CS1800 Day 23

Admin:

- hw8 (seq & series, function growth)
 - due this Friday
- hw9 (algorithms)
 - due next Tuesday
 - slightly shorter than most
- "exam3"
 - written to take 30 mins but you'll get 50 minutes to complete it (+20 min submit)
 - 2 math problems, 1 quick theory-ish problem
 - format identical to other exams
 - covers class 20, 22, 23
 - class 24, reccurence relations, will not be tested on exam3

Content (algorithms):

- search algorithms (unordered linear search & binary search)
- sort algorithms (insertion & merge)
- quantifying (estimating) algorithm run time

TRACE (Northeastern's survey of course quality)

TRACE feedback helps me be a better teacher (in a future semester) TRACE feedback helps NU identify strong / weak teachers

- feedback is anonymous
- we won't get feedback until after you've received your grade
- please review both CS1800 and CS1802
 - -CS1802 for recitation hour, materials, recitation related admin
 - -CS1800 for everything else (lesson, homework, exam, office hours, tutorial, all other admin...)

Please take a few minutes to give feedback about what worked and what didn't in the course. (accessible via myNortheastern or email)

Review: Log Operation

 $3^{3} = 8 + 106 = 3$

LOGBX is THE POWER OF B EQUAL TO X

$$Lob_{3} = 37 = 3$$

In Class Activity (log practice)

Solve for x in each of the equalities below

 $\log_{10} 1000 = x = 3$ log_2 16 = x = └ 9₁₀ = 10 $\chi = \partial^{\circ} = 0 \partial 4$ _00_ X= く $\log_x 125 = 3$ LOG2 16.256 = X

 $\log_2 16 + \log_2 256 = x - 4 + 3 = 0$ (++) write a general rule for the sum of logs with the same base which this example suggests List Convention: Let's start indexing our lists at zero

$$L = \begin{bmatrix} 14 & 102 & -4 & 6 \\ 102 & L[1] & L[2] & L[3] \end{bmatrix}$$

Definitions:

"Search": Find index of first occurance of an item in a list

Given the following list: [2, -2, 100, 2.347, 4, 100, 5, -17]

- search question: find the index of 2
- search question: find the index of 100
- search question: find the index of 18
- search output: 0 is index of first 2
- search output: 2 is index of first 100
- search output: 18 isn't in the list

"Sort": given a list of items, order them from least to greatest (equal items in any order)

Sort input: [6, 3, 2, 100, -5, 3] Sort output: [-5, 2, 3, 3, 6, 100]





Why sort?

 sorted lists are quicker to operate on (see binary search vs unordered linear search)

- sorted list positions offer insights
 - first item is minimum
 - last item is maximum
 - item in middle is median
 - "bob" isn't between "alice" and "chuck" in a sorted list, therefor bob not in list

search inputs: a list and an item to search for

Intuition: Starting at first index in list, check if equal to item, move rightward until item found

$$L = \begin{bmatrix} 14 & 103 & -4 & 6 \\ 167 & L[i] & L[i] & L[i] & L[i] \\ 1 & WE & CHECK & NEXT \\ 1 & NDEK \\ CURRENT \\ INDEX \end{bmatrix}$$

Search: Unordered Linear Search

search inputs: a list and an item to search for

Intuition: Starting at first index in list, check if equal to item, move rightward until item found

$$L = \begin{bmatrix} 14 & 103 & -4 & 6 \\ L[0] & L[1] & L[0] & L[3] \\ 1 & & & \\$$

Search: Unordered Linear Search

search inputs: a list and an item to search for

Intuition: Starting at first index in list, check if equal to item, move rightward until item found

$$L = \begin{bmatrix} 14 & 102 & -4 & 6 \\ L[0] & L[i] & L[2] & L[3] \\ \uparrow & & \\ CURRENT \\ INDEX \end{bmatrix}$$

Search: Unordered Linear Search

search inputs: a list and an item to search for

Intuition: Starting at first index in list, check if equal to item, move rightward until item found

$$L = \begin{bmatrix} 14 & 102 & -4 & 6 \\ L[0] & L[1] & L[2] & L[3] & WE RETURN 3 \\ 1 & 100$$

Is this algorithm any good? What do we want from our algorithms?

- Correctness
- Low memory use: doesn't require the computer to examine too much at once
- Quick runtimes: completes the task in as few "operations" as possible for input of size n

- Simplicity: all else equal, we humans have to build and maintain this thing. simplicity reduces the chance that we'll make an error

In practice (and in CS1800) folks usually focus on the runtimes of correct algorithms.

Quantifying runtime:

Runtime: how many "operations" required to complete algorithm for input of size n

To simplify our analysis of algorithms:

- lets only count comparisons (is item0 less than, equal to, or greater than item1?)

<whole class card demo: counting operations in a few unordered linear searches>

(punchline: different inputs require different number of comparisons)

Quantifying runtime:

Runtime: how many "operations" required to complete algorithm for input of size n

To simplify our analysis of algorithms:

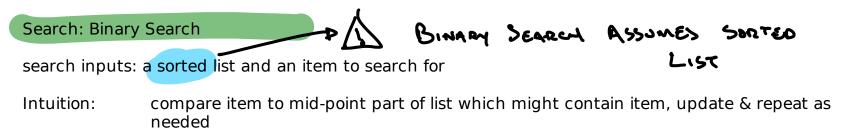
- lets only count comparisons (is item0 less than, equal to, or greater than item1?)
- lets assume the worst possible input for a given algorithm (requiring the most comparisons)

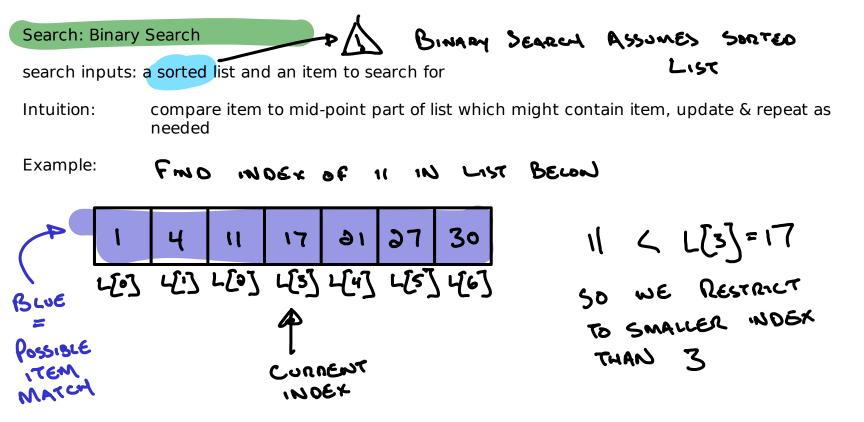
In the worst case, for an input list with n items:

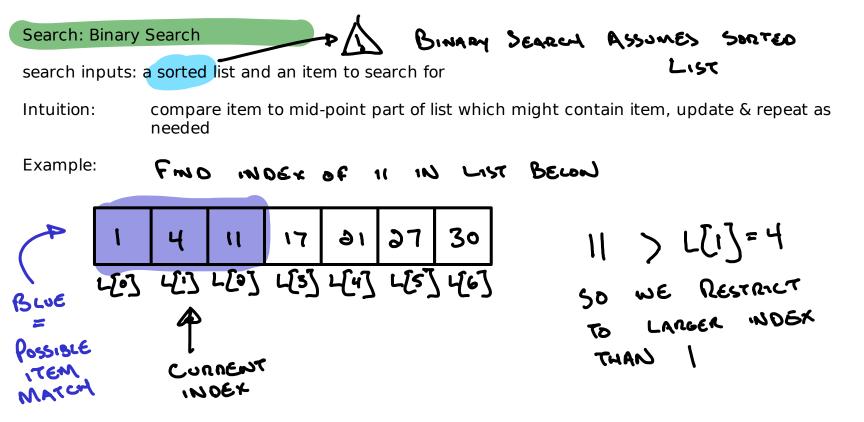
- unordered linear search requires we compare our item to every input: T(n) = n

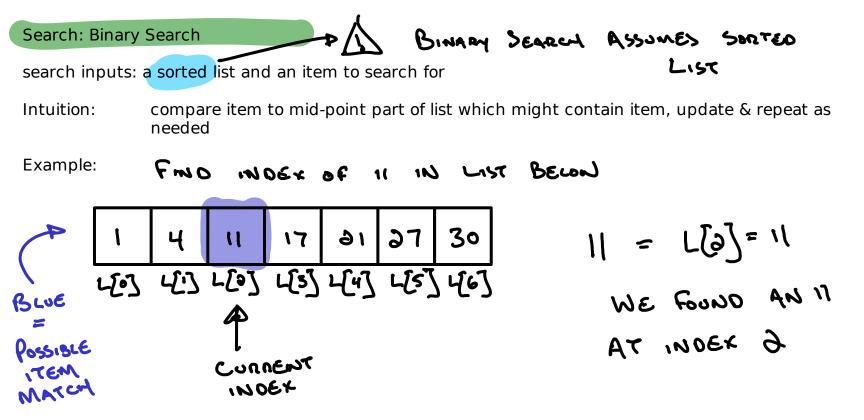
of comparisons

<show binary search with cards>









In Class Activity:

- Build an example (target item & list of size 7) where binary search works quickest (fewest comparison)

```
list=[2,3,4,5,6,7,8]
target = 5
list = [5,5,5,5,5,5,5]
```

- Build an example (target item & list of size 7) where binary search works slowest (most comparisons)

```
list = [2,3,4,5,6,7,8]
target = 2 (or 8)
```

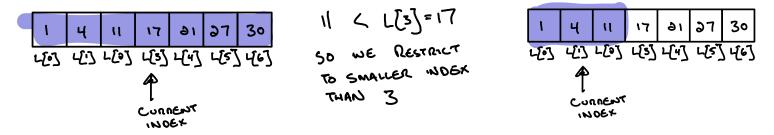
For a list of size n, what is the most comparisons binary search will require to complete?
 (hint: coming up with an exact expression can be tough here, feel free to approximate as needed to keep it simple. It can feel funny to approximate like this at first, but we'll justify it with our Big-O definition of function growth)

Loc,n

Notice:

- the "worst case" of binary search is when we cannot stop early for having found target item
- Each comparison cuts the set of possible matching indexes (blue shaded area) in *half

Previous Example (target item is 11):



Clearly, with 1 comparison we can run binary search on a list of size n=1. So...

- 2 comparisons run binary search (worst case) on a list of size n=2
- 3 comparisons run binary search (worst case) on a list of size n=4
- 4 comparisons run binary search (worst case) on a list of size n=8
- n comparisons run binary search (worst case) on a list of size 2^(n-1)

Remember logs?

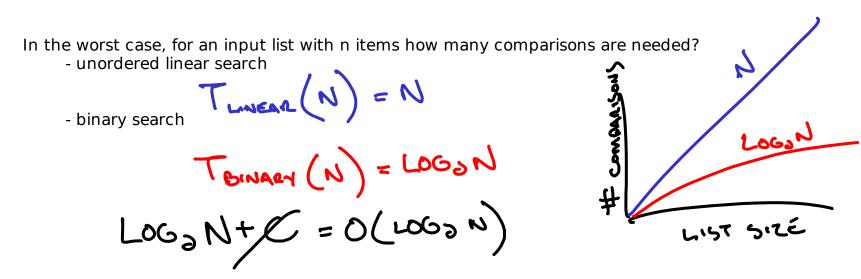
So how many comparisons, does binary search use on a list of size n, in the worst case?

Quantifying runtime:

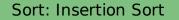
Runtime: how many "operations" required to complete algorithm for input of size n

To simplify our analysis of algorithms:

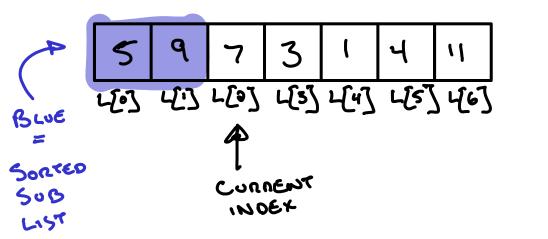
- lets only count comparisons (is item0 less than, equal to, or greater than item1?)
- lets assume the worst possible input for a given algorithm (requiring the most comparisons)



<insertion sort with cards>



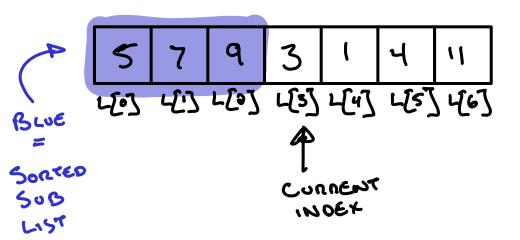




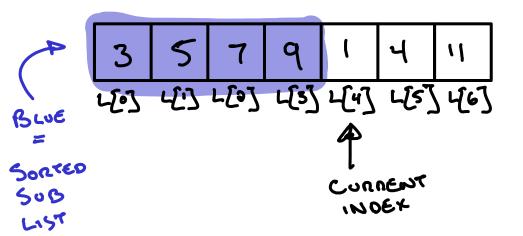


Intuition: add items, one-by-one, into a sorted sub-list (the first items in the list) Example:

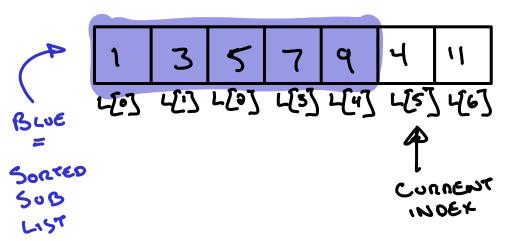
.



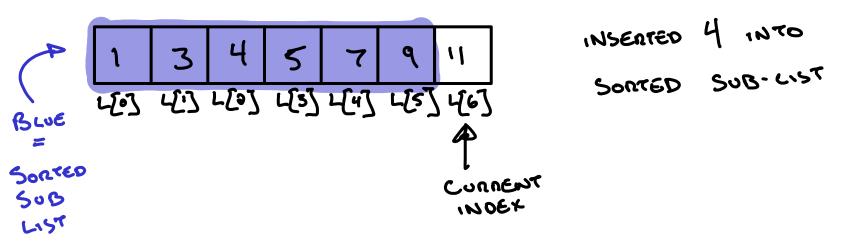


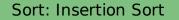


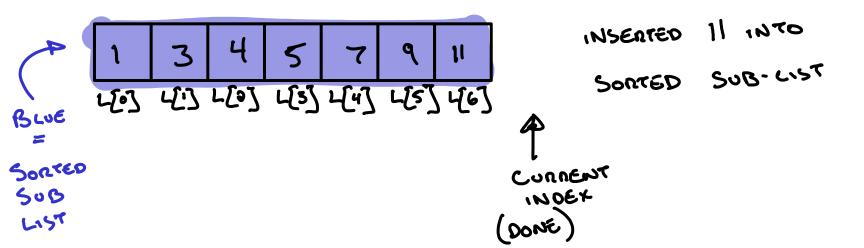










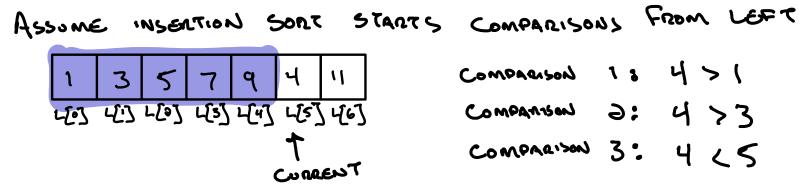


SHOWING INSERTION SORT ON HWG

Phase	Processed				\diamond	Unprocessed			
0	\diamond	34	16	12	11	54	10	65	37
1	34	\diamond	16	12	11	54	10	65	37
2	16	34	\diamond	12	11	54	10	65	37
3	12	16	34	\diamond	11	54	10	65	37
4	11	12	16	34	\diamond	54	10	65	37
5	11	12	16	34	54	\diamond	10	65	37
6	10	11	12	16	34	54	\diamond	65	37
7	10	11	12	16	34	54	65	\diamond	37
8	10	11	12	16	34	37	54	65	\diamond

EVENNTHING LEFT OF SYMBOL IS SOUTED In Class Activity

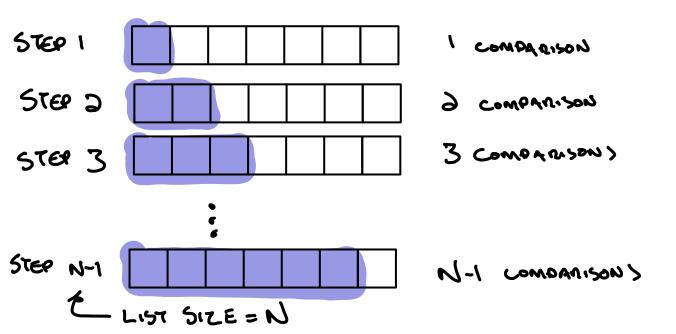
Build an input list of length 5 which requires as many comparisons as possible for insertion sort to complete.



(I'd love to take a response from you all to do with the cards, if you'd like please build your example with values 2,3,4,5,6)

Worst Case Analysis: Insertion Sort

In the worst case, each new item must be compared to all the previously sorted items.



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