CS 1800: day16

Admin:

- HW5 due Friday
- HW6 released Friday

Content:

- graph definitions & anatomy
- graph representation
 - list of lists
 - adjacency matrix
- graph equivilence (isomorphism)



More commonly, folks use the word "graph" to mean figure (as below). This is a different kind of graph. Many tech types use the word "figure" to describe these, no universal convention



Graph: Whats it good for?

Graphs are wonderful for representing things. Often, representing clearly is a big help!

Example: represent a maze as a graph.



Node = intersection in maze (start / end / dead-end too)

Edge = possible movement between intersections



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https://cdn.britannica.com/03/403-050-F1B9349F/Phylogeny-differences-cytochrome-c-protein-sequence-organisms.jpg



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GRAPH'S CAN BE DRAWN DIFFENTLY BUT ITS STILL SAME GRAPH





Warning:

There are a lot of terms referring to graph "stuff"

Most are super intuitive, but please double check definitions

Two nodes are adjacent in a graph if there is an edge between them.

AOJACENT: NOT ADJACENTI A, B A, C

A node and an edge are adjacent if the node is in the edge (remember, edge = pair of nodes)

Aozacent:
A,
$$\xi A, B, Z$$

Two edges are adjacent if one node is adjacent to both
Aozacent:
 $\xi A, O, Z$
 $\xi B, C, Z$
Not Aozacent:
 $\xi A, B, Z$
Not Aozacent:
 $\xi A, B, Z$
 $\xi A, B, Z$
Not Aozacent:
 $\xi A, B, Z$
 $\xi C, B, Z$

A node's degree is the number of edges which are adjacent to it





Draw a graph where the sum of degrees of all nodes is odd (or argue why this isn't possible)



- the sum of degrees for all nodes
 - the number of edges in the graph

Stuck? Draw some little examples until you have your own eureka moment (really, its fun!)





Z DEG = 4 2 EDUES











Rooted Tree - a tree (connected, acyclic graph) which has one special node identified as the root





CONVENTION

Root of TREE ON TOP

A (NOT RECCOMENDED FOR CHRISTMAS)

(useful fact about trees: there is a UNIQUE path between every pair of nodes)

Rooted Trees: Why go through the trouble?

Allows us to define family relationships:

parent of a node x: next node on path from x to root (root has no parent) ex: D is the parent of B

children of node x: the set of all nodes which x is parent of ex: {B, E} are children of D

a node is a leaf if it has no children: ex: A, C and E are leafs

sibling of node x: the set of all nodes which whose parent is also the parent of x

ancestor of x: all nodes on the path to root

descendant of x: all nodes which have x as an ancestor





tip: often thinking about a graph in terms of its connected components is fruitful for insights





Special Graphs:

Directed

Each edge has a direction



"DAG": Directed Acyclic Graph

Weighted

Each edge has a weight





a simple graph has no such edge

ok, lets take a breather ... that was a lot of new language ...

good news:

- only one more new graph vocab word today

- you needn't memorize anything, just take a peek back

not-so-good-news:

- graph language tends can have little inconsistencies per author (e.g. is a node its own ancestor?)

Two nodes are neighbors if they are adjacent (there is an edge between them) (note: definition assumes an undirected graph ... edges have no direction)



Graph Representation (on a computer): List Representation

Goal: represent all nodes & edges of a graph

Approach: For each node, store a list of all neighbors (convention: alphabetize)



Graph Representation (on a computer): Matrix Representation

Goal: represent all nodes & edges of a graph

Approach: Build $|V| \times |V|$ matrix (one row & col per node):

- 0 in row i and column j means node i and node j don't have edge between them

- 1 in row i and column j means node i and node j have edge between them



convention: alphabetize convention: a node is not its own neighbor Graph Representation (on a computer): Matrix Representation

Goal: represent all nodes & edges of a graph

Approach: Build $|V| \times |V|$ matrix (one row & col per node):

- 0 in row i and column j means node i and node j don't have edge between them

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convention: alphabetize convention: a node is not its own neighbor

In Class Activity:

Given the one representation of the graph, give its representation as the other two forms.

Forms of representing a graph:

- picture (as is most common in the notes)
- list representation on computer
- matrix representation on computer

NEIGABORS -A= [B] NEIGHBORS_B= NEIGNBORS_ BC



Э 0 0 0 0 C \square \mathbf{O} \odot C=[B,D] A=[E] D=[Bc]E=[A] ام ب

CDE

В

S

 \mathbf{C}

A

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D E



high level: two graphs are isomorphic if they have same shape



intuition: two graphs are isomorphic when we can "rename" the nodes of one to get another



"rename": one-to-one correspondance (i.e. bijection)