ENAMPLE 1+2+3+4+5 = 15 \* NUMBER OF TERMS Avenabe Term  $\frac{1+5}{2} = 3 \times$ 



Computing Geometric Series Partial Sums

$$S = \sum_{k=0}^{N} Q \Gamma^{k} = Q + Q\Gamma + Q\Gamma^{2} + \dots + Q\Gamma^{N}$$

$$S = \sum_{k=0}^{N} Q \Gamma^{k} = Q + Q\Gamma + Q\Gamma^{2} + \dots + Q\Gamma^{N}$$

$$P_{NATIONL} S_{UME}$$

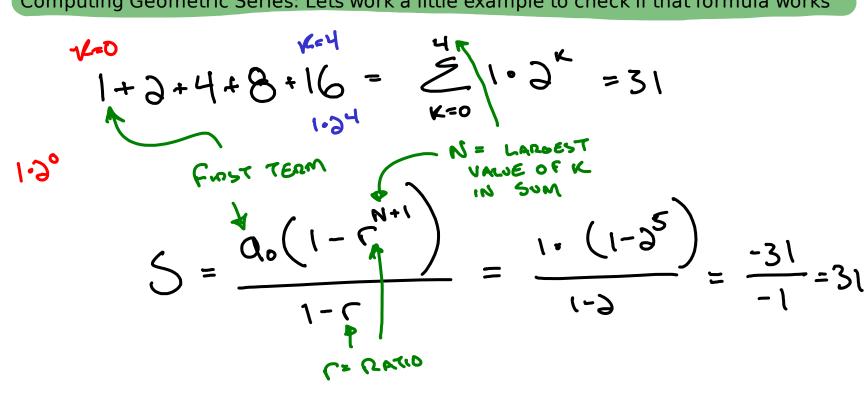
$$S = C = Q + Q\Gamma + Q\Gamma^{2} + \dots + Q\Gamma^{N} + Q\Gamma^{N}$$

$$We D \quad UME = TO$$

$$S = C = Q - Q\Gamma$$

$$S = Q - Q\Gamma$$

Computing Geometric Series: Lets work a little example to check if that formula works



## In summary (Arithmetic, Geometric & Quadratic Sequences / Series / Partial Sums)

	Arithmetic	Geometric	Quadratic
How to identify?	0 4 6 6 F	1 2 4 8 (6 x 3 x 3 x 3	1371321 +2 +4 +6 +8
	Constant First Difference	CONSTANT RATIO	+3 +3 +3 CONSTAUT SECOND DIFFERENCE
Expression of a single term	00+0K	a.r <sup>k</sup>	QK+bK+C
Computing partial sum	$ \frac{N}{\sum_{k=0}^{N} a_0 + d_k} = \left(\frac{a_0 + a_y}{\partial}\right) \cdot \left(N + 1\right) + Nomber $ Auscanse of TERM TERMS	$N = Q_{0} \left( K = \frac{Q_{0} \left( 1 - \Gamma^{N+1} \right)}{1 - \Gamma} \right)$	KIND OF A CALCULUS FAMG (NOT NEEDED FOR CS1800)

