CS 1800 Day 4

Admin:

- hw1 due Friday
- please read the HW instructions (group members, tagging pages etc)
- tutoring group update (they've been formed, a few missing TAs, we'll be in touch ASAP, if you'd like to join one please see instructions on site)

Content:

- logic statements & predicates
- truth tables
- logic operators (AND, NOT, OR)

(just an intro to these topics, we'll do more next lesson too)

- existential / universal quantifier
- conditionals

When should machine:

- give a soda
- return change



When should sunroof:

- open

- close



When should pacemaker: - send pulse to muscle to pump blood? - shock to restart heart



Logic gives us an unambiguous language to describe behavior (spoken languages, like english, can be ambiguous)



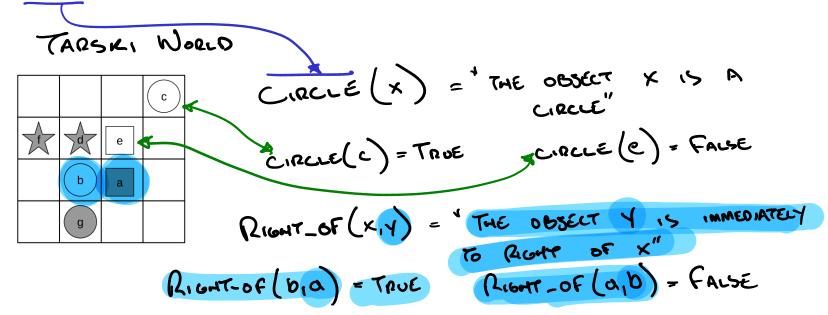
Statement - a sentence which is either true or false

Which of the following are statements?

- 1. Today is Sept 19
- 2. "This big wooden horse definitely doesn't have greek soldiers inside" - Greeks who just put soldiers in that horse
- 3. What is your favorite color?
- 4. There is intelligent life on mars



Predicate - a statement about one or more variables (i.e. mad libs)



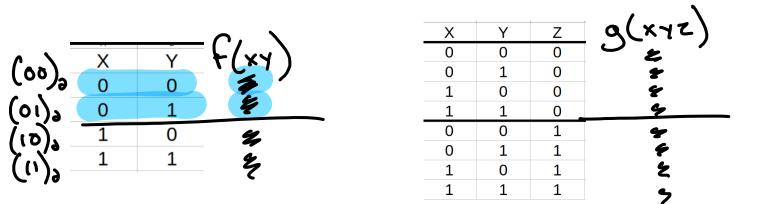
DO, 1 DTRUE, FALSE CONVENTION: BITS AND BOOLEANS

| = True() = FALSE

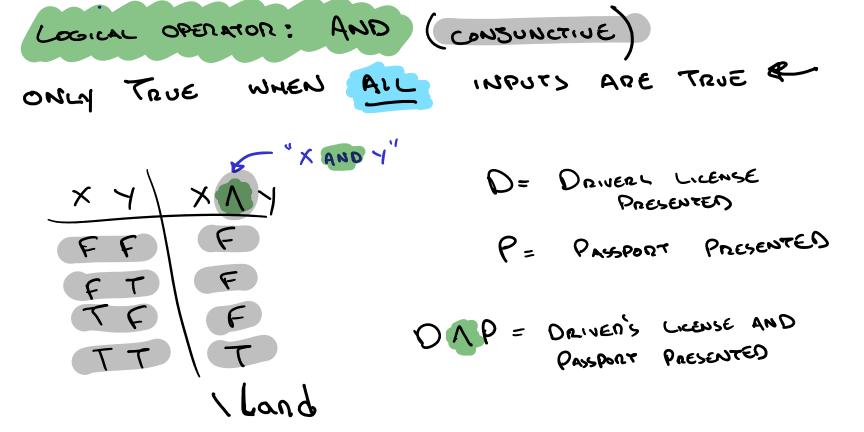


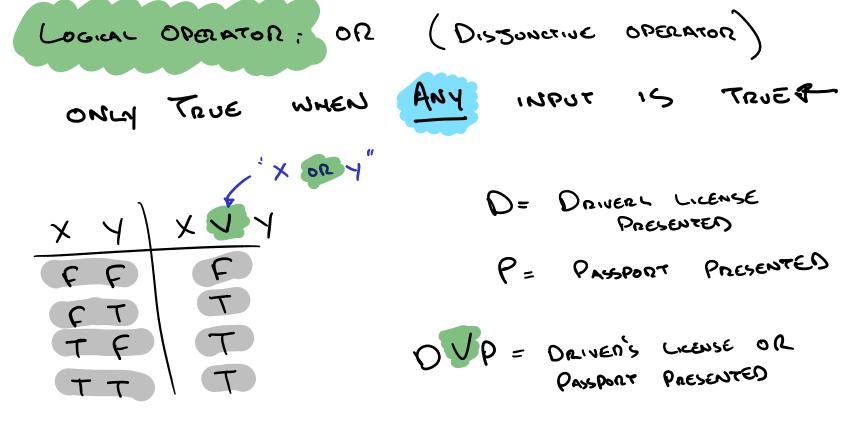
We'll often describe a function of one or more inputs (e.g. vending machine operation)

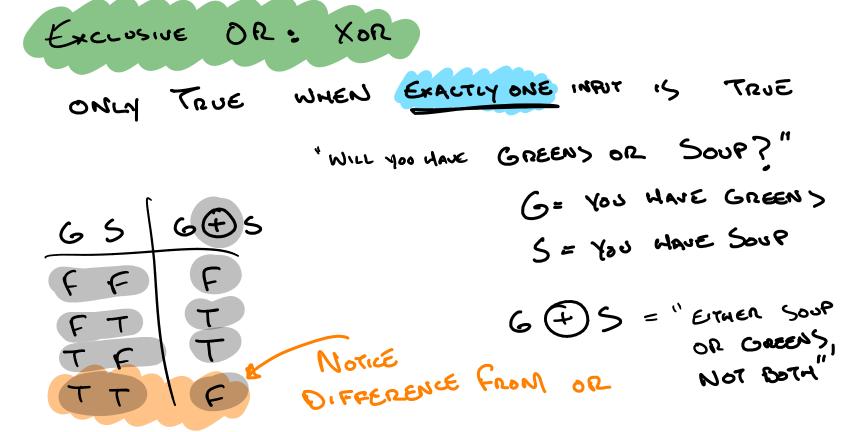
A Truth Table specifies an output associated with every possible combinations of inputs

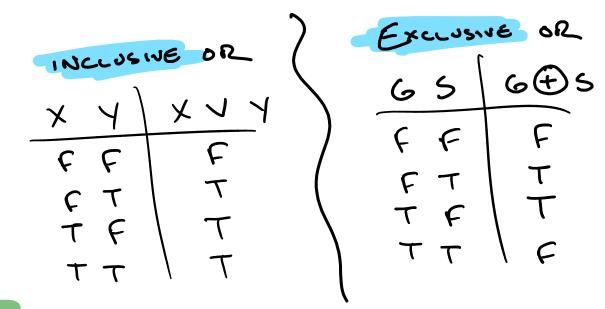


LOGICAL OPERATOR : NOT (NEGATION) (nx x VALUE CHANGES TRUTH *NOT × X= "IT'S RAINING" F T F 7 X = " IT'S NOT RAINING"





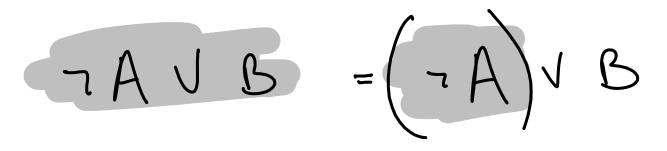




Convention": Most of the time when folks say "or" they intend the inclusive or

but not all the time ... good luck! ;)





Assume the negation operation applies to statement immediately to its right.

If the negation applies to multiple statements, use parenthases as below:

Truth tables allow us to build complex expressions in bite-size steps.

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In Class Assignment:

Build a truth table for each of the two expressions below. Results for both might feel familiar, thats ok :)

JA A JB 7 (AVB) A B [7 A [7 B 17A17B B ANB 7 (AND) 0 0 1 1 1 0 1 1 0 0 1 0 0 0 0 1 0 0 0 0



Two statements are logically equivalent if their truth table columns are identical.

Statements which are logically equivalent:

- always have the same truth value (True or False)
- may be substituted for each other
 - like one does in our familiar algebra (e.g. x = 3 into 10 = x + y)

Example: logically equivalent statements:

"This shape has exactly four sides of equal length at right angles to each other"

"This shape is a square"

There are other laws too:

- helpful to simplify an expression

we'll study these alongside
 set algebra & circuits, which are
 related topics, more to come later ...

Associative Laws

 $(P \lor Q) \lor R = P \lor (Q \lor R)$ $(P \land Q) \land R = P \land (Q \land R)$

Double Negation

 $\neg \neg P = P$

DeMorgan's Laws $\neg (P \lor Q) = \neg P \land \neg Q$ $\neg (P \land Q) = \neg P \lor \neg Q$

Distributive Laws

 $P \land (Q \lor R) = (P \land Q) \lor (P \land R)$ $P \lor (Q \land R) = (P \lor Q) \land (P \lor R)$

Absorption Laws $P \land (P \lor Q) = P$ $P \lor (P \land Q) = P$

Complement Laws

 $P \lor \neg P = T$ $P \land \neg P = F$

Idempotent Laws

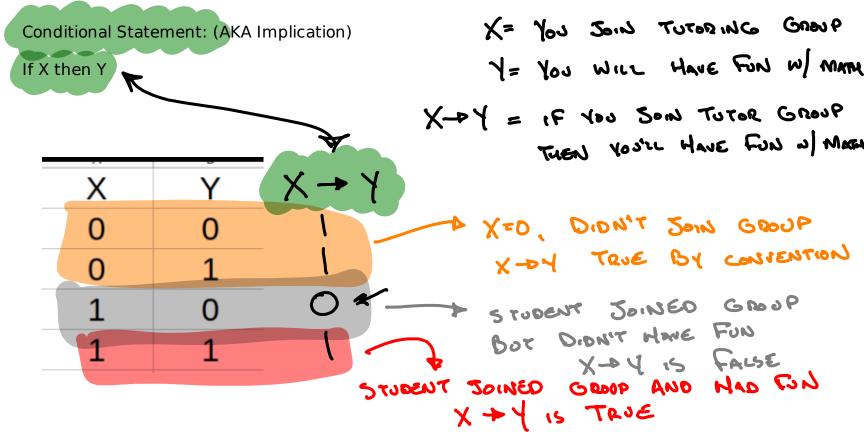
 $P \lor P = P$ $P \land P = P$

Identity

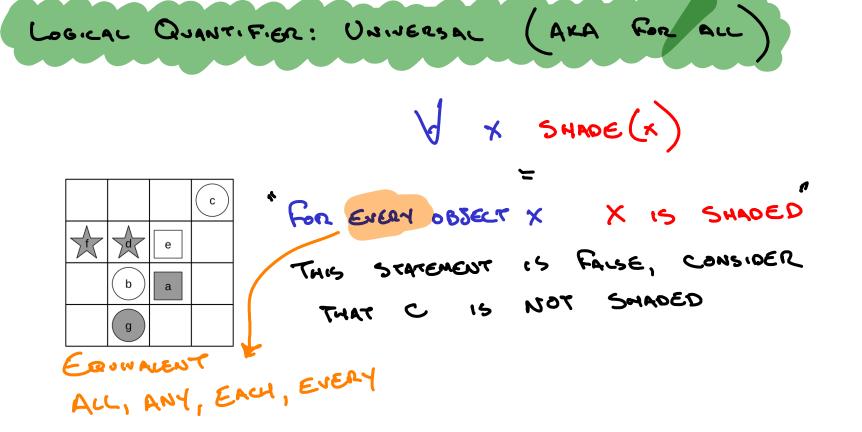
False \lor P = P True \land P = P

Domination:

True \lor P = True False \land P = False

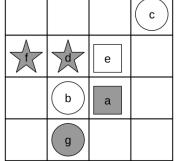


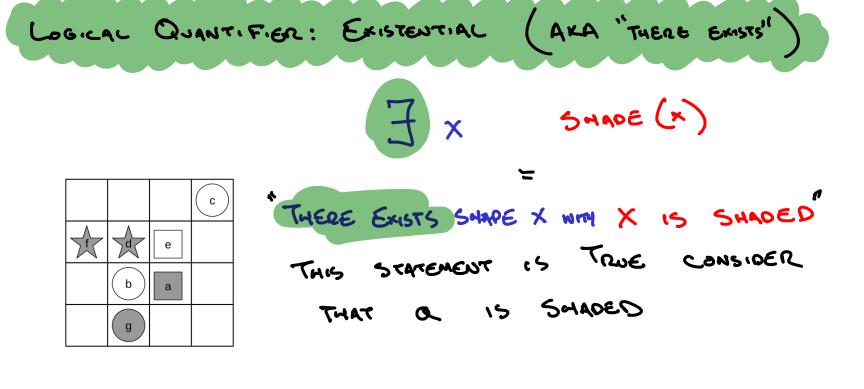
JOIN(R) = STUD X JOIN GROUP FUN(R) = STUD X FUN W/ WARY X STUDENT Y X JOIN(X) - FUNS(X)

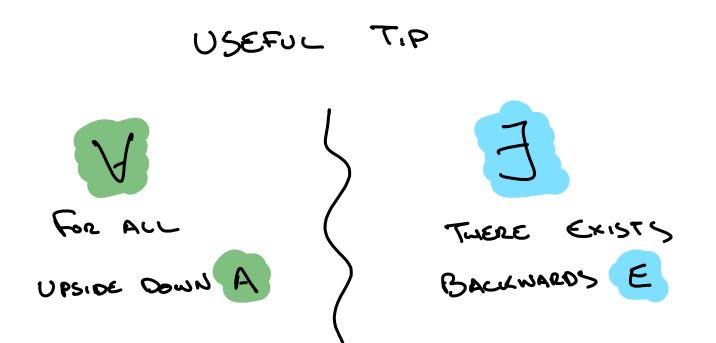


QUILL PRACTICE FOLLOWING STATEMENT TRUE? 15 Vx STAR(x) -> SHADE(x)

For all x, if x is a star then x is shaded







In Class Activity:

Using logical operators (AND, OR, NOT) quantifiers (for all, there exists) and conditionals (if-then), translate each statement below:

English to logic (define your own statements & predicates as needed)

- You shall not pass! - Gandalf

$$P = EVENT BALDOG PASSES$$

 $- P PERSON$
 $- P PERSON$
 $- P PERSON$
 $- P PERSON$
 $P(x) = EVENT PERSON$

- "Everybody loves you when you're 6 feet underground" - John Lennon

- I never leave the house without my blue shoes or a hat

L-BVH

- "There's no place like home" - Dorothy in Wizard of Oz

$$= \sqrt{2} \times Home(x)$$

HX XXHOME - X is NOT LIKE HOME LOVE (YX) HTY DEAD(x)->